

# An Improved Secure Dynamic ID Based Remote User Authentication Scheme for Multi-Server Environment

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## Abstract

Recently, Lee et al. proposed a secure dynamic ID based remote user authentication scheme for multi-server environment. They claimed their scheme can remedy the weaknesses of prior schemes and is thus more effective. However, we find Lee et al.'s scheme still fails to achieve the anonymity and has the security weakness of a smart card clone. In this article, we shall propose a new scheme to improve Lee et al.'s scheme. Our scheme not only overcomes the weaknesses of Lee et al.'s scheme, but also maintains a high efficiency standard.

**Keywords:** Anonymous, authentication, dynamic ID, multi-server, key agreement

## 1. Introduction

Today, network services are a popular issue, because increasingly more services are being provided. When we want to access information or ask something from the server, first we need to log on to the server. Therefore, we need an authentication scheme for network servers to authenticate the legitimate users. However, the Internet now is a public environment, anyone can intercept messages of communication between users and servers from the Internet. In order to protect users' secrets, schemes related to maintaining the security of user authentication is becoming more and more important nowadays [1, 6].

In 2004, Das et al. proposed a dynamic ID-based scheme to solve user tracking problems [2]. However, in 2005, Liao et al. pointed out that Das et al.'s scheme cannot protect against guessing attacks and achieve mutual authentication [5]. In 2009, Liao and Wang proposed a new authentication scheme with anonymity for a multi-server [7]. Their scheme only uses one way hash functions to improve efficiency. But Hsiang and Shih pointed out Liao and Wang's scheme cannot withstand insider attacks, masquerade attacks, server spoofing attacks, and registration center spoofing attacks in the same year [3]. To overcome the weaknesses of Liao and Wang's scheme, Hsiang and Shih proposed their scheme. Nevertheless, in 2011, Lee et al. found Hsiang and Shih's scheme still could not overcome masquerade attacks, and server spoofing attacks [4]. In addition, they proposed an improved scheme to solve the weaknesses of Hsiang and Shih's scheme. Lee et al.'s scheme let registration center share a secret value with a legal server to compute the legal user's secret value. In their paper, they claimed their scheme is practicable in the future. However, we find Lee et al.'s still scheme fails to achieve the anonymity and has security weakness of a smart card clone. To solve these problems of

anonymity authentication, we propose an improved scheme in this paper, which is more effective and secure than the others.

## 2. Review of Lee et al.'s Scheme

In this section, we will review the Lee et al.'s scheme. Three roles participate in this scheme: the registration center (RC), the remote server (S), and the User (U). The RC chooses a master key  $x$  and secret value  $y$  to compute  $h(x//y)$  and  $h(y)$ . After that, RC shares  $h(y)$  to registered server (S). User (U) registers at RC and login S, which registers at the same RC, to access resources. The scheme is divided into four phases: registration phase, login phase, verification phase, and password change phase. To shorten the length of this paper, we omit the review. Please refer to [4].

## 3. Cryptanalysis of Lee et al.'s Scheme

In this section, we will show the weaknesses of Lee et al.'s scheme that fails to achieve the necessary anonymity, and the situation is a high-risk when the information of the smart card is disclosed. In addition, their mechanism for changing a password is not really friendly. We will assume that the communication between  $U$  and  $S$  is eavesdropped on by an adversary  $Z$ , and explain how the adversary  $Z$  can attack Lee et al.'s scheme.

### 3.1. Fails to Achieve the Anonymity

When a legal user  $U_i$  wants to access roaming services from server  $S_j$ , he/she must send  $\{CID_i, P_{ij}, Q_i, N_i\}$  to  $S_j$ . If the adversary  $Z$  is another legal user who registers at the same  $RC$  with  $U_i$ ,  $Z$  can derive a unique value of  $U_i$  and trace  $U_i$  by the value at this moment. Because  $Z$  registered at the same  $RC$  with  $U_i$ , he/she also has the value  $h(y)$ . After intercepting  $\{CID_i, P_{ij}, Q_i, N_i\}$ ,  $Z$  can compute  $T_i = P_{ij} \oplus h(h(y)||N_i||SID_j)$ ,  $A_i = h(T_i||h(y)||N_i)$ , and  $h(b \oplus PW_i) = CID_i \oplus h(T_i||A_i||N_i)$ .

