

# An Enhanced Robust and Efficient Password-Authenticated Key Agreement Using Smart Cards

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## Abstract

*Although the smart card brings conveniences, it also increases the risk in the case of lost cards. When the smart card is possessed by an attacker, the attacker will possibly attempt to analyze the secret information within the smart card to deduce the authentication mechanism of the server and then forge user credentials or break the entire authentication system. In this paper, we analyze the lost smart card attack from Juang et al.'s scheme [5] that proposes password authenticated key agreement. In order to bolster the security of the entire system, we mitigated some of its weaknesses.*

**Keywords:** *key exchange, elliptic curve cryptosystem, smart card, authentication.*

## 1. Introduction

In 2008, Juang et al. (for short JCL-scheme) [5], point out the major drawbacks are loss of anonymity for the user and high computation and communication cost in Fan et al.'s scheme. To improve upon these drawbacks, Juang et al. proposed a scheme that not only can provide identity protection but also keep lower communication and computation cost by using elliptic curve cryptosystems. They also proposed a solution for minimizing the risk of lost cards. The use of a fixed server key allows an offline attack to be mounted against the server key when an attacker possesses the user card. Therefore, we propose to improve JCL-scheme and mitigate the exposure of the entire system when a smart card is compromised.

The paper is organized as follows: In Section 2, we review JCL-scheme [5] and analyze its weaknesses. In Section 3, we propose our scheme. In Section 4, the security analysis of our proposed scheme and comparison with JCL-scheme are discussed. Finally, in Section 5, we conclude the paper.

## 2. Review and Analysis of the JCL-scheme

A review and analysis of the JCL-scheme is given in this section.

### 2.1 The JCL-scheme

The JCL-scheme [5] consists of five phases: parameter generation, registration, pre-computation, log-in, and the password-changing phase. Descriptions of these phases are given below.

### Parameter Generation Phase

The related parameters in this scheme are as follows:

- (1) The server selects three numbers: a larger prime number  $P$  and two field elements  $(a, b)$ . Where  $a \in Z_p$  and  $b \in Z_p$  must satisfy  $4a^3 + 27b^2 \pmod{P} \neq 0$ , and the elliptic curve equation is defined as:  $E_p: y^2 = x^3 + ax + b$ .
- (2) The server generates a point  $G$  from order  $n$ , and satisfies  $n \times G = O$ .
- (3) The server selects a random number  $x_s$  to be the private key, and computes the public key  $P_s = (x_s \times G)$ .
- (4) The server publishes the parameters  $(P_s, P, E_p, G, n)$ .

### Registration Phase

- (1) The user will select a random number  $b$ , and  $\{ID_i, h(PW_i || b)\}$  will be passed to the server.
- (2) After the server receives the message, it will calculate  $b_i = E_s( h(PW_i || b) || ID_i || CI_i || h(ID_i || CI_i || h(PW_i || b)) )$  and  $V_i = h(ID_i, s, CI_i)$  where  $ID_i$  is the user's identity and  $CI_i$  is the card number. The server will store  $\{ID_i, CI_i\}$  in the internal registry. Finally,  $(ID_i, CI_i, b_i, V_i)$  is returned to the user.

### Pre-computation Phase

The smart card chooses a random number  $r$  and calculates  $e = (r \times G)$  and  $c = (r \times P_s) = r \times x \times G$ . Then  $(e, c)$  stored in card's memory. In the log-in phase,  $(e, c)$  will also be used.

### Log-in Phase

Step 1: The smart card calculates  $E_{V_i}(e)$  and sends  $E_{V_i}(e)$  and  $b_i$  to the server. The server uses the secret key  $s$  to decrypt  $b_i$  and obtain  $(ID_i || CI_i || h(PW_i || b))$ , and calculates  $V_i = h(ID_i, s, CI_i)$  to decrypt  $E_{V_i}(e)$ . Then, the server will verify the following things:

- Is  $CI_i$  stored in the registration table?
- Is  $ID_i$  in the registration?

Step 2: If any of the above checks are false, the server revokes the agreement. If the above verifications are true, the server chooses a random number  $u$  and calculates  $c = (r \times P_s) = r \times x \times G$  and  $M_s = h(c || u || V_i)$ . Then, the server sends  $(c, M_s)$  to the smart card.

Step 3: The smart card calculates and checks  $M_s$ . If  $M_s = h(c || u || V_i)$ , the smart card calculates  $M_U = h(h(PW_i || b) || V_i || c || u)$  and a session key  $S_k = h(V_i, c, u)$  and then sends  $M_U$  to the server.

Step 4 The server checks  $M_U$ . If  $M_U = h(h(PW_i || b) || V_i || c || u)$ , the server calculates a session key  $S_k = h(V_i, c, u)$ .

