Measuring Semantic Similarity of Word Pairs Using Path and Information Content

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Abstract

Measuring semantic similarity of word pairs is a popular topic for many years. It is crucial in many applications, such as information extraction, semantic annotation, question answering system and so on. It is mandatory to design accurate metric for improving the performance of the bulk of applications relying on it. The paper presents a new metric for measuring word sense similarity using path and information content. Different from previous works, the new metric not only reflects the semantic density information, but also reflects the path information. It is evaluated on the dataset provided by Rubenstein and Goodenough. Experiments demonstrate that the coefficient based on our proposed metric with human judgment is 0.8817, which is significantly outperformed than other existing methods.

Keywords: semantic similarity, word pairs, path, information content, WordNet

1. Introduction

Measuring semantic similarity of word pairs is a general issue in linguistics, cognitive science, and artificial intelligence. It has been successfully applied in word sense disambiguation [1], information extraction [2], semantic annotation and summarization [3-4], recommender system [5], question answering [6], and so on. Besides this, it also shows its talents in software domain [7] and bio-informatics domain [8]. Therefore a proper metric is curial for improving the performance of the bulk of applications relying on it. Many metrics have been proposed from different of view. Some metrics take the structure information into considered, and others assume that the semantic density information should be taken into account. Therefore, all the metrics can be divided into two classes: path based metrics and information content based metrics. Path based metrics assess semantic similarity by counting the number of edges separating two concepts. Information Content(IC) based metrics exploit the notion of Information Content (IC) of concepts. All the metrics are intuitive, simple and effective. However, they can’t distinguish different concepts pairs. The paper proposes a new metric for measuring word sense similarity combining path and information content.

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We evaluate the new metric on the data set of Rubenstein and Goodenough. Experiments show that the coefficient of our proposed metric with human judgment is 0.8817, which demonstrates that the new metric significantly outperformed than related work.

The rest of the paper is as follows: we introduce WordNet, definitions of related concepts and related works in section 2. In Section 3 a new semantic similarity metric of word pair using information content and path based on WordNet is proposed. In the new metric not only the semantic density information, but also the path information has been reflected. In section 4 we compare the six chosen metrics with our new algorithm by calculating the coefficients of correlation with human judgments of semantic similarity on the dataset provided by Rubenstein and Goodenough to evaluate the performance. Section 5 illustrates conclusion and future work.

2. Related Work

2.1. WordNet

The metrics in the paper are all based on WordNet. It is necessary to give a brief introduction.

Figure 1. A Fragment is-a Hierarchy Taxonomy in WordNet
WordNet is the product of a research project at Princeton University which has attempted to model the lexical knowledge of a native speaker of English [9]. Now it has become a valuable resource and plays an important role in human language technology. WordNet focuses on the word meanings instead of word forms. In WordNet nouns, verbs, adjectives, and adverbs are represented by a synset, which denotes a concept or a sense of a group of terms. These synsets are organized into taxonomic hierarchies via a variety of semantic relations, which makes it a useful tool for computational linguistics and natural language processing.

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In WordNet these semantic relations for nouns include hyponym/hypernym (is-a), part meronym/part holonym (part-of), member meronym/member holonym (member-of), substance meronym/substance holonym (substance-of) and so on. Figure 1 illustrates a fragment in WordNet. In Figure 1 we can see that car is an automobile vehicle, and rim is part of wheel, and person is member of people.

In this paper, we are only concerned about the similarity metrics based on is-a relations of WordNet. Some metrics have been proposed in past years. Generally the typical metrics based on WordNet can be grouped into two categories: path-based metrics and information-based metrics. Next, we will introduce these metrics briefly.