Because the unique value  $h(b \oplus PW_i)$  of  $U_i$  doesn't change frequently,  $Z$  can trace  $U_i$  by this unique value. For this reason, we can know that Lee et al.'s scheme fails to achieve the really anonymity.

### 3.2. Smart Card Clone

In Lee et al.'s scheme, the security is based on the secure value  $B_i$ . In both user authentication or session key establishment,  $B_i$  always plays an important role. However, this important value is not stored securely in the smart card. If the adversary  $Z$  is another legal user who registers at the same  $RC$  with  $U_i$  and if he/she temporarily possesses the smart card of  $U_i$ ,  $Z$  can easily obtain  $B_i$  and uses it to attack the system, such as by re-establishing the session key  $SK$ , which is established by  $B_i$ ,  $N_i$ ,  $N_j$ ,  $A_i$ , and  $SID_j$  to decrypt those cipher-text. Because  $\{N_i, N_j, SID_j\}$  can be intercepted from the public network environment, and as  $A_i$  can be derived as section 3.1 mentioned,  $Z$  can implement a man-in-the-middle attack and masquerade an attack as follows.

### 3.3. Man-in-the-middle Attack

If  $Z$  obtains  $B_i$ ,  $Z$  can execute a man-in-the-middle attack with processes as follows.

**Step ZV1:**  $Z$  intercepts  $\{CID_i, P_{ij}, Q_i, N_i\}$  and computes  $\{T_i, A_i, h(b \oplus PW_i)\}$  as  $T_i = P_{ij} \oplus h(h(y)||N_i||SID_j)$ ,  $A_i = h(T_i||h(y)||N_i)$ , and  $h(b \oplus PW_i) = CID_i \oplus h(T_i||A_i||N_i)$ .

**Step ZV2:** After  $Z$  obtains  $\{T_i, A_i, h(b \oplus PW_i)\}$ ,  $Z$  chooses a random number  $N_{Z_i}$  and computes  $\{CID_{Z_i}, P_{Z_{ij}}, Q_{Z_i}, N_{Z_i}\}$  as  $A_{Z_i}=h(T_i//h(y)//N_{Z_i})$ ,  $CID_{Z_i}=h(b \oplus PW_i) \oplus h(T_i//A_{Z_i}//N_{Z_i})$ ,  $P_{Z_{ij}}=T_i \oplus h(y)//N_{Z_i}//SID_j$ , and  $Q_{Z_i}=h(B_i//A_{Z_i}//N_{Z_i})$ . And then,  $Z$  sends  $\{CID_{Z_i}, P_{Z_{ij}}, Q_{Z_i}, N_{Z_i}\}$  to  $S_j$ .

**Step ZV3:** After  $S_j$  returns  $\{M'_{ij}, N_j\}$ ,  $Z$  also intercepts the data and computes both  $M''_{Z_j}=h(B_i//N_j//A_{Z_i}//SID_j)$  and the session key  $SK_{Z_j}=h(B_i//N_{Z_i}//N_j//A_{Z_i}//SID_j)$ .

**Step ZV4:**  $Z$  randomly chooses a number  $N_{Z_j}$  and intercepts the data and computes both  $M'_{Z_j}=h(B_i//N_{Z_j}//A_i//SID_j)$  and the session key  $SK_{Z_i}=h(B_i//N_i//N_{Z_j}//A_i//SID_j)$ . Finally,  $Z$  sends  $M''_{Z_j}$  to  $S_j$  and sends  $M'_{Z_j}$  to  $U_i$  individually.

