A Robust and Secure Block-SVD based Embedding of Encrypted Watermark in Digital Images using RDWT

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Abstract

Digital image watermarking has been proposed for treatment of the problem of copyright protection, authentication of digital data and ownership identification. In this paper a robust and secure digital image watermarking method based on Redundant Discrete Wavelet Transform (RDWT) and block-by-block SVD (Singular Value Decomposition) is presented. The watermark image is encrypted (scramble watermark) by using Cipher block chaining (CBC) to enhance its privacy and robustness. In the proposed scheme the gray scale host image is transformed by RDWT and is also segmented into non-overlapping blocks of each sub-band, and then a scramble watermark image is embedded in the singular values of these blocks in each sub-band. This scheme provides security by embedding encrypted watermark in block-by-block manner and has large capacity due to redundancy in RDWT domain and also preserves high imperceptibility due to SVD properties. The advantage of the given scheme is that it is much more robust to attacks such as cropping, compression, Gaussian noise. Experimental results show that this method performs better in terms of capacity, security and robustness than other block-based methods presented before.

Keywords: Digital image watermarking; Redundant Discrete wavelet transform; Singular value decomposition, Cipher Block Chaining, NCC and PSNR.

1. Introduction

Due to rapid growth of computer technology, multimedia and activity on the internet, digital data (Audio, Video, and Image) are widely spread and these data are not safe and the information hiding also becomes an important issue, so the problem of multimedia digital data security such as ownership identification, copyright protection, content authentication and tamper detection comes. Digital image watermarking is one the best solution to remove these problems. Watermarking means to hide the digital information into multimedia digital content (Audio, Video and Image) such that it is imperceptible to the human eye, only a real person can extract the information. The basic requirements of watermarking are robustness, imperceptibility, security [4]. Robustness means that the watermark should be resisted against various image processing attacks such as a noise addition, histogram manipulation, geometric attacks, filtering etc. Imperceptibility means that there is no difference between the original image and watermarked image. Security means the resistance against malicious attacks. As the capacity of the embedded data increase, performs of the system, improve but its effect on imperceptibility and robustness that is there is tradeoff between imperceptibility and robustness, as imperceptibility increases, the robustness decreases. This tradeoff is maintained by a factor is called scaling factor that is strength of embedding watermark. Digital image watermarking can be classified in two domains, one is spatial domain and other is transform domain. Spatial domain techniques advantages are simple to implement, low complexity and the capacity of data hiding is very high and disadvantage is less robust against various attacks [5].
transform domain techniques Discrete Cosine Transform (DCT), Singular Value decomposition (SVD), Discrete Wavelet Transform (DWT), Discrete Fourier Transform (DFT) etc. are highly robust and imperceptible as compared to spatial domain techniques[6,8,12]. The process of digital image scrambling by changing the pixel position of meaningful image through matrix transform into meaningless disorder image is called image scrambling. There are several techniques for scrambling the image such as based on permutation substitution are enhanced blowfish algorithm, chaotic standard map and image encryption based algorithms are chaos random sequence, AES encryption algorithm [17,18], hash algorithm and block cipher. In our proposed scheme we use Cipher Block Chaining for encryption of the watermark image [16,19]. In SVD watermarking modified the singular values of the host image by watermark [3, 14, 15]. For tradeoff between imperceptibility and robustness we take scaling factor 0.02 for LL band and 0.002 for other band. RDWT has spatio-frequency localization property and shift invariant and also overcome the DWT problem [10,11,12]. Some researcher use block SVD-based watermarking techniques[6,7,8,9,12] for improving the robustness and imperceptibility also reduce the computational complexity.

