

## Implementing A Data Mining Solution To Customer Segmentation For Decayable Products – A Case Study For A Textile Firm

Vahid Golmah and Golsa Mirhashemi

*Department of Computer Engineering, Islamic Azad University, Neyshabur Branch,  
Neyshabu, 6621901, Iran  
v.golmah@in.iut.ac.ir, mirhashemi.golsa@gmail.com*

### **Abstract**

*In this paper is developed a model to cluster customers who need to production change continuously. Mere mathematical models to cluster customers lead to ignoring the environment factors in model. Therefore, for Adjusting model to reality, we should use environment factors in model building. The proposed model is flexible against changes of environment and it causes to resulted model can use for clustering the customers of decay able productions. Proposed model perform on customer's information of a textile firm.*

**Key words:** *Customer segmentation, RFM model, Fuzzy Analytical Network process (FANP), Self organization Map (SOM)*

### **1. Introduction**

E-business is a new business model that transforms key business processes between customers, suppliers, employees, business patterns, provoking radical changes in the way in which businesses operate [1]. For most firms, becoming an e-business is an evolutionary journey from initial to final stages. This kind of transformation may involve adopting new technologies, redesigning business processes and restructuring management. To reduce the turbulence caused by change and enable firms to transform themselves into e-business, change must be supported by a critical mass of stakeholders, including employees, patterns and especially, customers [2]. From the perspective of niche marketing, all customers are not equal (they have different lifetime value or purchase behaviors). Therefore, Managers should carefully analysis customer behavior to better discriminate and more effectively allocate resources to the most profitable group of customers through the cycle of customer identification, customer attraction, customer retention, and customer development. However, instead of targeting all customers equally or providing the same incentive offers to all customers, enterprises can select only those customers who meet certain profitability criteria based on their individual needs or purchasing behaviors [3]. In this regard, Customer relationship management (CRM) is an important business approach to manage the customer's relationship (Marketing, Sales, Services, and Support). The Concept of customer lifetime value (CLV) or customer loyalty in CRM is the present value of all future profits generated from a customer and it is important for helping decision-makers target markets more clearly in fiercely competitive environments[4]. Several studies have done to calculate of CLV and use it [4-6]. Generally, Recency, Frequency, and Monetary (RFM) analysis have been used to measure the CLV [7-9].

This study uses sales transaction data of a textile manufacturing as the basis for work of knowledge discovery in database (KDD). It applies group decision-making to regard environmental effects on model by weighting RFM variables and data mining to segment customers. RFM weighting is performed using the analytical network process (ANP), which



allows measurement of dependency among RFM variables. At the same time, the AHP method is used in order to determine the RFM weights of the dependency or independency and their effects on customer analysis. A comparative presentation of the results follows. Self organization map (SOM) was then employed to group customers based on their weighted RFM value.

The remainder of this paper is organized as follows. Section 2 deals with the previous studies on customer analysis. The underlying methodology of the proposed approach, the hybrid method of FANP and SOM, is briefly introduced in Section 3. The proposed approach is explained and illustrated with a case study in Section 4. The paper ends with conclusions in Section 5.

## **2. Background**

This section will survey past research concerning customer relationship management (CRM), SOM methodology, RFM model, and Fuzzy logic.

### **2.1. Customer Relationship Management (CRM)**

CRM is defined as the managing of customer relationships on an organizational level through understanding, anticipating and managing of customer needs, based on knowledge gained of the customer, to increase organizational effectiveness and efficiency and thereby increasing profitability. Using the CRM strategies and tactics now serve as one of the major driving forces behind many companies' efforts to create superior value for their customers and generate a long-term revenue stream for themselves [10].

Growing of information technology (IT) in business, collection and storage of data about customers has become easier and less expensive, so databases in modern enterprises are now often massive. These massive databases often contain a wealth of important data that traditional methods of analysis fail to transform into relevant knowledge. Specifically, meaningful knowledge is often hidden and unexpected, and hypothesis driven methods, such as on-line analytical processing (OLAP) and most statistical methods, will generally fail to uncover such knowledge. Data mining tools could help organizations for extracting previously unknown and potentially useful knowledge and patterns from customer data within CRM framework [11].