Because  $Z$  has the secret value  $B_i$ , he/she can establish session  $\{SK_{Z_j}, SK_{Z_i}\}$  with  $S_j$  and  $U_i$  individually, and then  $Z$  can eavesdrop or alter the communication between  $U_i$  and  $S_j$ .

## 4. Our Scheme

In this section, we will show a new scheme, which satisfies Liao et al.'s ten requirements, to avoid those weaknesses of Lee et al.'s scheme and improve the computation efficiency. Our scheme also includes three roles as user ( $U_i$ ), registration center ( $RC$ ), and server ( $S_j$ ). There are five phases in this scheme: registration phase, login phase, verification phase, update session key phase, and password change phase.  $RC$  chooses a secret value  $x$  and computes  $h(x)$ , and then shares  $h(x)$  with each legal servers via a secure channel. The notations of our scheme are described as follows.  $U_i$  denotes the  $i$ -th user.  $S_j$  denotes the  $j$ -th server.  $RC$  denotes the registration center.  $PW_i$  denotes the password of  $U_i$ .  $ID_i$  denotes the identity of  $U_i$ .  $SID_j$  denotes the identity of  $S_j$ .  $CID_i$  denotes the dynamic ID of  $U_i$ .  $h(\cdot)$  denotes a one-way hash function.  $N_X$  denotes number used only once (Nonce) generated by an entity  $X$ .  $//$  denotes concatenation operation.  $\oplus$  denotes XOR operation.  $SK$  denotes session key between entity  $U_i$  and  $S_j$ .  $x$  denotes the secret value of  $RC$ .  $b$ ,  $b_{new}$  denotes random number generated by  $U_i$ .

### 4.1. Registration Phase

When a new user  $U_i$  wants to access the services  $S_j$ , he/she needs to register at the same  $RC$  that  $S_j$  registered. The communication between  $U_i$  and  $RC$  is via a secure channel.

**Step 1:** When the registration starts,  $U_i$  generates a random number  $b$ , and chooses his/her password  $PW_i$ . After that,  $U_i$  computes  $CID$  as  $CID=h(ID_i \oplus PW_i) \oplus b$ . And then,  $U_i$  sends  $CID$  to  $RC$ .

**Step 2:** After  $RC$  receives  $CID$  from  $U_i$ ,  $RC$  computes  $B_i$  as  $B_i=h(CID//h(x))$ , And then,  $RC$  returns  $\{B_i, h(\cdot)\}$  to  $U_i$ .

**Step 3:** When  $U_i$  receives  $\{B_i, h(\cdot)\}$ ,  $U_i$  computes  $BPW$  as  $BPW=B_i \oplus h(PW_i)$ . Finally,  $U_i$  stores  $\{BPW, b, h(\cdot)\}$  in smart card.

### 4.2. Login and Verification Phase

After the registration phase,  $U_i$  can access the resources of  $S_j$ . For security,  $U_i$  and  $S_j$  have to agree a session key to communicate each other, but  $U_i$  and  $S_j$  must mutual authenticate before that.

**Step 1:**  $U_i$  inputs his/her identity  $ID_i$  and password  $PW_i$ , and then the device computes  $\{CID, B_i\}$  as  $CID = h(ID_i \oplus PW_i) \oplus b$  and  $B_i=BPW \oplus h(PW_i)$ . After that,  $U_i$  generates two random

numbers,  $b_{new}$  and  $N_i$ . Next,  $U_i$  computes  $\{V_i, CID_{new}, Q_i\}$  as  $CID_{new} = h(ID_i \oplus PW_i) \oplus b_{new}$ ,  $V_i = CID_{new} \oplus h(B_i//N_i)$ , and  $Q_i = h(CID_{new}//B_i//N_i)$ . Finally,  $U_i$  submits  $\{CID, V_i, Q_i, N_i\}$  to  $S_j$ .