The rest of the paper is organized as follows In section 2 literature survey and brief background about SVD, RDWT and Cipher block chaining (CBC) then in section 3 embedding and extracting steps of proposed scheme are explained. The results and comparative analysis are in section 4 and finally conclusion are drown in section 5

2. Literature Survey

Liu et al. [3] Proposed SVD-based watermarking method that performs the embedding process to the singular values of the whole image. The Drawback of this scheme is watermark degradation due to some image processing attacks. Ganic et al. [2] Proposed DCT-SVD based watermarking scheme and suffers from the lack of robustness for some attacks. Kang et al. [1] used discrete Fourier transforms. it is more robust, but lack of imperceptible. Wang et al. [8] Using discrete Cosine transforms for transforming the block of pixel and improve the robustness. Navas et al. [7] Present a block based scheme using discrete wavelet transform and improve the imperceptibility as well as robustness. Mahammad et al. [12] proposed a DCT block based algorithm with human visual system (HSV) to get a higher detection rate as well as better fidelity, but the compression result is not good. Chin-Chen et al. [20] a block-based new watermarking technique using exclusive or operation to construct a secret key, this method is resist various attacks. Yixin Yan et al. [13] use just noticeable distance (JND) for an adaptive block based watermarking and quality factor above 40 this scheme is more robust. In Liu et al. [3] a single watermark embedded in singular values of the whole image and it is destroyed due to attacks. This is the main drawback of Liu et al. To avoid this drawback Ghazy et al. [9] proposed a block-by-block SVD based techniques and removes this disadvantage and find out better results, but in Ghazy et al. [9] Scheme the size of watermark is very small as compared to the host image and has very low embedding capacity. Our presented block-by-block RDWT–SVD based method has the high embedding capacity more robust against JPEG compression, cropping, rotation, blurring, Gaussian noise, resizing and rotation and also have high security and imperceptibility.

2.1. SVD

SVD is a numerical method for resolving the matrix for numerical analysis. It uses for extracting the algebraic feature of the image. The main properties of SVD are the singular values of an image matrix have good stability and when a small permutation is added to an image, its singular values do not change significantly [22]. In SVD transform, any n × n matrix A can be decomposed as A = UVᵀ where U and V are orthogonal matrix and D = diag(αₖ) is a diagonal matrix, where αₖ, i = 1,2,3 .... n are the singular values.
The column $U$ is the left singular and $V$ is the right singular matrix of the image matrix $A$. It can be written as

$$A = UDV^T$$

$$= \begin{bmatrix} u_1, u_2, \ldots, u_n \end{bmatrix} \times \begin{bmatrix} \alpha_1 & 0 & \cdots & 0 \\ 0 & \alpha_2 & \cdots & 0 \\ \vdots & 0 & \ddots & 0 \\ 0 & 0 & \cdots & \alpha_n \end{bmatrix} \times \begin{bmatrix} v_1, v_2, \ldots, v_n \end{bmatrix}$$

$$= \sum_{i=1}^{r} \alpha_i u_i v_i$$

Where $r$ is the rank of the matrix $A$. The singular values define the luminance of the image and the similar pair of singular matrix defines the geometry of the image.

2.2. RDWT

Watermarking in frequency domain, DWT is one of the mostly using techniques because it has spatio-frequency localization property. Due to shift variance a major change occur in the wavelet coefficients of the image even for minor shifts in the input image. As a result, there is an inaccurate extraction of watermark image and cover image data. [11, 21] RDWT solve this problem because it is shift invariant. 1D DWT and 1D RDWT can be described by Figure 1, Figure 2.Where $f(n)$ and $f'(n)$ represents the 1D input and reconstruct the signal. $h[-k]$ and $g[-k]$ are analysis filters and $h[k]$ and $g[k]$ are synthesis low pass and high pass filters respectively. $c_j$ and $d_j$ are the low-band and high-band output coefficients at level $j$. The analysis and synthesis equation of RDWT are shown in equation (2), (3), (4).

**Analysis**

$$c_{j+1}[k] = (c_j[k] * h_j[-k])$$

**Synthesis**

$$c_{j}[k] = \frac{1}{2} (c_{j+1}[k] * h_{j+1}[k] + d_j[k] * g_j[k])$$

![Figure 1. Analysis and Synthesis Filter Banks of 1D DWT](image-url)
Where * means convolution and ↓2 means down sampling and ↑2 means up sampling at each level of iteration in DWT. Size of each sub band decrease due to down sampling and increase in levels of decomposition. RDWT discard down sampling and up sampling of coefficients. At each level the number of output coefficient doubles that of the input. RDWT based signal processing is more robust than DWT based techniques.

2.3. Cipher Block Chaining

Cipher Block Chaining (CBC) encrypts the sequence of bit as a single or block by block and changes the original image into encoded image.[16,19] It uses a vector of same length of plaintext with first block is called an initialization vector (IV).