2.2. Definitions

Definition of related concept in the following metrics as follows:

1. \( \text{len}(c_i,c_j) \): the length of the shortest path from synset \( c_i \) to synset \( c_j \) in WordNet. eg. \( \text{len(bus,train)} \) is 2.
2. \( \text{ls}(c_i,c_j) \): the most specific common subsumer of \( c_i \) and \( c_j \). eg. \( \text{ls(bus,train)} \) is public transport.
3. \( \text{depth}(c_i) \): the length of the path to synset \( c_i \) from the global root entity. Here \( \text{depth(root)} \) is set to 1. eg. \( \text{depth(bus)} \) is 7.
4. \( \text{deep_max} \): the max depth(\( c_i \)) of the taxonomy. In Figure1 \( \text{deep_max} \) is 10.
5. \( \text{hypo}(c) \): the number of hyponyms for a given concept \( c \). eg. \( \text{hypo(software)} \) is 2.
6. \( \text{node_max} \): the maximum number of concepts that exist in the taxonomy.
7. \( \text{sim}(c_i,c_j) \): semantic similarity of concept \( c_i \) and concept \( c_j \).

2.3. Semantic Similarity Metrics

2.3.1. Path Based Metrics

Path based metrics proceed from the position of each concept in the taxonomy to obtain semantic similarity and assess semantic similarity by computing geometric distance separating two concepts, such as the number of edges. It is based on the assumption that the similarity of two concepts is related with the path length between two concepts and depth of each concept in the taxonomy respectively.
In a paper on “translating English verbs into Mandarin Chinese”, Wu and Palmer (W&P) presented a scaled metric for measuring the similarity between a pair of concepts \(c_1\) and \(c_2\). It is defined by how closely they are related in the hierarchy taxonomy. Formally, the metric is as follows [10]:

\[
sim_{W&P}(c_1, c_2) = \frac{2 \cdot \text{depth}(\text{iso}(c_1, c_2))}{\text{len}(c_1, c_2) + 2 \cdot \text{depth}(\text{iso}(c_1, c_2))}
\]

(1)

It is noticed that the similarity between two concepts \((c_1, c_2)\) is inversely proportional to length \((c_1, c_2)\) and proportional to depth \((\text{iso}(c_1, c_2))\). The values are range from 0 to 1.

Leakcock and Chodorow (L&C) took the maximum depth of taxonomy into account and proposed the following metric [11]:

\[
sim_{L&C}(c_1, c_2) = -\log \frac{\text{len}(c_1, c_2)}{2 \cdot \text{deep}_{\max}}
\]

(2)

It assumes that the similarity between two concepts was the function of the shortest path from \(c_1\) to \(c_2\) and depth of the taxonomy. For a specific version of WordNet, \(\text{deep}_{\max}\) is a fixed value. Therefore in the taxonomy, the smaller shortest path that two concepts have, the more similar they are. In practice, if two words have the same sense, \(c_1\) and \(c_2\) are the same node in the taxonomy. Then \(\text{len}(c_1, c_2)\) is 0, so we may add 1 to both \(\text{len}(c_1, c_2)\) and \(2 \cdot \text{deep}_{\max}\) to avoid \(\log(0)\). The values of \(\text{sim}_{L&C}(c_1, c_2)\) are range from 0 to \(\log (2 \cdot \text{deep}_{\max}+1)\).

Li et al., [12] uses multiple information sources to calculate the semantic similarity of concepts and proposes a metric based on the assumption that information sources are infinite to some extent while humans compare word similarity with a finite interval between completely similar and nothing similar. Intuitively the transformation between an infinite interval to a finite one is non-linear [13], which is expressed by:

\[
sim_{Li}(c_1, c_2) = e^{-\alpha \cdot \text{len}(c_1, c_2)} \frac{e^{\beta \cdot \text{depth}(\text{iso}(c_1, c_2))}}{e^{\beta \cdot \text{depth}(\text{iso}(c_1, c_2))} + e^{-\beta \cdot \text{depth}(\text{iso}(c_1, c_2))}}
\]

(3)

It is noticed that Li’s metric combines the shortest path and the depth of concepts in a non-linear function. Where \(\alpha (\alpha > 0)\) and \(\beta (\beta > 0)\) are parameters and used to adjust the contribution of shortest path length (ie. length \((c_1, c_2)\)) and depth (ie. depth \((\text{iso} (c_1, c_2))\) respectively, which need to be adapted manually for good performance. In our experiment the same as in literature [8]’s, \(\alpha\) is set to 0.2 and \(\beta\) is set to 0.6. It is noted that \(\text{sim}_{Li}(c_1, c_2)\) will increasing with respect to depth \((\text{iso} (c_1, c_2))\) and decreasing with \(\text{len} (c_1, c_2)\). The values of \(\text{sim}_{Li}(c_1, c_2)\) are range from 0 to 1.