**Step 2:** When  $S_j$  receives  $\{CID, V_i, Q_i, N_i\}$  from  $U_i$ ,  $S_j$  computes  $\{B_i, CID_{new}\}$  and verifies  $Q_i$ .

$$\begin{aligned} B_i &= h(CID//h(x)) \\ CID_{new} &= V_i \oplus h(B_i//N_i) \\ Q_i &= ?h(CID_{new}//B_i//N_i) \end{aligned}$$

If  $Q_i$  equals  $h(CID_{new}//B_i//N_i)$ ,  $S_j$  can authenticate  $U_i$ , and the authenticating phase of  $U_i$  is completed. After the authenticating phase of  $U_i$ ,  $S_j$  generates a random number  $N_j$ , and computes  $\{B_{new}, V_j, Q_j\}$  as  $B_{new} = h(CID_{new}//h(x))$ ,  $V_j = B_{new} \oplus h(B_i//N_j)$ , and  $Q_j = h(CID//B_{new}//N_j)$ . Finally,  $S_j$  returns  $\{V_j, Q_j, N_j\}$  to  $U_i$ .

**Step 3:** When  $U_i$  obtains  $\{V_j, Q_j, N_j\}$  from  $S_j$ ,  $U_i$  computes  $B_{new} = V_j \oplus h(B_i//N_j)$  and verifies  $Q_j$  as  $Q_j = ?h(CID//B_{new}//N_j)$ . If  $Q_j$  equals  $h(CID//B_{new}//N_j)$ ,  $U_i$  can authenticate the  $S_j$  and the authenticating phase of  $S_j$  is completed. Next,  $U_i$  computes  $BPW_{new}$  as  $BPW_{new} = B_{new} \oplus h(PW_i)$ . And then,  $U_i$  stores  $\{BPW_{new}, b_{new}\}$  for the next login. After that,  $U_i$  computes  $SK$  and  $Q_{ij}$  as  $SK = h(N_i//N_j//B_i)$  and  $Q_{ij} = h(N_i//B_i//N_j//B_{new})$ .  $SK$  is the session key of  $U_i$  which is used for the communication with  $S_j$  this time. And then,  $U_i$  submits  $Q_{ij}$  to  $S_j$  for double check.

**Step 4:** When  $S_j$  receives  $Q_{ij}$ ,  $S_j$  verifies  $Q_{ij}$  as  $Q_{ij} = ?h(N_i//B_i//N_j//B_{new})$ . If they are equal,  $S_j$  computes the session key  $SK = h(N_i//N_j//B_i)$ . After that, the login and verification phase is completed.

#### 4.3. Update Session Key Phase

In order to improve the overall security,  $U_i$  and  $S_j$  can update their session key  $SK$  when they have held the communication for a long time in our scheme. In this phase,  $\{N_i, N_j\}$  denotes the existing random values, and  $\{N^*_i, N^*_j\}$  denotes two random values. After this phase completed,  $U_i$  and  $S_j$  will replace  $\{N_i, N_j\}$  with  $\{N^*_i, N^*_j\}$ .

**Step 1:**  $U_i$  chooses a random number  $N^*_i$ . After that,  $U_i$  computes  $\{V^*_i, Q^*_i\}$  as  $V^*_i = N^*_i \oplus h(B_i \oplus h(N_i//N_j))$  and  $Q^*_i = h(N^*_i \oplus B_i)$ . Last,  $U_i$  submits  $V^*_i$  and  $Q^*_i$  to  $S_j$ .

