A Petri Net Processing Model of STeCEQL

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Abstract

The internet of vehicles is an important internet of things. It is an urgent problem that how to real-time processes these spatial and temporal data of the internet of vehicles. The complex event processing technology can filter the concerned data to the event by the complex event query language (EQL) and the system can responds effectively. The STeCEQL is a complex event language for the internet of vehicles, which constraint with spatial and temporal. The processing model of the complex event language is a core issue of the complex event processing technology. In this paper, we established a Petri Net processing model of STeCEQL. We give all kind of processing model of STeCEQL expressions. And these processing models are synthesized by two types of basic Petri Net model: the sequence structure and the logic and structure. Finally, we proved the Petri Net processing model of STeCEQL is structural boundedness and structural conservativeness, but it is not structural repetitiveness.

Keywords: internet of things, mobile system, complex event query language, complex event processing model, Petri Net

1. Introduction

The internet of vehicles is an important achievement of the internet of things [1]. There are not only a large number of non-mobile agents in the internet of vehicles, but also a lot of fast-moving mobile agents. In the system, the various sensors carried by each agent produce a continuous flood of data: time, position, direction, speed, temperature, *etc* [2, 3]. However, the conventional database technology can not deal these data effectively.

In recent years, the complex event processing technology has been successfully applied in the internet of vehicles projects. In internet of vehicles, the large amount of raw data generated by various sensors is seen as basic events. Through the complex event query language, the system will filter these basic events into meaningful complex events. Therefore, the massive amounts of data of the system can be effectively processed in real time. Moody K proposed a complex event of query language of internet of vehicles: SpaTec. This EQL has been applied to the London's bus monitoring system [4, 5]. Jin B proposed a complex event query language of internet of vehicles: CPSL [6]. We also proposed a complex event query language: STeCEQL. And it can describe a variety of temporal and spatial attributes of the events.

The processing model of the complex event query language is the core mechanism for dealing with massive data of the system. There are four types processing model of the EQL: Finite Automata Model [7,8], Matching Tree model[9,10], Directed Acyclic Graph model[11,12], Petri Net model[13,14].Petri Net can be used to model the systems with concurrent, asynchronous, distributed, non-deterministic, parallel and other characteristics. And it is considered to be the most powerful tool for studying discrete event systems. Meanwhile, Petri Net is a strictly defined mathematical model. The Petri Net methods can

analyze the structure of the system and the behavior of the dynamic characteristics of the system. In the internet of vehicles, complex event processing system is a typical distributed asynchronous concurrent system, so we use the Petri Net models.

In this paper, we have made the processing model of STeCEQL by Petri Net and analyzed the relevant properties of the model. The remainder of this paper is organized as follows: Section 2 reviews the STeCEQL. Section 3 simply introduces the Petri Net theory. Section 4 gives the various processing models of STeCEQL expressions. Section 5 analyzes the characteristics of the Petri Net model and proves the related properties. The last Section concludes this paper.

2. STeCEQL Language

The STeCEQL is complex event query language for the internet of vehicles of event driven architecture. It can express the basic events and the complex events. The syntax of STeCEQL is as follows:

ABexp:

```
attribute ::= true | false | x_a = a | x_a! = a | x_a > a | x_a < a
```

 $| attribute_0 \land attribute_1 | attribute_0 \lor attribute_1$

TBexp:

 $time ::= true | false | x_t BEFORE t | x_t AFTER t$

 $|x_t EQUAL t| x_t OVERLAP t| x_t DURING t$

 $|time_0 \lor time_1|time_0 \land time_1$

LBexp:

location ::= true | false | $x_1 EQ l | x_1 OP l | x_1 IN l$

 $|x_1 \text{ NORTH } l | x_1 \text{ SOURTH } l | x_1 \text{ EAST } l | x_1 \text{ WEST } l$

 $|x_{i}| NORTHWEST l | x_{i}| NORTHEAST l$

 $|x_{i} SOURTHWEST l | x_{i} SOURTHEAST l$

 $|location_0 \lor location_1| locaiton_0 \land location_1|$

DBexp:

direction ::= true | false | $x_d = d | x_d! = d$

EBexp:

```
e ::= agent^{time}(attribute_1; attribute_2; attribute_3 \cdots)
```

```
|agent_{location}(attribute_1; attribute_2; attribute_3 \cdots)
```

```
|agent_{location}^{time}(attribute_1; attribute_2; attribute_3 \cdots)
```

```
|agent_{(location, direction)}^{time}(attribute_1; attribute_2; attribute_3 \cdots)
```

