Development of a High Precision Infrasonic Sound Sensor

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Abstract

Infrasonic wave is the usually sound wave caused by vibrating body at frequency below 20Hz, which is commonly found in a variety of industry, transportation, nature and living environment. This paper designs a high precision infrasonic sound sensor based on PVDF, which is a new piezoelectric material of macromolecule with piezoelectric property. The research results proved that when a given frequency values between 3Hz to 30Hz, the proposed sensor has good performance and high precision, which could meet the design requirements, and has a certain practical value.

Keywords: PVDF, infrasonic wave sensor, signal process circuit

1. Introduction

Generally speaking, in the acoustic spectrum division, if the frequency of sound is lower than 20Hz, we call it infrasonic sound, which is made by vibrating and we human could not hear them because the frequency is beyond the limit of audibility [1, 2]. Infrasonic wave is real exiting in various natural, industrial, transportation and living environment. Such as bridge shaking, cars speed up, and even home stereo system. The infrasonic sound has characteristics of low frequency and long wavelength, these performances make it could spread far, with strong penetrating power and good anti-jamming. Therefore, the research on the infrasonic wave has become a hot topic recently in many countries, to design infrasound weapons, sound exploration [3, 4], natural disaster prediction [5, 6], medical [7] and so on. The initial research on infrasonic sound is upon weapons, primarily for military surveillance and weapons.

Early to 1990s, U.S. has developed military high-power micro infrasound weapons, and then put it into the simulated field test. In paper [8], the researchers proposed real-time infrasound data processing system based on FGPA (Field Programmable Gata Array), and the use discrete wavelet transforms (DWT) to build a high-pass and a low-pass filter.

Ham presents a classification system with performance results and associated confidence intervals (CIs) to sort four infrasound waves by using parallel RBF neural network [9].

In order to make best use of infrasonic wave signal in the application of forecast earthquake, paper [10] presents the software based on MATLAB software to analyze abnormal infrasound signal, which is very important to forecast earthquake. Shan, et al. presented an infrasound wave system to monitor the process of low carbon steel damage, which confirmed that during the damage phase, it will generate about 2Hz infrasound wave signal, by this method, the workers could find out the unqualified steel quickly [11].

Due to the wide range application of infrasonic wave, it is necessary to design an infrasonic sound sensor, which should have very high precision. However, the existing sound sensor to detect sound have some shortcomings, such as sensitivity to low
frequency range or big volume, which is not convenient to install and require higher environment. Therefore, in this paper, we proposed a smart and portable infrasonic sound sensor with high precision based on PVDF sensors. The rest of this paper is organized as follows. In Section 2, the methodology of design infrasonic sound sensor is introduced, which include the piezoelectric equation and mechanical equation. Section 3 presents the detail whole design for hardware circuit, which is consists of signal extraction module, normalized amplifying circuit, network filter and overload detection module. The results and analysis are given in Section 4. Finally, Section 5 concludes the paper.

2. Methodology

2.1. Piezoelectric Equation

Piezoelectric equation refers to the relationship between the mechanics upon the piezoelectric materials (such as stress tensor T, deformation tensor S) and electrical signal (such as electric field intensity E, electric displacement D). Currently, the most widely used is the first kind of piezoelectric equation, which is as shown in formula (1) and (2).

\[ S = s^E T + d^T E \]  \hspace{1cm} (1)

\[ D = dT + \varepsilon^T E \]  \hspace{1cm} (2)

Where, \( d = [d_{ij}] \), \( i=1,2,3 \); \( j=1,2, \ldots,6 \), which is piezoelectric constant matrix, \( \varepsilon^T \) is dielectric constant matrix when the stress remains unchanged, \( \varepsilon^E \) is flexible constant matrix when the electric field remains unchanged.

According to the Gauss theorem, we can obtain the equation of electric quantity of any free point on the surface of the electric field, the formula is as shown in Error! Reference source not found., and furthermore, the formula could be simplified as (4) if the size of PVDF is small.

\[ Q(t) = Q(t_0) + E_p + d_{31} \int_0^\omega Sd_\sigma d_{ij} \]  \hspace{1cm} (3)

\[ Q(t) = Q(t_0) + E_p d_{31} S_l t \omega \]  \hspace{1cm} (3)

Where, \( Q(t) \) and \( Q(t_0) \) are the surface electric quantity on the PVDF surface at \( t \) and \( t_0 \), respectively, \( S \) is the strain capacity along the drawing direction.