**Step 2:** When  $S_j$  receives  $V^*_i$  and  $Q^*_i$  from  $U_i$ ,  $S_j$  computes  $N^*_i$  and verifies  $Q^*_i$  as  $N^*_i = V^*_i \oplus h(B_i \oplus h(N_i//N_j))$  and  $Q^*_i = ?h(N^*_i \oplus B_i)$ . If  $Q^*_i$  is equal to  $h(N^*_i \oplus B_i)$ ,  $S_j$  generates a random number  $N^*_j$ . Next,  $S_j$  computes  $\{V^*_j, Q^*_j\}$  as  $V^*_j = N^*_j \oplus h(B_i \oplus h(N_j//N_i))$  and  $Q^*_j = h(N^*_j \oplus B_i)$ . Finally,  $S_j$  returns  $\{V^*_j, Q^*_j\}$  to  $U_i$ .

**Step 3:** When  $U_i$  obtains  $V^*_j$  and  $Q^*_j$  from  $S_j$ ,  $U_i$  computes  $N^*_j$  and verifies  $Q^*_j$  as  $N^*_j = V^*_j \oplus h(B_i \oplus h(N_j//N_i))$  and  $Q^*_j = ?h(N^*_j \oplus B_i)$ . If  $Q^*_j$  and  $h(N^*_j \oplus B_i)$  are equal,  $U_i$  updates the session key  $SK$  to  $SK^*$  as  $SK^* = h(N^*_i//N^*_j//B_i)$ . Next,  $U_i$  computes  $Q^*_{ij}$  as  $Q^*_{ij} = h(N^*_i \oplus N^*_j \oplus B_i)$ . Finally,  $U_i$  sends  $Q^*_{ij}$  to  $S_j$ .

**Step 4:** When  $S_j$  obtains  $Q^*_{ij}$  from  $U_i$ ,  $S_j$  verifies  $Q^*_{ij}$  first as  $Q^*_{ij} = ?h(N^*_i \oplus N^*_j \oplus B_i)$ . If  $Q^*_{ij}$  and  $h(N^*_i \oplus N^*_j \oplus B_i)$  are equal,  $S_j$  also updates the session key  $SK$  to  $SK^*$  as  $SK^* = h(N^*_i//N^*_j//B_i)$ . And then, the session key update is finished.

#### 4.4. Password Change Phase

A user-friendly system should provide a mechanism with respect to the password chosen so that a password may be changed. In our scheme, the user can change his/her password

freely at will by the owner. If a user wants to change his/her password, he/she just needs to input the existing password  $PW_i$  and chooses a new password  $PW_{new}$ . Our scheme will implement the password-changed phase, which is similar to both the authentication and establishment of session key phase.

**Step 1:**  $U_i$  inputs his/her password  $PW_i$ , and chooses a new password  $PW_{new}$  then the device computes  $\{CID, B_i\}$  as  $CID = h(ID_i \oplus PW_i) \oplus b$  and  $B_i = BPW \oplus h(PW_i)$ . After that, the device generates two random numbers,  $b_{new}$  and  $N_i$ . Next,  $U_i$  computes  $\{V_i, CID_{new}, Q_i\}$  as  $CID_{new} = h(ID_i \oplus PW_{new}) \oplus b_{new}$ ,  $V_i = CID_{new} \oplus h(B_i // N_i)$ , and  $Q_i = h(CID_{new} // B_i // N_i)$ . Finally,  $U_i$  submits  $\{CID, V_i, Q_i, N_i\}$  to  $S_j$ .

**Step 2:** When  $S_j$  receives  $\{CID, V_i, Q_i, N_i\}$  from  $U_i$ ,  $S_j$  computes  $\{B_i, CID_{new}\}$  and verifies  $Q_i$  as  $B_i = h(CID // h(x))$ ,  $CID_{new} = V_i \oplus h(B_i // N_i)$ , and  $Q_i = ?h(CID_{new} // B_i // N_i)$ . If  $Q_i$  equals  $h(CID_{new} // B_i // N_i)$ ,  $S_j$  can authenticate  $U_i$ , and the authenticating phase of  $U_i$  is completed. After the authenticating phase of  $U_i$ ,  $S_j$  generates a random number  $N_j$ , and computes  $\{B_{new}, V_j, Q_j\}$  as  $B_{new} = h(CID_{new} // h(x))$ ,  $V_j = B_{new} \oplus h(B_i // N_j)$ , and  $Q_j = h(CID // B_{new} // N_j)$ . Finally,  $S_j$  returns  $\{V_j, Q_j, N_j\}$  to  $U_i$ .