CEexp:

 $e ::= e_1 \land e_2 \mid e_1 \lor e_2$ $\mid e_1 BEFORE \mid e_2 \mid e_1 AFTER \mid e_2$ $\mid e_1 EQUAL \mid e_2 \mid e_1 OVERLAP \mid e_2 \mid e_1 DURING \mid e_2$ $\mid e_1 EQ \mid e_2 \mid e_1 OP \mid e_2 \mid e_1 IN \mid e_2$ $\mid e_1 NORTH \mid e_2 \mid e_1 SOURTH \mid e_2 \mid e_1 EAST \mid e_2 \mid e_1 WEST \mid e_2$

 $|e_1 NORTHWEST |e_2||e_1 NORTHEAST |e_2$

$|e_1 SOURTHWEST e_2 |e_1 SOURTHEAST e_2$

3. The Petri Net Theory

Definition 1 Meet the following conditions triples N = (S, T; F) is called Network:

 $(1)^{\mathsf{S}} \cup T \neq \emptyset$ $(2)^{\mathsf{S}} \cap T = \emptyset$ $(3)^{\mathsf{F}} \subseteq S \times T \cup T \times S$ $(4)^{\mathsf{dom}(\mathsf{F})} \cup \mathsf{cod}(\mathsf{F}) = S \cup T$ $\mathsf{dom}(\mathsf{F}) = \{x \mid \exists x : (x, y) \in \mathsf{F}\}, \mathsf{cod}(\mathsf{F}) = \{y \mid \exists x : (x, y) \in \mathsf{F}\}.$

S and T are two disjoint sets, which are the basic elements of the network set N. S elements is called the S- or library (place), T elements called T- or changes (transition), F is the flow of the network N.

Definition 2 Let N = (S, T; F) is a net. Mapping M: $S \rightarrow \{0,1,2,...\}$ is called a marking of net N. The tuple (N, M) is called a marking net.

Definition 3 A Petri net system is a marking net $\Sigma = (S, T; F, M)$ and has the following transition firing rule:

(1)For transition $t \in T$, if $\forall s \in S : s \in t \rightarrow M(s) \ge 1$, then says that the transition t have the firing rule, denoted by M[t>.

(2)If M[t>, the under the marking M, the transition t can fire: the transition t fired from the marking M to the new marking M', denoted by M[t> M'.

And $\forall s \in S$, $M'(s) = \begin{cases} M(s) - 1, & \text{if } s \in t - t \\ M(s) + 1, & \text{if } s \in t - t \\ M(s), & \text{else} \end{cases}$

Definition 4 Let $\Sigma = (S, T; F, M)$ is a Petri net, $S = \{s1, s2, \dots, sm\}, T = \{t1, t2, \dots, tn\}$, then the structure of the Petri net $\Sigma(S, T; F)$ can be expressed by a matrix of n rows and m

columns A=[a_{ij}]_{n×m}. $a_{ij} = a_{ij}^{+} - a_{ij}^{-}$, i \in (1,2,...,n), j \in (1,2,...,m), $a_{ij}^{+} = \begin{cases} 1, i f(t_{i}, s_{j}) \in F; \\ 0, else; \end{cases}$, $a_{ij}^{-} = \begin{cases} 1, i f(s_{j}, t_{i}) \in F; \\ 0, else; \end{cases}$,

A is called incidence matrix of the Σ (or net N = (S, T; F)).

Theorem1 Let A is the incidence matrix of the network N = (S, T; F), then the necessary and sufficient conditions of the N is structural boundedness are: there is a m(m=|S|) dimensional vector of positive integers Y make AY ≤ 0 .

Theorem2 Let A is the incidence matrix of the network N = (S, T; F), then the necessary and sufficient conditions of the N is structural conservativeness are: there is a m(m=|S|) dimensional vector of positive integers Y make AY=0.

Theorem3 Let A is the incidence matrix of the network N = (S, T; F), then the necessary and sufficient conditions of the N is structural repetitiveness are: there is a n(m=|T|) dimensional vector of positive integers X make $ATX \ge 0$.

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These are some basic concepts and key theorems of Petri net models. In the modeling process, the calculation of Petri net is also important. These calculations include: insert, delete, replace, synthesis and decompose. Here is the definition of combination computing.