![Diagram of encryption by Cipher Block Chaining](image)

Figure 3. Encryption by Cipher Block Chaining

Initialization vector (IV) is not secret but unpredictable. Each plaintext block is XORed with the previous cipher block and then encrypted. Original image can be recovered by applying decryption process with the correct key. $P_i, E_i, C_i, D_k, C_0$ are plaintext, encrypted text, cipher text, decrypted text, and initialization vector respectively. The block diagram and the equation of encryption and decryption are shown in Figure 3, Figure 4 and equation (5), (6), and (7).

\[
C_i = E_i(P_i \oplus C_{i-1}) \tag{5}
\]

\[
C_0 = IV \tag{6}
\]

\[
P_i = D_k(C_i) \oplus C_{i-1} \tag{7}
\]
3. The Proposed Scheme

The proposed watermark embedding and extracting steps are given below.

3.1. Watermark Embedding steps:

1. The host image is transformed by RDWT and then divides all sub-bands into non-overlapping blocks, here we show partition of LL bands in embedding block diagram in Figure 5.
2. An SVD process is applied on each block of LL sub-band and get a matrix of singular values $P_i$, where $i=1,2,3,\ldots,N, N$ is no of blocks

$$S_{bi} = K_i P_i L_i^T$$

(8)

Figure 4. Decryption by Cipher Block Chaining

Figure 5. Watermark Embedding Process
3. Taking \( f \) logo as a watermark image and scrambled by using Cipher Block Chaining algorithm, now this scrambled watermark image is embedded.

- Watermark image \( f \) is divided into non-overlapping blocks and considers 8 successive pixels of the image as a single block for generation of key process.
- Now taking XOR operation with each block to obtain the encrypt image by using key.
- Encrypted image is called scrambling image.

4. This scrambled watermark directly adds to singular values of each block of LL sub band.

\[
R_i = P_i + \alpha W
\]  
(9)

5. Again SVD process apply to modify the matrix \( R_i \)

\[
R_i = U_{wi} M_{wi} W_i^T
\]  
(10)

6. Perform new operation to modify the coefficient for each block of LL sub band

\[
S_{\text{bw}i} = K_i M_{wi} I_i^T
\]  
(11)

7. Apply inverse RDWT and rearrange all watermarks in each block and get watermarked image \( S_W \)
3.2. Watermarking Extracting Steps:

1. By applying RDWT on distorted image $S_w^*$ and decompose it into four sub-bands
2. SVD is applied to all sub-bands as fallows
   
   $S_{bw_i}^* = E_i^* G_{wi}^* H_i^T$ (12)

![Figure 7. Host Images: (a) Rudra, (b) Watermark Image f Logo, (c) Encrypted Watermark Image, (d) Watermarked Image Rudra, (PSNR 53.785dB.), (e) Extracted Watermark Images f Logo, (f) Magnified Watermark Maximum Correlation, (g) Watermark Normalized Correlation Coefficients](image)

![Figure 8. Watermarked Images after Applying Attacks (a) Gaussian Noise (0.01) (b) Blurring (3×3) (c) Cropping, All Images Size are 512×512](image)
3. Now abstain $J_i^{*}$ by applying operation

$$J_i^{*} = U W_i G_i^{*} V_i^{T}$$  \hspace{1cm} (13)

4. Now find extracted scrambled watermark

$$W_i^* = \frac{J_i^{*} - P_i}{\alpha}$$  \hspace{1cm} (14)

5. Now applying inverse encryption method to extract the watermark $W_{k_i}^*$

6. Now rearrange all extract watermark images in each block of each sub band and get combine image.

Figure 9. Watermarked Images after Applying Attacks
(d) Resizing (512-256-512) (e) Rotation (150) (f) Compression All Images
Size are 512×512

Figure 10. Extracted Watermark Images Image and Reconstructed Image of
LL Sub-Band after Applying Attacks (a) Gaussian Noise(0.01),
(b) Blurring(3×3), (c) Cropping, (d) Resizing 512-256-512),  (e) Rotation,
(150) (f) Compression
Figure 11. Extracted Watermark Images of Sub-Band (LL,LH,HL,HH) After Applying Attacks (a) Gaussian Noise(0.01), (b) Blurring(3×3), (c) Cropping, (d) Resizing(512-256-512), (e) Rotation, (150) (f) Compression

