

# Image Denoising Method based on Threshold, Wavelet Transform and Genetic Algorithm

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## Abstract

*In the process of image acquisition and transmission, noise is always contained inevitably. So it is necessary to image denoising processing to improve the quality of image. Generally speaking, each algorithm has some filtering and threshold parameters. Taking variety kinds of images into account, it is a key problem of how to set these parameters in denoising algorithms under different conditions to achieve better performance. There are many algorithms for the determination of the parameters, and each of them has its application field. Because the wavelet transform has good performance, therefore, it has been widely applied as a kind of signal and image processing tools. In this paper, wavelet transform is used in the image denoising, and the genetic algorithm is used to estimate the denoising results. Experimental results show the validity of the new algorithm.*

**Keywords:** image denoising, threshold, wavelet transform, genetic algorithm

## 1. Introduction

In the process of image acquisition and transmission, noise is always contained inevitably. So it is necessary to image denoising processing to improve the quality of image. Much practical noise can be approximated as white noise with Gauss distribution, and removal of superposition of Gauss white noise has become an important direction in image denoising research. Generally speaking, each algorithm has some filtering and threshold parameters. Taking variety kinds of images into account, it is a key problem of how to set these parameters in denoising algorithms under different conditions to achieve better performance.

Simple linear smoothing filter, such as Gauss filter [1-3], will cause the detail information loss of image. In recent years, a large number of complex denoising algorithms mean of nonlinear filter has appeared. Common algorithms include a variety of adaptive median filter algorithms: the wavelet threshold [4-8] (also called wavelet shrinkage) algorithm, the anisotropic diffusion equation algorithm [9-12], the total variation minimization algorithm [13-16], non-local mean filter algorithm [17-20], etc.

At present, the noisy image restoration methods are mainly as the following three:

### (1) Mean Filter Principle

Mean filter is also known as the linear filter, and the main methods are the neighborhood average method. The basic principle of linear filtering is to replace the original image pixel values with mean values. That is to say, for the current pixel  $(x, y)$ , we should select a template, which is composed of a plurality of pixels in its neighbor. Mean values for all pixels would be calculated and the give the mean values to the current pixel  $(x, y)$  as the gray  $g(x, y)$  in the points on the process image. This means:

$$g(x, y) = \frac{1}{M} \sum_{f \in s} f(x, y) \quad (1)$$

Where,  $s$  means template, and  $M$  is the total number of pixels including current pixel the template.

Mean filter using neighborhood average method is applicable to remove granular noise in the scanning image. Neighborhood average method effectively suppresses the noise. But during the process of calculating the average value, scenery edge points would be processed too. Then, the image would be in the state of low resolution. Based on this situation, the improved algorithm is proposed to realize various mean filters, and new mean filter is developed, such as weighted mean filter, gray minimum variance mean filter,  $K$  nearest neighbor mean filter, symmetric neighbor mean filter and so on. When these filters are working, scene boundary smoothing is avoided, and it can greatly reduce the fuzzy image.

### (2) The Median Filter

The median filter is a kind of effective noise suppression of nonlinear signal processing technology based on the order statistical theory. The basic principle of the median filter is a sample value replaced with the median value of points in neighborhood point set. Pixel gray value, which is different with surrounding pixel gray values, would be replaced by the close value with the neighborhood points. Then, isolated noise points would be removed. The main idea of the method is establishing a two-dimensional sliding template, in which the pixel values would be ordered by size. Two-dimensional data sequence would be generated monotonically increasing (or down). Two dimensional median filter output is  $g(x, y) = \text{Med}\{f(x-k, y-l), (k, l) \in W\}$ . Where,  $f(x, y)$  and  $g(x, y)$  are the original images and the processed images.  $W$  is a two-dimension template with usually  $3 \times 3$  or  $5 \times 5$  area, and it can be in different shapes, such as linear, circular, figure ten, ring, etc.