Definition 5 Let Ni=(Si,Ti;Fi), i=1,2, $S_1 \cap S_2 \neq \emptyset$, $T_1 \cap T_2 = \emptyset$, then

 $N = (S_1 \cup S_2, T_1 \cup T_2; F_1 \cup F_2)$ is called a shared combination net of N1 and N2, denoted by N=N1CsN2.

Theorem4 Let net N is the shared combination net of N1 and N2, N=N1CsN2. then:

(1) If the net N1 and N2 is structural boundedness, then the net N is also structural boundedness.

(2) If the net N1 and N2 is structural conservativeness, then the net N is also structural conservativeness.

(3) If the net N1 and N2 is structural repetitiveness, then the net N is also structural repetitiveness.

4. The Petri Net Processing Model of STeCEQL

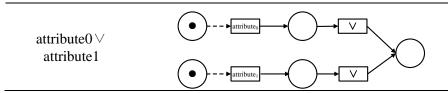
In the Petri net processing model of complex event query language, we use the input library of Petri net indicate the basic events and the output library of Petri net express the complex events. The number of the tokens in the library represents the number of event instances. When an event instance is coming, the number of the token in the library will be changed. Through calculating the transition function, the model can determine whether the transition conditions are met. If the transition rule is satisfied, the transition will fire and the status of the input and the output library will change.

We establish the Petri net processing model of all kinds of STeCEQL expressions. Assuming that the capacity of each library is limited and the number of token in libraries represents the number of the event instances.

ABexp:

ABexp	Petri net model
x _a =a	
x _a !=a	$\bullet \qquad \qquad$
x _a >a	
x _a <a< td=""><td></td></a<>	
attribute0 attribute1	

Table 1. The Model of ABexp



The Petri net processing models of ABexp of STeCEQL are in Table 1. From the table, we can conclude that the four kind expressions: $x_a=a$, $x_a!=a$, $x_a>a$ and $x_a<a$ have the similar basic net structure. The dotted lines of the logic and operation and the arithmetic operation model indicate that there are many libraries and transitions in the front sets of the model.

TBexp:

TBexp	Petri net model	
x _t BEFORE t	• X, BEFORE t	
$time_0 \wedge time_1$		
$time_0 \lor time_1$		

Table 2. The Model of TBexp

The Petri net processing models of TBexp of STeCEQL are in table 2. We only list the model of expression x_t BEFORE t and the other expression's models are similar. The dotted lines of the logic and operation and the logic or operation model indicate that there are many libraries and transitions in the front sets of the model.

LBexp:

	-	
LBexp	Petri net model	
$x_1 EQ 1$	$\bullet \qquad \qquad$	
$location_0 \land location_1$	● → location → ↓ ∧ → ↓	
$location_0 \lor location_1$	$ \underbrace{\bullet}_{} \underbrace{\bullet}_{\text{location}_0} \underbrace{\vee}_{\text{V}} \underbrace{\vee}_{$	

The Petri net processing models of LBexp of STeCEQL are in Table 3. We only list the model of expression x_1 EQ l and the other expression's models are similar. The dotted lines of

the logic and operation and the logic or operation model indicate that there are many libraries and transitions in the front sets of the model.

DBexp:

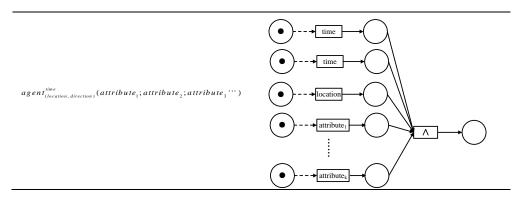
Table 4. The Model of DBexp			
DBexp	Petri net model		
x _d =d			
$x_d!=d$	$\textcircled{\bullet} \xrightarrow{x_d \neq d} \xrightarrow{x_d \neq d}$		

A The Medal of DD Table

EBexp:

EBexp	Petri net model
agent ^{time} (attribute ₁ ; attribute ₂ ; attribute ₃ ···)	$ \underbrace{\bullet}_{+} \underbrace{\operatorname{time}}_{\operatorname{tribute}_1} \underbrace{\bullet}_{\operatorname{tribute}_2} \underbrace{\bullet}_{\operatorname{tribute}_k} \underbrace{tribute}_k} \underbrace{\bullet}_{trib$
agent _{incation} (attribute ₁ ; attribute ₂ ; attribute ₃ ····)	$\bullet \xrightarrow{\text{location}} \\ \bullet \text{locat$
agent ^{time} (attribute ₁ ; attribute ₂ ; attribute ₃)	$\bullet \xrightarrow{\text{time}} \\ \bullet \xrightarrow{\text{location}} \\ \bullet \xrightarrow{\text{location}} \\ \bullet \xrightarrow{\text{location}} \\ \bullet \xrightarrow{\text{direction}} \\ \bullet \xrightarrow{\text{direction}} \\ \bullet \xrightarrow{\text{location}} \\ \bullet \xrightarrow{\text{direction}} \\ \bullet \text{directi$

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The Petri net processing models of EBexp of STeCEQL are in Table 5. We list the models of the four basic expressions. The dotted lines of the model indicate that there are many libraries and transitions in the front sets of the model.