### **2.2. Self Organization Map (SOM) Methodology**

[4] Liu, H., Yu, L., "Toward integrating feature selection algorithms for classification and clustering", *IEEE Transactions on knowledge and data engineering*, Vol. pp. 491-502, 2005.

Within the context of CRM, data mining can be seen as a business driven process aimed at the discovery and consistent use of profitable knowledge from organizational data. Data mining could help business in CRM as: (1) improve business efficiency in the least budget. (2) Utilize database marketing to maintain customer relationship. (3) Increase customer loyalty and customer value contribution, decrease customer loss rate. (4) Learn customer need to develop strategy. (5) Evaluate the effectiveness of advertisement and promotion. (6) Control competitive advantages and improve brand orientation. (7) Respond to the expectation of customer and strengthen service quality [12]. The generative aspect of data mining consists of the building of a model from data [13]. There are various data modeling to extract and identify useful information and knowledge from large customer databases[9, 14-16]: Association, Classification, Clustering, Forecasting, Regression, Sequence discovery, and visualization. Choice of data mining models should be based on the data characteristics and business requirements [17]. The most common learning model in data mining is



clustering. It segments a heterogeneous population into a number of more homogenous clusters to filter, classify, and extract patterns from database records. There are numerous machine learning techniques available for classification model. Self Organization map (SOM) is one of the well-known algorithms for clustering.

Self-organizing map (SOM) are unsupervised networks able to learn both the distribution (as competitive layers do) and the topology of the input vectors on which they are trained. Consequently, excellent clustering results are obtained. In addition, an easy evaluation of the result is possible through the graphical representation on map whose different labels (customers or vectors identifiers) can be grouped by visual inspection. Applying some index functions, it is possible to obtain an optimum clustering, but some “supervision” is necessary to filter the results of the maps (i.e., the operator selects the maximum number of clusters)[18]. In this study, SOM methodology is applied to cluster customers based on weighted RFM variables.

### 2.3. RFM Model

Customer retention rate or customer loyalty has important role to improve customer relations with organization in the area of sales, management, and customer services. According to Feinberg and Kadam, profits increase by 25-80% when customer retention rates increase by five points [19]. Elements of customer retention include one-to-one marketing, loyalty programs and complaints management [17]. The concept called Customer Lifetime Value (CLV) is used to measure the customer loyalty in CRM. CLV is the present value of all future profits generated from a customer [16] and help decision makers to target markets more clearly. Several authors have proposed different models to calculate CLV and applying it [20-22]. Generally, CLV is evaluated by RFM technique for each customer or cluster. This study use RFM terms as follows [23]:

- Recency (R): period since the last purchase.
- Frequency (F): the total number of purchases during a specific period.
- Monetary (M): Monetary value spent during one specific period.

One common approach to RFM analysis is what is known as hard [24]. Hard coding RFM is a matter of assigning a weight to each of the variables Recency, Frequency, and Monetary value, then calculating CLV by equation (1) for each customer or cluster in the database

$$C_i^j = w_R C_R^j + w_F C_F^j + w_M C_M^j \quad (1)$$

Where  $w_R$ ,  $w_F$  and  $w_M$  the relative importance of the RFM variables [8]. Assigning weight to RFM variables has had lots application. Stone [25] suggested that different weights should be assigned to RFM variables depending on the characteristics of the industry. His proposed model is efficient for particular databases without employing a systematic approach. , Liu and Shih[8] proposed a weighted RFM-based method (WRFM-based method) that integrates AHP and data mining to recommend products based on customer lifetime value. Although the AHP technique removes the deficiencies inherent in the measurement and evaluation steps of RFM analysis, it does not measure the possible dependencies among factors. The AHP method assumes that the variables presented in the hierarchical structure are independent; however, this is not always a reasonable presumption. This is particularly true for customers that their needs to production change continuously.