Median filtering is a nonlinear filtering technique. The advantage of the median filter is simple operation and faster speed, and it has excellent performance in filtering adding white noise and long tail noise. But for some more details, especially for a point, line and multi spire image should not use median filtering. In order to expand the scope of its application, the median filter has many improved algorithms, such as weighted median filter, switching median filter algorithm based on threshold, and adaptive median filter. In the weighted median filter, pixels within the window are to assign different weights to adjust the contradiction between noise suppression and detail preservation. However, the method obtains more effective detail preserving ability at an expense of noise suppression compared with a traditional filter. In switching median filter algorithm, it is based on threshold and gets the better effect by median filter for noise point and the flat region. This algorithm does not deal with the details in order to obtain good protection effect. For adaptive median filter, it can be used to deal with a high probability impulse noise. When it is processing, its neighborhood region can be changed rely on a certain condition. Its advantage is saving details in processing the smooth non impulse noise.

### (3) Wavelet Transform

Wavelet transform is a time-frequency analysis method with fixed window size and varied shape with time. Principle of removing noise by wavelet transform is that the noise mostly belongs to the high frequency information. Therefore, noise information is mostly concentrated in sub blocks with infra-low frequency, infra-high frequency, and high frequency. Sub blocks with high frequency are almost composed of noise information. Therefore, if we set high frequency sub block to zero and suppress low frequency and high frequency sub blocks on certain inhibition, it can achieve a certain effect of the noise

removal. Usually the image denoising processing based on wavelet method is as the following: wavelet transform; threshold of wavelet detail coefficients; reconstruction.

The principle of the wavelet denoising shows that wavelet transform is fit for removing the image with a high frequency signal. Now, the wavelet transform is often used to remove the white Gauss noise. Due to the characteristic of multi-resolution analysis of wavelet transform, it can be put in the signal and noise in different frequency domain to recognize them. For the signal, wavelet denoising is a signal filtering problems. Although largely wavelet denoising can be seen as a low pass filter, it is still better than the traditional low pass filter due to the retaining of the image feature after denoising. Thus, wavelet denoising is actually a comprehensive feature extraction and low passes filter function.

Generally speaking, each algorithm has some filtering and threshold parameters. Due to the variety of the image content, how to set these parameters for denoising algorithms to achieve a better performance under different conditions is a key problem.

In research image denoising method, many algorithms have been developed, such as adaptive wavelet transform with soft threshold denoising algorithm [21], algorithm of systolic function considering the gradient, scale and spatial geometric consistency information into consideration in in adaptive process [22], adaptive wavelet transform with two step variance adaptive algorithm and local variance and balanced multi wavelet coefficient model [23], multivariate generalized Gauss model [24], estimation of threshold parameter with correlated noise and the edges of the image [25], steerable wavelet reconstruction algorithm [26], and so on.

Because the wavelet transform has good local character, therefore, it has been widely applied as a kind of signal and image processing tools.

Since the concept of wavelet threshold has been proposed, because it can obtain the optimal estimate in the Besov space and other linear estimators cannot get the same result, much attention has been paid on it. Wavelet thresholding is a nonlinear method, and denoising purpose can be achieved according to the process of wavelet coefficients in the wavelet domain. Its theoretical premise is coefficients of the image followed Gauss distribution, and wavelet coefficient with absolute larger magnitude is mainly obtained from the transformed signal and wavelet coefficient with absolute smaller magnitude is mainly obtained from the noise signal transformed. Then we can clear the noise by setting a threshold.

In this paper, wavelet transform is used in the image denoising, and the genetic algorithm is used to estimate the denoising results. The main contribution of the paper is to the proposal of an algorithm for image denoising. And the remainder of the paper is shown as the following: Threshold determination is listed in Section 2. Experimental verification is shown in Section 3. And the conclusion is described in Section 4.

## **2 Threshold Determination**

### **2.1 Wavelet Transform Denoising**

When the useful signal is transformed by wavelet, the energy will concentrate on the small number of wavelet coefficients. At the same time, noise will be distributed on the entire time axis at all-time scales due to the not related wavelet coefficients. In the processing, other points value will be set as zero or reduced maximum, and the processed wavelet would be inverse transformed. Then, noise will be suppressed.

Threshold denoising is based on the comparison of transform domain coefficients and threshold value, and processed coefficient should be transformed to reconstruct the denoising image. Concrete steps of wavelet threshold denoising method are shown as the following:

Step 1: wavelet decomposition of the image: Determine the wavelet function and decomposition levels  $N$ , and decompose the image with  $N$  layer wavelet.