CEBexp:

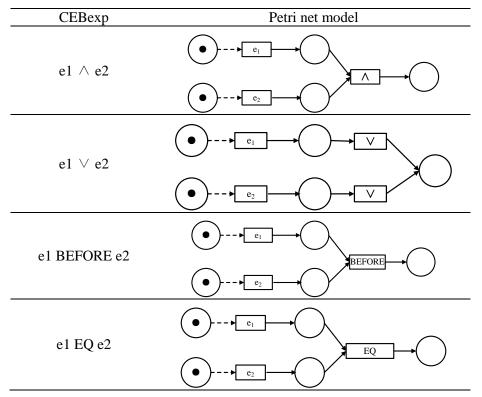


Table 6. The Model of CEBexp

The Petri net processing models of CEBexp of STeCEQL are in table 6. We only list the model of expression e1 EQ e2 and e1 BEFORE e2, the other expression's models are similar. The dotted lines of model indicate that there are many libraries and transitions in the front sets of the model.

According to the above Petri net models, we can compose various models of all kind of STeCEQL expressions. The following are two examples:

Example1

```
cel: car1_{(x_t \ EQ \ (500,1300)\}, x_d = NORTH)}^{(x_t \ DURING \ (14:38:30,14:38:40)\})}(x_v > 124).
```

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The Petri net processing model is as Figure 1.

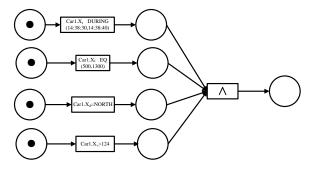


Figure 1. The Processing Model of e1

Example 1

e1: $car 5_{(x_{t} \ BEFORE \{(9:30:8:26:30)\})}^{(x_{t} \ DURING \{(8:26:30,8:26:35)\})}_{(x_{t} \ IN \{(695,85),(697,85)\},x_{d} = EAST\}}(x_{v} > 60 \land x_{v} < 95),$ $e2: car 6_{(x_{t} \ BEFORE \{(9:30:42,9:40:03)\})}^{(x_{t} \ BEFORE \{(9:30:42,9:40:03)\})}_{(x_{t} \ EQUAL \{(1324,90)\},x_{d} = NORTHEAST\}}(x_{v} \le 120),$

ce2: e1 OVERLAP e2.

The Petri net processing model is as Figure 2.

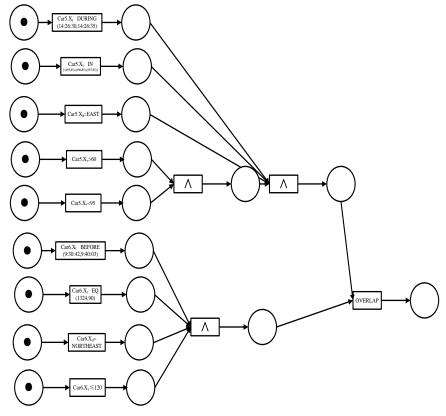


Figure 3. The Processing Model of ce1

5. Analysis of the Petri Net Model of STeCEQL

5.1. The Characteristic of the Petri Net Model of STeCEQL

From the models of tables 1 to 6, the processing models of STeCEQL consist of the sequence structure model and the logic and structure model. The sequence structure model is as Figure 3. The logic and structure model is as Figure 4.

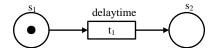


Figure 3. The Petri Net Model of Sequence Structure

As the Figure 3 shows, the Petri net model consists of two libraries s1 and s2, a transition t1. According to this model, its incidence matrix as below:

The output matrix: $a_{ij}^+ = \begin{bmatrix} 0 & 1 \end{bmatrix}$, and the input matrix: $a_{ij}^- = \begin{bmatrix} 1 & 0 \end{bmatrix}$, So the incidence matrix is $A_1^- = a_{ij}^+ - a_{ij}^- = \begin{bmatrix} -1 & 1 \end{bmatrix}$.