Table 1. Correlation Coefficient Value after Applying Attacks (a) Gaussian Noise (0.01), (b) Blurring (3×3), (c) Cropping, (d) Resizing (512-256-512), (e) Rotation, (150) (f) Compression in All Sub Band (LL,LH,HL,HH)

<table>
<thead>
<tr>
<th>Attacks</th>
<th>Proposed Scheme(RDWT+Block based SVD and using CBC)</th>
<th>LL</th>
<th>LH</th>
<th>HL</th>
<th>HH</th>
</tr>
</thead>
<tbody>
<tr>
<td>Gaussian noise(0.01)</td>
<td>0.5152</td>
<td>0.5644</td>
<td>0.5648</td>
<td>0.5731</td>
<td></td>
</tr>
<tr>
<td>Blurring(3×3)</td>
<td>0.7839</td>
<td>0.7748</td>
<td>0.6981</td>
<td>0.5251</td>
<td></td>
</tr>
<tr>
<td>Cropping</td>
<td>0.5381</td>
<td>0.8938</td>
<td>0.9197</td>
<td>0.9979</td>
<td></td>
</tr>
<tr>
<td>Rotation(150)</td>
<td>0.5448</td>
<td>0.9114</td>
<td>0.8933</td>
<td>0.9393</td>
<td></td>
</tr>
<tr>
<td>Resizing512-256-512</td>
<td>0.5445</td>
<td>0.6459</td>
<td>0.6118</td>
<td>0.5773</td>
<td></td>
</tr>
<tr>
<td>Compression</td>
<td>0.6791</td>
<td>0.6551</td>
<td>0.6489</td>
<td>0.6187</td>
<td></td>
</tr>
</tbody>
</table>

Table 2. Imperceptibility (dB.) Compression Table in Proposed Scheme, Liu et al. [3], and Ghazy et al. [9] with Watermarked Image Rudra in Different Domain

<table>
<thead>
<tr>
<th>Domain</th>
<th>Proposed Scheme</th>
<th>Liu et al.[3]</th>
<th>Ghazy et al. [9]</th>
</tr>
</thead>
<tbody>
<tr>
<td>Spatial</td>
<td>51.8412</td>
<td>60.5250</td>
<td>45.8749</td>
</tr>
<tr>
<td>RDWT</td>
<td>53.7851</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>DWT</td>
<td>47.2581</td>
<td>61.1391</td>
<td>46.3865</td>
</tr>
<tr>
<td>DCT</td>
<td>48.9857</td>
<td>60.5284</td>
<td>49.7598</td>
</tr>
</tbody>
</table>
4. Experimental Results

In this section some experiments are executed by using the MATLAB 13a and find out the results and also checked the performance of the proposed scheme. In our experiments two gray scale standard images (Lena, Rudra) of size (515×512) and each block size is 64×64. Different block size can be use but this size has less complexity. Figure 7 (i) shows that the correlation coefficient is more than 0.5 for all extracted watermarks. This ensures that in the absence of attacks, the watermark can extract perfectly. In this paper results are given by taking Rudra as host image and f logo as a watermark image. For tradeoff between imperceptibility and robustness, we have taken two scaling factor for embedding the watermark into the host image are 0.02 for LL sub band and 0.002 for other sub bands are taken in this scheme. The imperceptibility analysis can be measured by calculating the PSNR (peak signal to noise ratio) value. The acceptable value of PSNR is 30 db.

The PSNR can be calculated by the given formula as.

$$PSNR = 10 \log_{10} \left( \frac{\text{max}(x(i,j))^2}{\text{MSE}} \right)$$

MSE (Mean square error between host image x and watermarked image y can be calculated as

$$MSE = \frac{1}{m \times n} \sum_{i=1}^{M} \sum_{j=1}^{N} [x(i,j) - y(i,j)]^2$$

For robustness we can calculate the normalize correlation coefficient (NCC) by given formula.