**Step 3:** When  $U_i$  obtains  $\{V_j, Q_j, N_j\}$  from  $S_j$ ,  $U_i$  computes  $B_{new}$  and verifies  $Q_j$  as  $B_{new} = V_j \oplus h(B_i // N_j)$  and  $Q_j = ?h(CID // B_{new} // N_j)$ . If  $Q_j$  equals  $h(CID // B_{new} // N_j)$ ,  $U_i$  can authenticate the  $S_j$  and the authenticating phase of  $S_j$  is completed. Next,  $U_i$  computes  $BPW_{new}$  as  $BPW_{new} = B_{new} \oplus h(PW_{new})$ . And then,  $U_i$  stores  $\{BPW_{new}, b_{new}\}$  for the next login. After that, the password changed phase is completed.

## 5. Analysis of our Scheme

We analyze the security of our scheme in this section. Our scheme not only withstands the various leaks of previous studies but also has more efficacies.

First, we assume an adversary  $Z$  in following scenarios, and explain some hurdles that the adversary  $Z$  will come across if the adversary  $Z$  wants to break the security of our scheme. **Anonymity:** If the adversary  $Z$  attempts to use the information, which can be intercepted from the public communicating environment, to trace the user  $U_i$ , he/she needs to discern the relation between each communication. However, we use a random number  $b$ , which is changed for each authorization, to compose the values as  $\{CID, V_i, Q_i\}$ , and  $b$  has never been disclosed. Namely the values are different for each communication, and there is no any relation between each change. In addition,  $\{CID, V_i\}$  are not directly composed with the parameters from  $RC$ . Therefore, those values have no relation with other legal users, and  $Z$  can't derive constant values by the public information even if he/she is also a legal user. Moreover, as there are no verification tables stored in servers,  $Z$  unable to obtain any information about the user even if  $Z$  invades any server in this system successfully. For the above reasons, we claim our scheme achieves the necessary anonymity.

**Perfect forward secrecy and backward secrecy:** In this scheme, the session key is established by  $\{N_i, N_j, B_i\}$ , where  $\{N_i, N_j\}$  are two random numbers generated each time and  $B_i$  is a secure value, which is also changed for each authentication phase. Although  $Z$  can intercept  $N_i$  and  $N_j$  when the authentication phase proceeds, but he/she cannot obtain  $B_i$  which is always computed by one-way hash function. In addition, the new  $\{N^*_i, N^*_j\}$  are always encrypted by  $h(B_i \oplus h(N_i // N_j))$  and  $h(B_i \oplus h(N_j // N_i))$  respectively except for first time. Therefore,  $Z$  cannot use one of the session keys to derive other key. Hence, we claim our scheme achieves perfect forward secrecy and backward secrecy.

**Masquerade attack:** We suppose the adversary  $Z$  intercepts the legal user  $U_i$ 's information and he/she attempts to masquerade the legal user  $U_i$  to communicate with the legal server  $S_j$  or masquerade the legal server  $S_j$  to communicate with the legal user  $U_i$  in our scheme. However, he/she will come across some difficulties in following scenarios.

**$Z$  intercepts  $\{CID, V_i, Q_i, N_i\}$  when  $U_i$  submit them to  $S_j$  and replays them for disguising the user  $U_i$  after  $U_i$  is offline:** This action will pass the first authentication of  $S_j$  but will not be approved in the second authentication. As a result,  $Z$  cannot obtain  $\{B_i, B_{new}\}$  to compute  $Q_{ij}$ . For this reason,  $Z$  cannot disguise the user  $U_i$  and communicate with  $S_j$ .