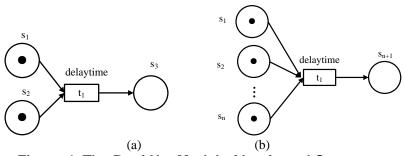


Figure 4. The Petri Net Model of Logic and Structure

As the Figure 4 shows, the Petri net model consists of multiple libraries and a transition t1. According to this model, its incidence matrix as below:

As the Figure 4 (a) shows, if there are two branches in the model. The output matrix:

$$a_{ij}^{+} = \begin{bmatrix} 0 & 0 & 1 \end{bmatrix}$$
, the output matrix: $a_{ij}^{-} = \begin{bmatrix} 1 & 1 & 0 \end{bmatrix}$, so the incidence matrix:
 $A_{2} = a_{ij}^{+} - a_{ij}^{-} = \begin{bmatrix} -1 & -1 & 1 \end{bmatrix}$

As the figure4 (b) shows, if there are multiple branches in the model. The input matrix:

$$a_{ij}^{+} = [0 \ 0 \ \cdots \ 1]$$
, and the output matrix: $a_{ij}^{-} = [1 \ 1 \ \cdots \ 0]$, so
the incidence matrix: $A_{3}^{+} = a_{ij}^{+} - a_{ij}^{-} = [-1 \ -1 \ \cdots \ 1]$.

5.2. Analysis of the Petri Net Model of STeCEQL

According to the Petri net models of STeCEQL, we analyze the properties of these structures.

Property1 the Petri Net models of the STeCEQL are structural boundedness. Proof: Let N0=(S, T; F) is the basic net of a STeCEQL expression,

Case1: when N0 only include the basic sequence structure as Figure 3,

the incidence matrix: $A_1 = a_{ij}^+ - a_{ij}^- = [-1 \ 1]$, then exist $Y = \begin{bmatrix} 3 \\ 1 \end{bmatrix}$ make AY=-3+1=-2 \le 0.

According to theorem1, N0 is structural boundedness.

Case2: when N0 only include the structure as figure4 (a),

the incidence matrix: $A_2 = a_{ij}^+ - a_{ij}^- = [-1 - 1 1]$, then exist $Y = \begin{bmatrix} 3 \\ 3 \\ 1 \end{bmatrix}$ make $AY = -3 - 3 + 1 = -5 \le 0$.

According to theorem1, N0 is structural boundedness.

Case3: when N0 only include the structure as figure4 (b),

the incidence matrix:
$$A_3 = a_{ij}^+ - a_{ij}^- = [-1 - 1 \cdots 1]$$
, then exist Y=
3
3
 $\begin{bmatrix} 3\\ \\ \\ \\ \\ \\ \end{bmatrix}$
make AY=-3n+1=1-3n ≤ 0 .

According to theorem1, N0 is structural boundedness.

Because the Petri net processing models of STeCEQL consist of the sequence structure and the logic and structure. And these models are shared combination net. According to theorem4, the Petri net processing models of STeCEQL are structural boundedness.

We finish the proof of this theorem.

Property2 the Petri Net models of the STeCEQL are structural conservativeness. Proof: Let N0=(S, T; F) is the basic net of a STeCEQL expression,

Case1: when N0 only include the basic sequence structure as Figure 3,

the incidence matrix: $A_1 = a_{ij}^+ - a_{ij}^- = [-1 \ 1]$, then exist $Y = \begin{bmatrix} 1 \\ 1 \end{bmatrix}$ make AY=-1+1=0.

According to theorem2, N0 is structural conservativeness.

Case2: when N0 only include the structure as figure4 (a),

the incidence matrix:
$$A_2 = a_{ij}^+ - a_{ij}^- = \begin{bmatrix} -1 & -1 & 1 \end{bmatrix}$$
, then exist $Y = \begin{bmatrix} 2 \end{bmatrix}$ make AY=-1-1+2=0.