$$NC(w, \bar{w}) = \frac{\sum_{i=1}^{M} \sum_{j=1}^{N} [w(i,j) - \mu_w][\bar{w}(i,j) - \mu_{\bar{w}}]}{\sqrt{\sum_{i=1}^{M} \sum_{j=1}^{N} [w(i,j) - \mu_w]^2} \sqrt{\sum_{i=1}^{M} \sum_{j=1}^{N} [\bar{w}(i,j) - \mu_{\bar{w}}]^2}}$$

Where $N$ and $M$ present the no of pixel in watermark. $w, \bar{w}$ are original watermark and extracted watermark and are mean of original watermark and extracted watermark. Here we apply six attacks Gaussian noise with zero mean and 0.01 variance, blurring using an average filtering, cropping, resizing(512-256-512), rotation(150) and compression, on watermarked image, whose results have been shown in the Table.1 and also these results, compared with the other previous scheme in Table.3 and get the better results. In our proposed scheme (Rudra) has been taken as host image and their corresponding watermarked image which is shown in Figure 7. The PSNR value of watermarked image Rudra is (53.7851dB.) and for Lena is 53.164dB.) It shows a big similarity between the host images and their corresponding watermarked images. The robustness can be calculated by finding the Normalized Cross-Correlation (NCC) from equation (17). The value of NCC should be in the range between −1 and 1. If the value of NCC closes to +1 then the extracted watermark is strongly correlated. If it is close to −1, the extracted watermark is also strongly correlated, but it seems to be a negative images. And if it is near 0, the extracted watermark is completely uncorrelated generally the NC acceptable value is 0.75 or above. The highest correlation coefficient between extracted watermark and original watermark is 0.9989 with no attack, values are given in Table.3. From Figure 7 and experimental values of PSNR in Table.2, it shows that our proposed scheme is highly imperceptible.
The extracted watermark image and reconstructed image of LL sub bands after applying attacks Gaussian noise, blurring, cropping, resizing, rotation and compression are shown in Figure 10, whose highest correlation coefficient values are also given in Table 3 and by seeing these values, We can say that the presented scheme is rich in terms of robustness and imperceptibility in comparison to previously proposed methods.

Comparative Study

In this section, we compare the results of the proposed scheme with Liu et al. [3], Ghazy et al. [9] scheme is shown in Table 3. Liu et al. [3] Proposed SVD-based watermarking method that performs the embedding process to the singular values of the whole image. The main fragility in their systems is watermark degrade due to some image processing attacks. Ghazy et al. [9] proposed a block-by block SVD based techniques and solves this shortcoming and get better results, but the size of watermark is very small as compared to the host image. Comparative char is shown in Figure 12. Here (a) is without attack (b) is Gaussian noise with zero mean and 0.01 variance (c) is blurring using an average filtering (d) is cropping, (e) is resizing(512-256-512) (f) is rotation(150) and (g) is compression attacks.

Comparative Chart

![Figure 12. Competitive Chart where a, b, c, d, e, f, g are Attacks](image-url)
In our proposed scheme we use RDWT and encrypted watermark to enhance its privacy and robustness. This presented block-by-block RDWT-SVD based method more robust against compression, cropping, rotation, blurring, Gaussian noise, resizing and rotation. After seeing the NCC values in Table 3, comparative chart, Figure 8, 9, 10, we can say that our proposed method is more robust than previously proposed techniques.

5. Conclusion

In this paper, we present a digital image watermarking scheme based on RDWT and block-SVD, to embed an encrypted (scramble) watermark image in the singular values of each block with all RDWT sub bands of the gray scale host image. The advantage of block based method is, to attend the each block independently, so each block with a distinct key can be used to increase the security. Also the size of the payload of each block depends on its characteristics may vary from one block to another, which enhance the visual quality and robustness by comparing the size of payload with these characteristics. This scheme has the high embedding capacity and a little degradation in the image due to the RDWT-SVD properties. Encrypted watermark inserted in the LL sub band is resist to some attacks and for other sub bands (LH, HL, HH) is resisted to other attacks to enhance the robustness of this scheme. So it is difficult to remove or destroy the watermark from all sub bands. The experimental results show that it is more robust against JPEG compression, cropping, rotation, blurring, Gaussian noise, resizing attacks and also improve the performance in terms of imperceptibility, capacity, and security. The future scope of this presented scheme is, by using a multilevel decomposition of RWDT with optimization techniques for different images to make it adaptive and get the better results.

References


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