Step 2: Threshold selection: select the threshold for each wavelet coefficients of each layer, and judge the threshold of detail coefficients.

Step 3: Image reconstruction: coefficient with threshold processed will be used to reconstruct the image by inverse wavelet transform.

The signal and noise have different correlation in wavelet domain. The wavelet coefficients of the signal have a strong correlation at the corresponding positions, while the coefficients of the noise are weakly related or not related. Scale correlation denoising is using different correlation characteristics of the image signal and noise in wavelet transform domain. Comparing the two denoising algorithms, they adopt different approaches to wavelet coefficients. Threshold denoising uses the “horizontal” process method. It firstly selects the threshold, and then compared to the wavelet coefficients.

In the threshold denoising method, due to the fixed threshold, it will not change with the wavelet coefficients, which leads the inevitably error on the part of the wavelet coefficients. When the threshold is properly selected, most error coefficients will appear in the neighborhood of threshold. In the adjacent region of the threshold, there will be less error wavelet coefficients according to scale correlation estimation. So, scale correlation estimation method used for the wavelet coefficients can reduce the error and improve the accuracy of the wavelet coefficient threshold judgment. There is no doubt that it will be more effectively for image denoising.

## 2.2 Threshold Correction

In the process of wavelet threshold denoising, threshold should be estimated, and the general threshold calculation method can be described as the following:

$$\delta = \sigma \cdot \sqrt{2 \ln(n)} \quad (2)$$

Where,  $\sigma$  is the noise standard deviation,  $n$  is the length of sampling signal. The universal threshold formula may appear the phenomenon of “killing” in the denoising process, then some image edge details would be lost. In order to protect the image edge details, it should introduce a shrinkage factor in general the threshold formula. However, if the shrinkage factor value is too small, the threshold would be small too. When the wavelet coefficient threshold is applied, the noise component will be contained too much, and it cannot be an effective denoising. Some methods have been proposed to solve the problem. For example, denoising threshold for ground penetrating radar (GPR), the threshold would be as the following:

$$\delta = \sigma \cdot \sqrt{2 \ln(n)} / (1 + \lg j) \quad (3)$$

Where,  $j$  is the level of decomposition. For the characteristics of infrared image, wavelet coefficients for signal are small, and the threshold determined by the threshold formula would be smaller. In order to keep the infrared image denoising effect, the shrinkage factor should not be too small. Then the modified function has been proposed and the mathematical expressions are shown as the following:

$$\delta_{new} = \delta \cdot \exp(-1 + \frac{1}{N}) \quad (4)$$

Where,  $\delta_{new}$  is the threshold determined by the threshold correction method,  $N$  is the total number of layers, and  $\delta$  is the threshold calculated by universal threshold formula.

## 2.3 New Threshold Functions

In the process of denoising, wavelet coefficient should be processed. There are mainly two methods to process: hard thresholding and soft thresholding. Equation (5) and equation (6) are hard thresholding function (Hard-TF) and soft threshold function (Soft-TF), respectively. Both the equations are described as the following:

$$\omega_{\delta} = \begin{cases} \omega, & |\omega| \geq \delta \\ 0, & |\omega| < \delta \end{cases} \quad (5)$$

$$\omega_{\delta} = \begin{cases} \text{sgn}(\omega) (|\omega| - \delta), & |\omega| \geq \delta \\ 0, & |\omega| < \delta \end{cases} \quad (6)$$

Where,  $\delta$  is the threshold,  $\omega$  is the magnitude of the wavelet coefficients, and  $\omega_{\delta}$  is the wavelet coefficient which is processed with threshold. Although the hard threshold is the natural choice and it can preserve the image edge details, the hard threshold function is discontinuity and it would cause ringing and pseudo Gibbs effect when used in the denoising. For the image soft thresholding, due to the inherent deviation, it may cause the defect image fuzzy. Aiming at the defects of hard threshold and soft threshold function, a comprehensive treatment method, which named half thresholding function (Half-TF) has been proposed. It can be described as the following:

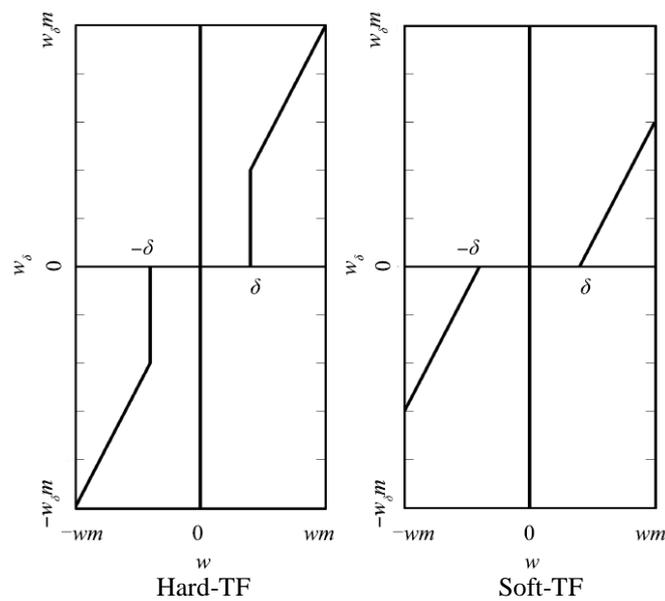
$$\omega_{\delta} = \begin{cases} \text{sgn}(\omega)(|\omega| - \alpha \cdot \delta) & |\omega| \geq \delta \\ 0, & |\omega| < \delta \end{cases} \quad (7)$$

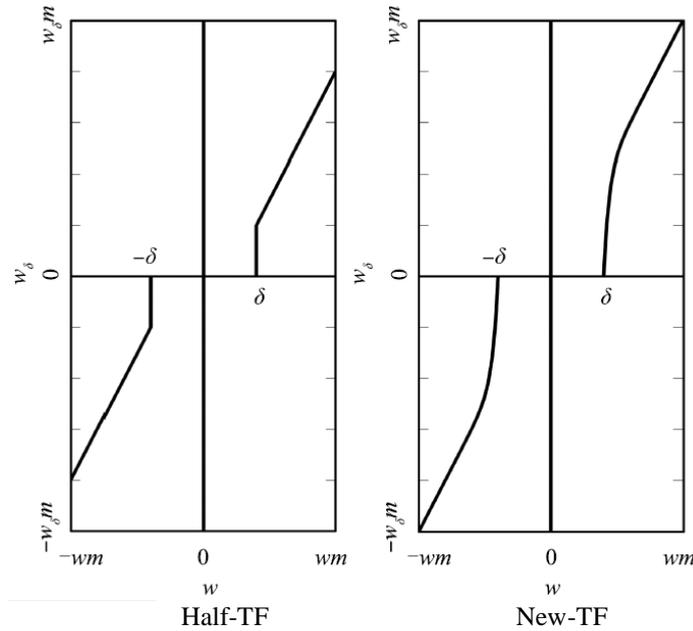
Where,  $\alpha$  is between the range of 0~1. Wavelet coefficients calculated by the Half-TF is between that calculated by the hard and soft threshold method. It can improve the estimate, fuzzy ringing, pseudo Gibbs effect, other visual distortion and edge phenomenon. However, parameter  $\alpha$  in the actual operation is often a constant and the method is not adaptive. So, there will still be the inherent deviation and discontinuous phenomenon.

Aiming at the existing defects of hard threshold function, soft threshold function and half threshold function, reasonable threshold function should meet some requirements: (1) input and output curves should be continuous and it should be relatively smooth in treatment to reduce the ringing, pseudo Gibbs effect; (2) wavelet coefficients for signal should be remained basically unchanged to properly preserve the image edge details. Therefore, based on the half threshold function, parameter  $\alpha$  should be adaptive, and it can be changed according to the different wavelet coefficients. When  $|\omega|$  value is small and close to the threshold, parameter  $\alpha$  would be close to the value of 1 to have characteristics of soft threshold function. It will reduce ringing, pseudo Gibbs effect. When  $|\omega|$  value is increasing, parameter  $\alpha$  would be rapidly approaching 0, which has the characteristic of hard threshold function and preserve image edge details. The exponential function can meet this demand. Adaptive is achieved according to the comparison between  $|\omega|$  and  $\delta$ . In order to make the threshold function can be extended, an adjustable parameter will be introduced in the exponential part. That is the new threshold function which is with adaptive features.