According to theorem2, N0 is structural conservativeness. Case3: when N0 only include the structure as figure4 (b), [1]

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the incidence matrix: A_3 = a_{ij}^+ - a_{ij}^- = [-1 - 1 - 1 - 1], then exist Y=
[1]
| |
|:|
\lfloor n \rfloor make AY=-n+n=0.
```

According to theorem2, N0 is structural conservativeness.

Because the Petri net processing models of STeCEQL consist of the sequence structure and the logic and structure. And these models are shared combination net. According to theorem4, the Petri net processing models of STeCEQL are structural conservativeness.

We finish the proof of this theorem.

Property3 the Petri Net models of the STeCEQL are not structural repetitiveness. Proof: Let N0=(S, T; F) is the basic net of a STeCEQL expression, Case1: when N0 only include the basic sequence structure as Figure 3,

the incidence matrix: $A_{i} = a_{ij}^{+} - a_{ij}^{-} = [-1 \ 1]$. If there is a $X = \begin{bmatrix} x_1 & x_2 \end{bmatrix}$ make A1TX ≥ 0 . Then $\begin{cases} -x_1 - x_2 \ge 0 \\ x_1 + x_2 \ge 0 \\ \end{cases}$ there are positive integer solutions. $\begin{cases} -x_1 - x_2 \ge 0 \\ x_1 + x_2 \ge 0 \end{cases} \xrightarrow{\rightarrow} x_1 + x_2 = 0 \\ \text{, so there are not positive integer solutions.} \end{cases}$ So, there are not X make A1TX \geq 0, According to theorem3, N0 is not structural repetitiveness. Case2: when N0 only include the structure as Figure 4 (a), the incidence matrix: $A_2 = a_{ij}^+ - a_{ij}^- = [-1 - 1 - 1]$ If there is a $X = \begin{bmatrix} x_1 & x_2 & x_3 \end{bmatrix}$ make A2TX ≥ 0 . $\left[-x_{1}-x_{2}-x_{3}\right] \geq 0$ $\begin{cases} -x_{1} - x_{2} - x_{3} \geq 0 \\ \end{array}$ Then $\begin{vmatrix} x_1 + x_2 + x_3 \\ x_1 + x_2 + x_3 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 + x_3 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 + x_3 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 + x_3 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_3 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_3 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_3 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_3 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_3 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_3 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_3 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_3 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_3 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_3 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_3 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_3 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_3 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_3 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_3 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_3 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_3 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_3 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_3 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1$ $\left(-x_{1}-x_{2}-x_{3} \geq 0\right)$ $\begin{cases} -x_{1} - x_{2} - x_{3} \geq 0 \rightarrow x_{1} + x_{2} + x_{3} = 0 \end{cases}$ But $\begin{bmatrix} x_1 + x_2 + x_3 \ge 0 \end{bmatrix}$, so there are not positive integer

solutions.

So, there are not X make A2TX ≥ 0 ,

According to theorem3, N0 is not structural repetitiveness.

Case3: when N0 only include the structure as Figure 4 (b),

the incidence matrix: $A_3 = a_{ij}^+ - a_{ij}^- = [-1 - 1]$ 1] If there is a $X=\begin{bmatrix} x_1 & x_2 & \cdots & x_{n+1} \end{bmatrix}$ make A3TX ≥ 0 , $\begin{bmatrix} -x_1 - x_2 - x_3 \ge 0 \end{bmatrix}$ $\begin{cases} | -x_1 - x_2 - x_3 | \ge 0 \end{cases}$ Then $\begin{vmatrix} x_1 + x_2 + x_3 \\ x_1 + x_2 + x_3 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 + x_3 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 + x_3 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 + x_3 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 + x_3 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 + x_3 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_2 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1 + x_3 \\ x_2 + x_3 \\ x_3 + x_3 \\ x_1$ $\left[-x_{1}-x_{2}-x_{3} \ge 0\right]$ $\begin{cases} -x_{1} - x_{2} - x_{3} \geq 0 \rightarrow x_{1} + x_{2} + x_{3} = 0 \end{cases}$ But $\int_{-\infty}^{\infty} x_1 + x_2 + x_3 \ge 0$, so there are not positive integer

solutions.

So, there are not X make A3TX ≥ 0 ,

According to theorem3, N0 is not structural repetitiveness.

Because the Petri net processing models of STeCEQL consist of the sequence structure and the logic and structure. And these models are shared combination net. According to theorem4, the Petri net processing models of STeCEQL are not structural repetitiveness.

We finish the proof of this theorem.

6. Conclusions

In this paper, we propose the Petri Net processing model of the STeCEQL. We analyse the relevant properties of the model. And we proved the Petri Net processing model of STeCEQL is structural boundedness and structural conservativeness, but it is not structural repetitiveness.

We only analyse the Petri Net processing model of the STeCEQL. Next, we will design the processing algorithms based the model and implement these algorithms.

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