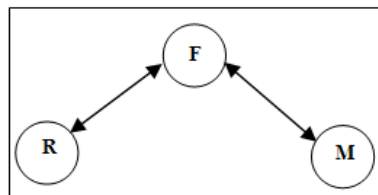
A customer doesn't buy all of yearly needs at one purchase during a year. Specially, when needs be as decayable commodities or stuffs that time decrease their quality. Therefore, the higher Frequency value decrease the Recency value and this corresponds to a higher probability of the customer's making a repeat purchase. A similar relationship exists between



Monetary and Frequency. Customers don't usually spend high amount money in few numbers of purchases. Customers with more purchase power have more purchase number, i.e., the higher Monetary value increase the Frequency value (Figure 1).

As can be seen, the RFM variables are not independent of each other, and moreover, there may even be a relationship among some variables. Since the variables weights are traditionally computed by assuming that the variables are independent, it is possible that the weights computed by including the dependent relations could be different. Possible changes in the variables weights can change the loyalty of customers, and these changes, in turn, will affect the CRM strategies and tactics. Therefore, it is necessary to employ analyses which measure and take the possible dependencies among variables into account in RFM analysis

In this study, RFM analysis is performed using the analytical network process (ANP), which allows measurement of dependency among RFM variables. At the same time, the AHP method is used in order to determine the variable weights of the dependency or independency and their effects on the loyalty rate of customers. A comparative presentation of the results follows.



**Figure 1. Internal Dependency among RFM Variables**

## 2.4. Fuzzy Logic

In most cases, many decision problems are too complex to be understood with certainty and all the necessary information are rarely available, but people can manage to come up with a solution or decision by using knowledge that is imprecise rather than precise. The key idea of fuzzy set theory is that an element has a degree of membership in a fuzzy set. Fuzzy set theory (FST) resembles human reasoning in its use of approximate information and uncertainty to generate decisions. FST is a mathematical theory introduced by Zadeh[26] in 1965 to model the uncertainty attributed to the vagueness and imprecision in real systems. This theory can be viewed as a generalization of the classical set theory to deal with classes of non-sharp boundaries. Thus, any methodology or theory implementing 'crisp' definitions such as the classical set theory, arithmetic and programming may be 'fuzzified' by generalizing the concept of a crisp set to the fuzzy set with blurred boundaries. The benefit of extending crisp theory or analytical methods to fuzzy techniques is in its strength in solving real-life problems, which inevitably entails some degree of uncertainty due to imprecision and fuzziness [27]. A fuzzy set is defined by a membership function. The membership function maps elements (crisp inputs) in the universe of discourse (interval that contains all the possible input values) to elements (degrees of membership) within a certain interval, which the most commonly used range for expressing degree of membership is the unit interval [0, 1]. If the value assigned is 0, the element does not belong to the set (it has no membership). If the value assigned is 1, the element belongs completely to the set (it has total membership). Finally, if the value lies within the interval [0, 1], the element has a certain degree of membership (it belongs partially to the fuzzy set). A fuzzy set, then, contains elements that have different degrees of membership in it. In this study, triangular fuzzy numbers,  $\tilde{1}$  to  $\tilde{9}$ , are used to represent subjective pair wise comparisons of selection process (equal to extremely



preferred) in order to capture the vagueness (Table). A triangular fuzzy number denoted as  $\tilde{M} = (l, m, u)$ , where  $l \leq m \leq u$ , has the following triangular type membership function:

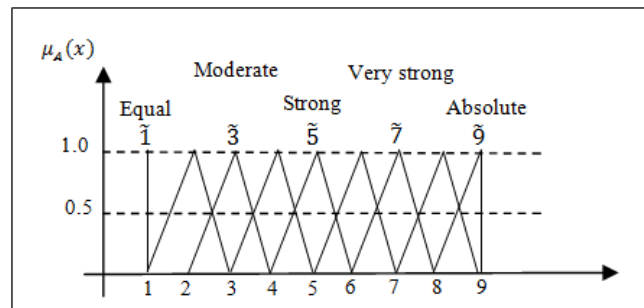
$$\mu_A(x) = \begin{cases} 0; & x \leq l \\ (x-l)/(m-l); & l \leq x \leq m \\ (x-u)/(m-u); & m \leq x \leq u \\ 0; & x \geq u \end{cases} \quad (2)$$