$$\omega_{\delta} = \begin{cases} \operatorname{sgn}(\omega) \left( |\omega| - \frac{\exp(\beta \cdot \delta)}{\exp(\beta \cdot |\omega|)} \delta \right) & |\omega| \geq \delta \\ 0, & |\omega| < \delta \end{cases} \quad (8)$$

Where,  $\beta$  is in the range of non-negative. Different values of  $\beta$  would affect the property of new threshold function, of which two kinds of extremes are  $\beta = 0$  and  $\beta \rightarrow \infty$ . When  $\beta = 0$ , the new threshold function is converted into a soft threshold function, and when  $\beta \rightarrow \infty$ , the new threshold function into the hard threshold function. In the extreme conditions, the new threshold function has no help to overcome the defects of soft threshold function or hard threshold function, so  $\beta$  in the new threshold function should be given a moderate value. When the value is given, the new threshold function can be carried out according to different treatment on the size of the wavelet coefficient. When the  $|\omega|$  is small, the new threshold function is similar with soft threshold function, and when the  $|\omega|$  is big, the new threshold function is similar with hard threshold function.





**Figure 1. Threshold Function**

Figure 1 shows the comparison of different threshold function.  $w$  axis means wavelet coefficients  $w$ ,  $w_m$  is the maximum of  $w$ .  $w_\delta$  axis represents  $w_\delta$  which is wavelet coefficient applied with threshold.  $w_\delta m$  is the maximum of  $w_\delta m$ .  $\delta$  is the threshold. According to the comparison, we can discover the new threshold function satisfies the input-output curve continuous, and wavelet coefficients of the signal remained basically unchanged.

## 2.4 Modified Threshold Denoising Algorithm

The improved threshold based improved wavelet denoising of infrared image can be divided into some steps:

Step 1: Wavelet decomposition: decomposition of the image with  $N$  layers wavelet discretion;

Step 2: Threshold processing: modified threshold processing scheme will be used to determine the threshold size, and new threshold function would be used to deal with the wavelet coefficients;

Step 3: Image reconstruction: reconstruct the image by inverse wavelet transformation.

## 2.5 Genetic Algorithm in Image Processing

(1) Basic principle of genetic algorithms used in image processing

Genetic Algorithm [21-25] is a method simulated with evolutionary of self-existence and fittest survival. It is repeated use the basic operation in genetics to continuously create new group for the population may contain the solution. It is in a style of continuous evolution of the group and with global parallel search technique in the optimization for the best individual to get the solution which meets the requirements. Genetic algorithm is simple, robust, and with prominent characteristics of self-organization, self-adaptive, self-learning and parallel in essence. In image denoising process, it is expected to get the denoising image, which contains all the information of the original image. That is to say that getting the optimal denoising image. In the paper, genetic algorithm is also taken into the threshold determination to find the optimal threshold. According to the comparison between denoised image and the original image, best threshold processing results would

be determined. But both the two images are unknown, so it is still difficult to determine the optimal value. However, the noisy image  $x(T)$  is the original image of  $s(T)$  generated after the noise pollution, therefore the denoised image can be used to generate another noisy image according to same pollution process. The noisy image generated would be compared with the initial noisy image. The compared method can be described as:

$$E(s_t) \approx \|x - x(T)\|^2 \quad (9)$$

When the comparison result is quite small, we will get the best denoising image. From the perspective of genetic algorithm, the smaller  $E(s_t)$ , the higher image fitness the individual represents. The process of the denoising process is the minimize value of  $E(s_t)$ .