2.2 Mechanical Model

The elastic surface equation is as shown in formula(5), under the action of concentrated force \( F \) on the scope of the small deflection.

\[ \varepsilon_r = \frac{1}{E} (\sigma_r - \mu \sigma_t) = \frac{3F}{E 2\pi h r^2} \left( 1 - \mu^2 \right) \left( \ln \frac{R}{r} - 1 \right) \]  \hspace{1cm} (4)

Where,
- \( \mu \) is the Poisson’s ratio of material
- \( \omega \) is the deflection of the diaphragm
- \( F \) is the force on the diaphragm
- \( h \) is the thickness of the diaphragm
- \( E \) is the material elastic modulus
- \( r \) is the distance to the diaphragm center
- \( R \) is the radius of diaphragm

We could get the maximum deflection of the diaphragm when \( r=0 \), and the simplified equation is as shown in Error! Reference source not found..
\[ \omega_0 = \frac{3(1-\mu^2)FR^2}{4\pi Eh^3} \]  
\[ \omega_{r=R} = -\frac{3F}{2\pi h^2} \]

When \( r=R \), the simplified equation is as shown in (7).

According to the distribution of concentration on the small area, we could get the maximum stress, the corresponding strain formulas are as follows:

The radial stress and strain is as shown in equation (8).

\[ \omega_r = \frac{3(1-\mu^2)}{4\pi} \frac{1}{Eh^3} \left( R^2 - r^2 + 2r^2 \ln \frac{r}{R} \right) F \]  
\[ \varepsilon_r = \frac{1}{E} \left( \sigma_r - \mu \sigma_\theta \right) \]  

3. Signal Processing

3.1 Overall Design

Figure 1 shows the whole design of signal process circuit, it is consists of three main parts, first is signal extraction part, which extracts weak electric signals from PVDF sensor, and then the second part is normalized amplifying circuit, which is in charge of amplifying the signal to a definite range, after that, the signal will be sent to a network filter, which is made up of high-pass filter circuit and low-pass filter circuit. Furthermore, we design an overload detection module to monitor system ensure it is in normal condition. The details of these modules will be introduced below.

3.2 Normalized Amplifying Circuit

Due to the sensitivity of the sensor is not the same, if we use different sensors, the output voltage generated by the amplifying circuit is also different. In order to control the output voltage within a certain range, it is essential to design a normalization amplifying circuit, which is as shown in Figure 2. R12 is a digital potentiometer, which is controlled by the microcontroller, besides that, R14 is a trimming potentiometer. The gain K of normalized amplifying circuit is shown as in formula (10), it is easily seen that, if we adjust the R12 and R14 to the appropriate value, and we will be able to get a match with the designed sensor gain value.

\[ K = \frac{U_{O3}}{U_{O2}} = \frac{R_{13} + R_{14}}{R_{12} + R_{11}} \]
3.3 Filter Circuit

The filter circuit is one of the most important modules to get the precision of the measurement. Hence, the design of the filter circuit is very important. The filter circuit consists of two parts, one is the high-pass filter circuit, and the other is low-pass circuit. Low-pass filter circuit in the system will only make the signal pass, whose frequency is lower than cut-off frequency, and filter out the signal, whose frequency is higher than cut-off frequency. On the other hand, the function of high-pass module is on the contrary. The combination of low-pass circuit and high-pass-circuit could control select the signal we want to reserve.

The circuit of low-pass module is designed by MAX293, which is a programmable low pass filter. First, we will use microcontroller to measure the frequency of input signal and then, by controlling the analog switch to achieve frequency filtering. The circuit of high-pass module is shown as in Figure 3, where C24, R15, U5 constitute a first-order RC high-pass filter, which will filter the DC component in the input signal, the cut-off frequency of high-pass module is calculated by equation (11).

\[ f_h = \frac{1}{2\pi R_{15}C_{24}} \]  

(9)

3.4 Overload Detection Circuit

In order to ensure that the output signal is not distortion, we designed the overload monitoring module and the circuit is as shown in Figure 4. The operating principle of overload detection circuit is to monitor the amplifier by microcontroller, when the output signal is beyond a certain range, overload indicator light will be lighted, which implies the circuit is overload.
Figure 5 shows the specific working process of overload detection circuit as follows:

1. $U_i$ is greater than $U_1$, $D_1$ is cut-off, and $D_2$ is turn-on, the output signal, $U_o$ is high level;

2. $U_i$ is lower than $U_2$, $D_1$ is turn-on, and $D_2$ is cut-off, the output signal, $U_o$ is high level;

3. $U_i$ is between $U_1$ and $U_2$, both $D_1$ and $D_2$ are turn-on, and the output signal, $U_o$ is low level;

![Figure 5. Output Waveform of Detection Circuit](image)

4. Results and Discussions

The aim of this part is to verify the performance of infrasonic sound sensor designed in this paper, and the experiment could be divided into two parts. The first part is generating infrasonic sound, which is done by signal generator, and the signal is 1~20Hz sine wave. On the other hand, the other part is receiving the infrasonic sound, which is done by proposed system in this paper.