2.3.2. Information Content Based Metrics

The notion of information content of the concept is directly related to the frequency of the term in a given document collection. The frequencies of terms in the taxonomy are estimated using noun frequencies in some large collection of texts [14]. The idea behind semantic
similarity information content metrics is that each concept includes much information in WordNet. It assumes that the similarity of two concepts is related to information they share in common. The more common information two concepts share, the more similar the concepts are.

In 1995 Resnik first proposed information content based similarity metric [15]. It assumed that for a concept $c$, 

$$IC = -\log p(c)$$

(4)

Where $p(c)$ is the probability of encountering and instance of concept $c$.

Probability of a concept was estimated as follows:

$$p(c) = \frac{freq(c)}{N}$$

(5)

Where $N$ is the total number of nouns, and $freq(c)$ is the frequency of instance of concept $c$ occurring in the taxonomy.

When computing $freq(c)$, each noun or any of its taxonomical hyponyms that occurred in the given corpora was included.

$$Freq(c) = \sum_{w \in W(c)} count(w)$$

(6)

Where $W(c)$ is the set of words subsumed by concept $c$.

For two given concepts $c_1$, $c_2$, the similarity is indicated by a highly specific concept that subsumes them both in the taxonomy

$$sim_{Resnik}(c_1, c_2) = -\log p(lso(c_1, c_2)) = IC(lso(c_1, c_2))$$

(7)

It is noticed that $sim_{Resnik}(c_1, c_2)$ is depended by concept pairs’ most specific subsumer in the taxonomy. Lin took the IC of compared concepts into account respectively and proposed another metric for similarity metric [16]. This metric uses both the amount of information needed to state the commonality between the two concepts and the information needed to fully describe these concepts.

$$sim_{Lin}(c_1, c_2) = \frac{2 * IC(lso(c_1, c_2))}{IC(c_1) + IC(c_2)}$$

(8)

We can see that:

(1) A term compared with itself will always score 1.
(2) The similarity values are range from 0 to 1.

Contrary to the above similarity metrics, Jiang proposed a metric from a different point of view. He calculated semantic distance to obtain semantic similarity [17]. Semantic similarity is the opposite of the distance.
It is noted that the IC value of each concept is an important dimension in assessing the similarity of two concepts or two words and provides an estimation of its abstract or specialty. Generally speaking, there are two methods to obtain IC. One is Corpora-dependent IC metric. Corpora-dependent IC metric obtains IC through statistical analysis of corpora. The other is Corpora-independent IC metric. Recent years the latter has drawn great concern. One commonly used IC model was proposed by Nuno. The model use WordNet as a statistical resource to compute the probability of occurrence of concepts. It is based on the assumption that the taxonomic structure of WordNet is organized in a meaningful and structured way, where concepts with many hyponyms convey less information than concepts that are leaves. As of this, the more hyponyms a concept has the less information it expresses. Likewise, concepts that are leaf nodes are the most informative in the taxonomy. In other words, the Information Content of a WordNet concept is commented as a function of the population of its hyponyms[13]. The model is defined as [18]:

$$\text{IC}(c) = 1 - \frac{\log(\text{hypo}(c) + 1)}{\log(\text{node\_max})}$$  \hspace{1cm} (10)$$

According to formula (10), two concepts with the same number of hyponyms will have the same IC values.

3. A New Semantic Similarity Metric Based on WordNet

In this section, let’s take Figure 1 as example and discuss the metrics stated above. Firstly, let’s discuss path-based metrics.

It is noticed that, len (mail, bicycle) and len (wheeled vehicle, bus) are both equal to 4. For a specific version of WordNet, deep_max is a fixed value. Therefore, the two pairs will have the same similarity value with L&C’s metric. Another fact must be noted that, both Iso (mail, bicycle) and Iso (wheeled vehicle, bus) are conveyance. This fact make the two pairs will have the same similarity value with Wu&Palmer’s metric and Li’s metric, too.

Next, let’s analyze information content based metrics.