**$Z$  intercepts  $\{V_j, Q_j, N_j\}$  when  $S_j$  returns them to  $U_i$  and replays them for disguising the  $S_j$  to communicate with  $U_i$ :** This action cannot pass the authentication of  $U_i$ . When  $Z$  replays  $\{V_i, Q_i, N_i\}$ ,  $U_i$  verifies that  $Q_j$  is equal to  $h(CID//V_j \oplus h(B_i//N_j)//N_j)$ , and detects they are not equal, because the secure value  $B_i$  of  $U_i$  will be changed after the authentication phase between  $U_i$  and  $S_j$  each time. Hence,  $Z$  cannot disguise  $S_j$  and communicate with the user  $U_i$ .

**$Z$  intercepts  $\{CID, V_i, Q_i, N_i\}$  and  $\{Q_{ij}\}$  when  $U_i$  submit them to  $S_j$  and replays them for disguising the user  $U_i$  after  $U_i$  is offline:** The action cannot pass the second authentication of  $S_j$ . As a result,  $S_j$  verifies  $Q_{ij}$  when it receives  $Q_{ij}$  by  $N_j$  which is a random and temporary number generated by itself. Because the  $S_j$  doesn't store  $N_j$  after each communication, it cannot compute  $h(N_i//B_i//N_j//B_{new})$  again. Therefore,  $Z$  cannot disguise the user  $U_i$  and communicate with  $S_j$ .

Because of the above reasons, we claim our scheme can withstand the masquerade attack and replay attack.

**Device is lost:** If a user  $U_i$  lost his/her device and the adversary  $Z$  picks it up,  $Z$  can obtain the information which is stored in the device as  $\{BPW, b\}$ . But  $Z$  still cannot use that information he/she obtains to disguise  $U_i$  and communicate with the server  $S_j$ . Because  $Z$  cannot compute  $B_i = BPW \oplus h(PW_i)$  and cannot compute  $\{V_i, Q_i\}$ , hence,  $Z$  cannot pass the authentication of  $S_j$  and disguise  $U_i$ . For the reason, we claim the information of a user is secure even if the user lost his/her device in our scheme.

**Password be disclosed:** Suppose a user  $U_i$  discloses his/her password carelessly and the adversary  $Z$  obtains it,  $Z$  also cannot use the password to break the security of this scheme. In our scheme, the parameters, which are transmitted between  $U_i$  and  $S_j$  aren't constructed from password of  $U_i$ . Because of that,  $Z$  cannot use the password to disguise the user  $U_i$  or decrypt the information he/she intercepts. Our scheme not only withstands the attack from the adversary  $Z$  when user's password lost, but also provides a friendly way to users about password changed that is described in section 4.4 of this article. For the above reasons, we claim our scheme is secure even if a user lost his/her password.

In addition, we provide a mechanism for updating the session key  $SK$  between  $U_i$  and  $S_j$  when the communication has been hold a long time. This mechanism can strengthen the security of our scheme. Because it can allow the cipher-text encrypted by different  $SK$  in the same communication, the adversary  $Z$  cannot decrypt all of them even if  $Z$  obtains one of  $SK$ . For the above reasons, we claim the security of our scheme is better than previous schemes.

## 6. Conclusion

In this article, we propose an improved scheme of anonymous authentication to improve the security and efficiency of a multi-server environment. The scheme not only overcomes the secure leaks of Lee et al.'s scheme but also maintains a high level of computational efficiency. Our analysis shows that our scheme can achieve the real anonymity and better efficiency by means of easy computations as one-way hash functions and XOR operations. Moreover, our scheme has other advantages, such as a changeable password, no verification table, and mutual authentication, etc. From the above advantages, we can claim that our scheme is very suitable for a multi-server environment.

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