The triangular fuzzy numbers,  $\tilde{1}$  to  $\tilde{9}$ , are utilized to improve the conventional nine-point scaling scheme. In order to take the imprecision of human qualitative assessments into consideration, the five triangular fuzzy numbers  $\tilde{1}$ ,  $\tilde{3}$ ,  $\tilde{5}$ ,  $\tilde{7}$  and  $\tilde{9}$  are defined with the corresponding membership function. All attributes and alternatives are linguistically depicted in Figure 2. The shape and position of linguistically terms are chosen in order to illustrate the fuzzy extension of the method.

**Table 1. The Linguistic Scaled Corresponding Triangular Fuzzy Numbers**

Numeric rating	Linguistic scale <sup>a</sup>	Fuzzy scale
1	Just equal	$\tilde{1} = (1,1,1)$
3	Moderate dominance	$\tilde{3} = (2,3,4)$
5	Strong dominance	$\tilde{5} = (4,5,6)$
7	Very strong dominance	$\tilde{7} = (6,7,9)$
9	Absolute dominance	$\tilde{9} = (8,9,9)$

<sup>a</sup> For pair wise verbal comparisons, dominance of element i over element j may be interpreted as importance, preference, likelihood or influence



**Figure 2. Here's The Fuzzy Membership Function Scale**

### 3. Research Method

This study proposes a new procedure, joining quantitative value of RFM attributes and SOM methodology to extract meaning rules from records about customers to cluster