If two pairs have the same most specific subsumer, they will have same similarity values with Resnik’s metric. For example, in Figure 1, sim(bus, train) is equal to sim(bus, boat train).

Lin’s metric and Jiang’s metrics have taken the IC of compared concepts into account respectively. If the summation of IC of compared two pairs with the same lowest subsumer is equal, they will have the same similarity values. For example, in Fig.1 the IC value of all the leaves is equal to 1 according to formula (10), which makes the similarity values of pairs (mail, car) and pairs (school bus, car) are equal.

Based on stated above, it is noted that the similarity metric could not distinguish different concepts pairs effectively. There is still room for improvement.

Here a new metric is presented, which takes account not only path length, but also local density information. It combines information content and paths of concepts, formally:
Where \( k \) is a parameter, and \( 0 \leq k \leq 1 \), which can be adapted manually to make the metric to get the best performance.

We can see that,

1. Sim\(_{\text{new}}\)(\( c_1, c_2 \)) is inversely proportional to \( \text{len}(c_1, c_2) \). If \( \text{len}(c_1, c_2) = 0 \), Sim\(_{\text{new}}\)(\( c_1, c_2 \)) get the maximum value of 1.

2. Because \( 0 \leq 2 \cdot \text{IC(ISO)})/(\text{IC}(c_1) + \text{IC}(c_2)) \leq 1 \), as \( \text{len}(c_1, c_2) \) increases to \( \infty \), Sim\(_{\text{new}}\)(\( c_1, c_2 \)) is close to 0.

3. Therefore the values of Sim\(_{\text{new}}\)(\( c_1, c_2 \)) are range from 0 to 1.

4. If two pairs have the same most specific subsumer and the sum of IC are the same too, but their length path are not equal, they will have different similarity values.

In next section, we will analyze our new metric from different perspectives.

4. Evaluation

In this section, we evaluated the results by correlating our similarity values with that of human judgments.

4.1. Data set and Words Similarity Calculating Method

In the experiment, the dataset provided by Rubenstein and Goodenough (1965) [19] was adopted. In R&G’s study, 51 undergraduate subjects were asked for rate 65 pairs of words, which ranged from “highly synonymous” to “semantically unrelated”. Subjects were asked to rate them on the scale of 0.0 to 4.0. In formula (11), the k value is very important, which decides the performance of the metric. We compute different correlation coefficients between proposed metric and human judgments corresponding to different k values. Because either or both of the words have more than one sense in WordNet, in the result, we took the most similarity pair of sense.

\[
\text{sim}(\text{Word}_1, \text{Word}_2) = \max_{(i,j)} \{\text{sim}(c_{i1}, c_{j2})\}
\]

Experiments show that when k is 0.08, the correlation gets the maximum value 0.8817.

4.2. Results Analysis

Before our analysis we first compute semantic similarity between pairs of words with the six chosen metrics listed in Section 2 and the new metric. Then the semantic similarity distributed graph with different metrics is illustrated in Figure 2. For the convenience of expression and comparison, the values are normalized in \([0, 1]\). The IC value is obtained according formula (10).
In accordance with previous research, we compare the six chosen metrics with our new algorithm by calculating the coefficients of correlation with human judgments of semantic similarity. The results are shown in Table 1.

**Figure 2. Semantic Similarity Distributed Graph with Different Metrics**

For the convenience of comparison intuitively, the compared results of our proposed metric with other six metrics are provided in Figure 3.
5. Conclusion and Future Work

This paper presents metric for measuring word sense similarity using path and information content. It combines path based metric and information content based metric. Different from previous works, in the new metric not only the semantic density information, but also the path information has been reflected. We evaluate our model on the data set of Rubenstein and Goodenough and compare the results of our proposed metric with Wu&palmer’s metric, Leacock&Chodorow’ metric, Li’s metric, Resnik’s metric, Lin’s metric and Jiang’s metric. The distributed graphs of 65 word pair’s similarity value with different metrics are illustrated. Experiments show that the coefficient of our proposed metric with human judgment is 0.8817, which is significantly outperformed than related works. In future work, we will put the metric into query suggestion, ontology construction, documents clustering and so on for practical application.

Reference


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