In order to make the measurement results more convincing, we extend the frequency of generating signal from 1~20Hz to 1~34Hz, and besides that, we take the average method to get more precision data, the calculation formulas of frequency and voltage of signal is as shown in the equation (12) and (13), respectively.

\[
\bar{f} = \frac{1}{n} \sum_{i=1}^{n} f_i \quad (10)
\]

\[
\bar{U} = \frac{1}{n} \sum_{i=1}^{n} U_i \quad (11)
\]

The measurement results are as shown in Table 1. In order to analyze the results, Figure 6 are presented, which shows the change curve of output frequency of infrasonic sound sensor along with real frequency of signal generated by signal generator; and Figure 7 shows the output voltage of proposed system along with real frequency of signal generated by generator.

<table>
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<tr>
<th>No.</th>
<th>O-F /Hz</th>
<th>M-F /Hz</th>
<th>M-V /mV</th>
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<td>1</td>
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<tr>
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From Figure 6, we can see that, first when the frequency is below 3Hz, the output frequency of sensor is clearly not right, with the output results is 0.2Hz according to 1Hz, and 0.5Hz according to 2Hz. This implies the lower limit frequency of this proposed infrasonic sound sensor is 3Hz. Secondly, when the input frequency is higher than 30Hz, the output frequency decrease sharply and down to zero, the reasons for this phenomenon are consists of two parts, one is the higher limit frequency of sensor is about 30Hz, and the other reason is that the cut-off frequency of low-pass filter circuit is designed at 30Hz. Thirdly, when the frequency is between 3Hz and 30Hz, the output results show perfect linearity, which suggests that the designed sensor is success.

![Figure 6. Measurement of Output Frequency](image)

The same conclusion could be got through Figure 7, when the frequency is lower than 3Hz of higher than 30Hz; the output voltage is almost zero. Otherwise, the change curve of voltage is slowly rising with frequency. It is could be drawn a conclusion that:

(1) The low limit frequency of infrasonic sound sensor proposed in this paper is 3Hz.
(2) The high limit frequency of infrasonic sound sensor proposed in this paper is 30Hz.

Figure 7. Measurement of Output Voltage

Figure 8 shows the error of measurement frequency according to the equation Error! Reference source not found. From Fig.8, it is can be seen that the value of measurement error is big when the frequency below 3Hz or high 30Hz. Furthermore, the error changes small along with the increasing of frequency and the average error between 3Hz and 30Hz is 1.78%, which suggest the precision of this system is very good.

$$e_i = \frac{f_i - M_i}{M_i} \times 100\% \tag{14}$$

Figure 8. Measurement Error of Frequency

Besides the error, we import two evaluation indexes, the first is frequency linearity, which is calculated by equation Error! Reference source not found., and the other is voltage sensitivity, which is calculated by equation Error! Reference source not found..

$$e_L = \pm \frac{\Delta L_{\text{max}}}{y_{FS}} \times 100\% \tag{15}$$

Where, $\Delta L_{\text{max}}$ is the max vertical value between output frequency and real frequency in Figure6, the valid frequency range is from 3Hz to 30Hz definitely, $y_{FS}$ is the theoretical max measurement range, and the value of $y_{FS}$ is 30Hz. It is can be found that $\Delta L_{\text{max}}$ is 0.7Hz, so the frequency linearity $e_L$ is 2.25%. By the same method, we could get the voltage linearity is 2.64%.

$$K = \frac{\Delta y}{\Delta x} \tag{16}$$

Sensitivity is the ratio between output increment and input increment, which is the slope when the situation is linear system. So the voltage sensitivity of this system could be got as:

$$K = \frac{17.77 - 12.12}{30 - 3} = 0.135 \text{mv/Hz}$$
5. Conclusion
The experiment results show that the developed infrasonic sound sensor based on PVDF in this paper has good performance and high precision, furthermore it has advantage of light structure, strong anti-jamming capability, stability, which makes it could meet the design requirements, and has a certain practical value. Following are main conclusions of this paper:
(1) The frequency range of designed infrasonic sound sensor is from 3Hz to 30Hz.
(2) When a given frequency values between 3Hz to 30Hz, the voltage steady increase slowly, illustrate the sensor works stability and can meet the design requirement.
(3) The frequency error is 1.78% and frequency linearity is 2.25%.
(4) The voltage linearity is 2.64%, and voltage Sensitivity is 0.135mv/Hz.

References

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