### Password-Changing Phase

If the user  $i$  wants to change his password, the smart card can encrypt the password changing message using the session key that is produced in the log-in phase. To do so, the smart card selects a random number  $b^*$  and produces another new password  $PW_i^*$  and sends  $E_{S_k}(ID_i, h(PW_i^* || b^*))$  to the server. After the server receives the message, it recalculates  $b_i^* = E_s(h(PW_i^* || b^*) || ID_i || CI_i || h(ID_i || CI_i || h(PW_i^* || b^*)))$  and sends  $E_{S_k}(b_i^*)$  to the smart card. The smart card will decrypt  $b_i^*$  using a session key and store it in its memory.

## 2.2 Security Analysis of the Juang et al. Scheme

The system may be compromised by extracting information from the smart card in order to falsify server authentication. Specifically, in the case of known  $ID_i$  and  $CI_i$

(these messages are stored on the smart card), the attacker will attempt to solve  $V_i = h(ID_i, s, CI_i)$ . The attacker can seek out the secret server key  $s$  using offline attack. After the secret value  $s$  is known, the attacker can freely tamper with the internal value of  $b_i$ , compromising the security of the entire system.

### 3. The Proposed Scheme

We improve on JCL-scheme and propose an enhanced password-authentication key agreement. This scheme not only maintains all the benefits of the JCL-scheme but also can enhance the security of the server when the smart card contents are disclosed. Our proposed scheme also consists of the same five phases: parameter generation, registration, pre-computation, log-in, and password-changing.

#### Parameter Generation Phase

In this phase, the proposed methods modeled after JCL-scheme.

#### Registration Phase

The user can use the smart card to send identification information for the server to authenticate. Descriptions of these steps (as depicted in Figure 1) are as follows:

Step 1: The smart card chooses a random number  $b$  and calculates Eq.(1).

$$T_1 = h(PW_i || b^{-1}). \quad (1)$$

Then the smart card sends  $\{ID_i, h(PW_i || b), T_1\}$  to the server.

Step 2: The server chooses another random number  $S_2$  and calculates Eqs.(2-4).

$$T_2 = T_1 * S_2^{-1} \quad (2)$$

$$b_i = E_{S_1}(h(PW || b) || T_2 || ID_i || CI_i || h(ID_i || CI_i || h(PW || b))) \quad (3)$$

$$V_i = h(ID_i, T_1, CI_i) \quad (4)$$

Then, the server issues credentials to user  $i$  that contains parameters  $(ID_i, CI_i, b_i, V_i)$ .

Step 3: The user receives  $(ID_i, CI_i, b_i, V_i)$  and then stores these parameters and  $b$  into the smart card.

#### Pre-computation Phase

The smart card chooses a random number  $r$  and calculates  $e = (r \times G)$  and  $c = (r \times P_s) = r \times x \times G$ .

Then  $(e, c)$  is stored in card memory for use in the log-in phase.

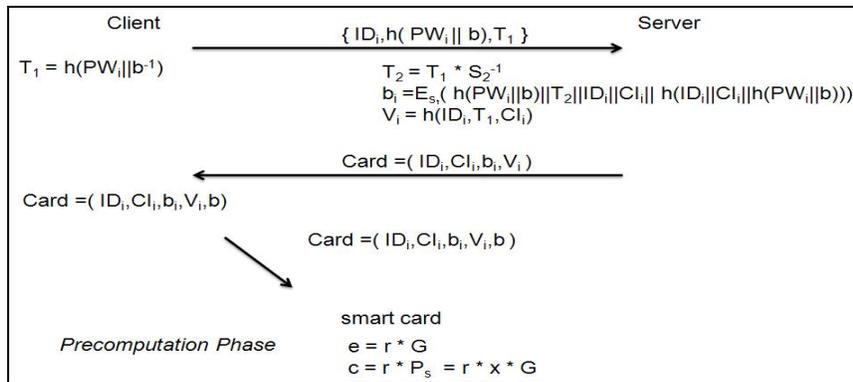


Figure 1. Registration and Pre-computation Phase of the Proposed Scheme

#### Log-in Phase

The user  $i$  wants to login to the server and must use his own smart card and password. Descriptions of these steps (as depicted in Figure 2) are as follows:

Step 1: After calculating  $E_{V_i}(e)$ , the smart card sends  $E_{V_i}(e)$  and  $b_i$  to the server.