In the use of a genetic algorithm to find the optimal denoising image, initial population which contains initial solution should be firstly produced. Traditional genetic algorithm generates the initial population by a random form. It not only slows down the convergence speed of evolution, but also greatly increased the computing time. In the algorithm, we will firstly evaluate the initial population and encoding, and then genetic manipulation for the group. The sequence of the process would be as the following: selection, crossover and mutation operator. Selection principle is elimination of lower fitness individuals and retains high fitness individuals until to get the final optimal solution

(2) Optimal threshold selection for wavelet transform based on genetic algorithm

In the search process of the genetic algorithm, evaluation function is used to evaluate individual. The evaluation results would be taken as a basis for future operation. This evaluation function is determined by:

$$E(s_t) \approx \|x - x(T)\|^2 \quad (10)$$

Selection or copy operation is designed to choose excellent individuals from the current population, so that they have the opportunity as a parent for the next generation. The fitness value is the criterion used to evaluate the individual quality. Higher individual fitness is the greater chance of survival.

### 3. Verification

We calculated two typical images for the denoising process. The results are shown in Figure 2 and Figure 3.



(a) Original image

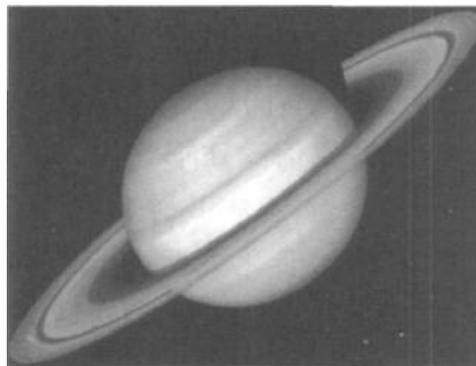


**(b) Image with noise**

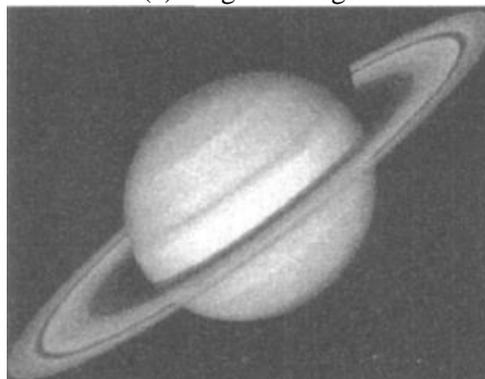


**(c) Denoising image**

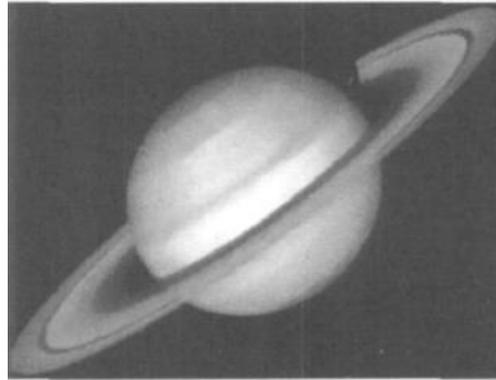
**Figure 2. Image 1 with Denoising Process**



**(a) Original image**



**(b) Image with noise**



(c) Denoising image

**Figure 3. Image 2 with Denoising Process**

**Table 1. Comparison of Signal-to-noise Ratio with Different Noise Intensity by Different Methods-image 1**

Image 1	Noise level	Traditional method	New algorithm
	20	31.3683	32.0127
	25	29.13	29.98
	30	27.3265	28.76

**Table 2. Comparison of Signal-to-noise Ratio with Different Noise Intensity by Different Methods-image 2**

Image 2	Noise level	Traditional method	New algorithm
	20	31.3683	32.2083
	25	29.13	30.12
	30	27.3265	29.01

From the Table 1 and Table 2, we can find that the new algorithm has better performance in denoising process for image.

#### 4. Conclusion

It is necessary to image denoising processing to improve the quality of image. Much practical noise can be approximated as white noise with Gauss distribution, and removal of superposition of Gauss white noise has become an important direction in image denoising research. Since the concept of wavelet threshold has been proposed, for its optimal estimate in the Besov space, much attention has been paid on it and various algorithms based on it have been developed. Wavelet thresholding used for denoising is according to the adjustment of wavelet coefficients in the wavelet domain. Then we can clear the noise by setting threshold.

In this paper, wavelet transform is used in the image denoising, and the genetic algorithm is used to estimate the denoising results. Two typical images are used to verify the validity of the new algorithm, and the results show that the new algorithm can improve the signal to noise ratio compared with the traditional algorithm.

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