Step 2: The server decrypts  $b_i$  using the secret key  $S_1$  and obtains  $(T_2//ID_i//CI_i//h(PW_i//b))$ , and calculates Eq.(5) and Eq.(6), respectively.

$$T_1 = T_2 \times S_2 \quad (5)$$

$$V_i = h(ID_i, T_1, CI_i) \quad (6)$$

Then, the server will verify the following:

- Is  $CI_i$  stored in the registration table?
- Is  $ID_i$  in the registration?

If any of the above verifications are false, the server revokes the agreement. If the above verifications are true, the server chooses a random number  $u$  and calculates:

$$c = (e * x) = (r * x * G) \quad (7)$$

$$M_S = h(c // u // V_i) \quad (8)$$

Then, the server sends  $(c, M_S)$  to the smart card.

Step 3: The smart card calculates and checks  $M_S$ . If  $M_S$  is true, the smart card calculates:

$$M_U = h(h(PW_i//b)//T_1//c//u) \quad (9)$$

$$S_k = h(V_i, c, u) \quad (10)$$

And then the smart card sends  $M_U$  to the server.

Step 4: The server checks  $M_U$ . If  $M_U$  is true, the server calculates a session key  $S_k = h(V_i, c, u)$  and accepts the log-in request.

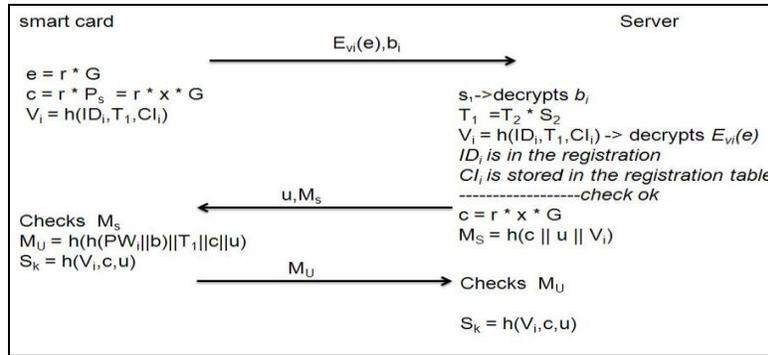


Figure 2. Log-in Phase of the Proposed Scheme

### Password-Changing Phase:

If the user  $i$  wants to change his password, the smart card can encrypt the password changing message using the session key that is produced in the log-in phase. To do so, the smart card selects a random number  $b^*$  and produces another new password  $PW_i^*$  and sends  $E_{S_k}(ID_i, h(PW_i^*//b^*))$  to the server. After the server receives the message, it recalculates  $b_i^* = E_{S_k}(h(PW_i^*//b^*)//ID_i//CI_i//h(ID_i//CI_i//h(PW_i^*//b^*)))$  and sends  $E_{S_k}(b_i^*)$  to the smart card. The smart card will decrypt  $b_i^*$  using a session key and store it in its memory.

## 4. Security Analysis and Comparison

### ● Lost smart card

Assume the attacker accesses the smart card and wants ascertain internal value  $b_i$ . Value  $b_i$  cannot be decrypted without possessing the secret server key  $S_1$ . In the case of known  $ID_i$  and  $CI_i$ , if the attacker tries to calculate  $V_i = h(ID_i, T_1, CI_i)$ , the value  $T_1$  is required. In order to obtain  $T_1$ , the attacker needs to know the user password  $PW_i$  in

$h(Pw_i//b^{-1})$ . Disclosure of the information on the smartcard still requires additional information in order to be of any value.

● **Comparison**

The following table compares the properties of the proposed scheme and previous schemes. Where C1: low communication and computation cost; C2: no password table; C3: users can choose the passwords; C4: no time-synchronization problem; C5: mutual authentication; C6: revoking a lost card without changing the user’s identity; C7: identity protection; C8: session key agreement; C9: preventing offline dictionary attack against the smart card information.

**Table 1:** Properties of the proposed scheme versus previous schemes

	Hwang & Li scheme	Fan et al scheme	Juang scheme	Sun scheme	Chien et al scheme	Juang et al scheme	Our Scheme
C1	X	O	O	O	O	O	O
C2	O	O	O	O	O	O	O
C3	X	X	O	X	O	O	O
C4	X	X	O	X	X	O	O
C5	X	O	O	X	O	O	O
C6	X	X	X	X	X	O	O
C7	X	X	X	X	X	O	O
C8	X	O	O	X	X	O	O
C9	X	X	X	X	X	X	O

**5. Conclusion**

In our scheme, even if the attacker holds the user’s card, and mounts an offline attack to obtain the server key, it will not result in risk to the entire system. We use Juang et al.’s mechanism to revoke cards and ensure the privacy of the user. Possession of a smart card does not allow knowledge of the second secret key in the server, so the attacker cannot break the security of the system.

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