customers that their need to production change continuously, as is shown in

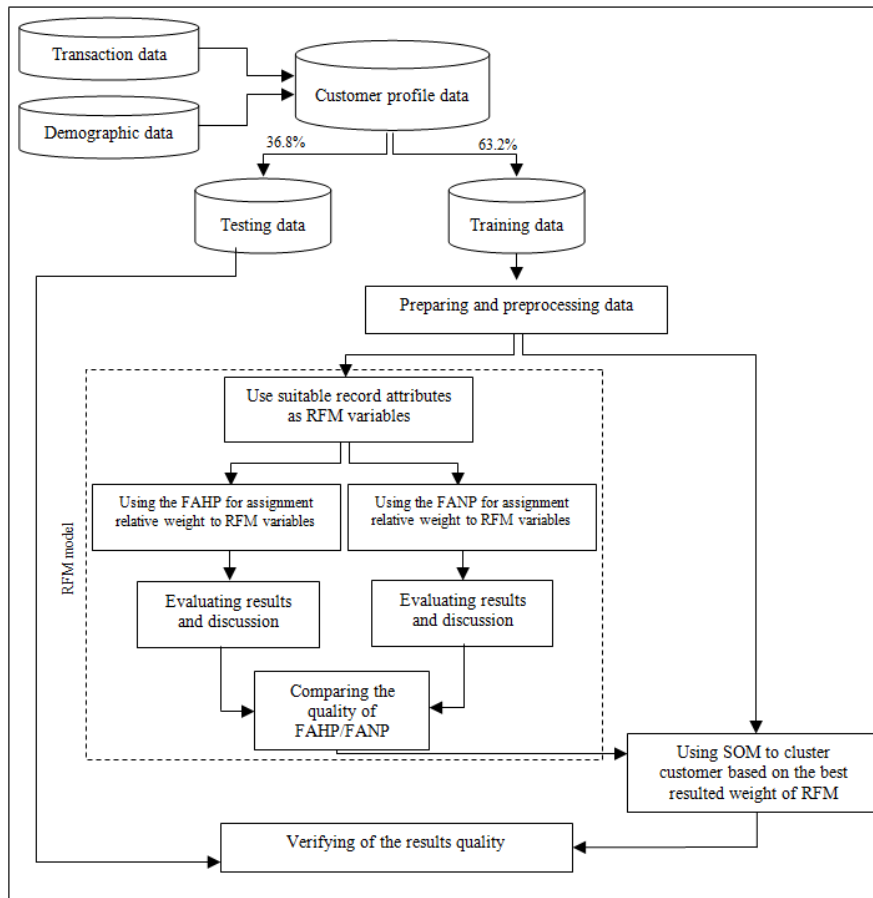


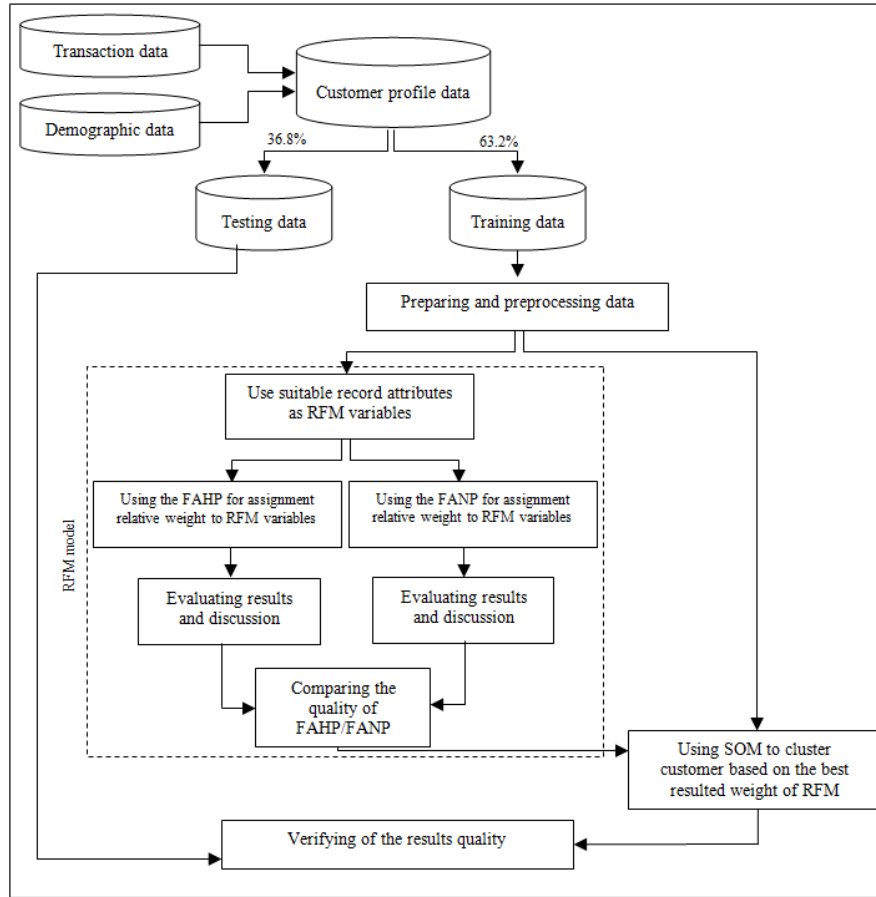
Fig. This section briefly introduces the research model of this study and the proposed procedure for classifying customer value.

The proposed procedure can be divided into four processes: (1) select the dataset and preprocess data: (2) transfer the data into RFM variables to yield quantitative value as input attributes for customers analysis by ANP and AHP techniques. Compare the results of two techniques and use proper RFM variables for next step (3) split dataset into training data and testing data, and then cluster customers based on their weighted RFM variables resulted from previous step by SOM methodology and (4) finally, evaluate the results of experiment and analyses the customers of any cluster. We further explain the proposed procedure for classifying customer value in follows:

*Step 1: select the dataset and data preprocessing:*

At first, select the dataset for empirical case study to discover hidden knowledge in it. In any knowledge discovering application the dataset to be mined may contain noisy or inconsistent data, some data may be missing and in almost all cases the database is large. Data preprocessing addresses each of those issues and includes such preliminary tasks as data cleaning, data integration, data transformation, and data reduction.





**Figure 3. Information Flow of Proposed Model**

*Step 2: transfer the data into RFM variables:*

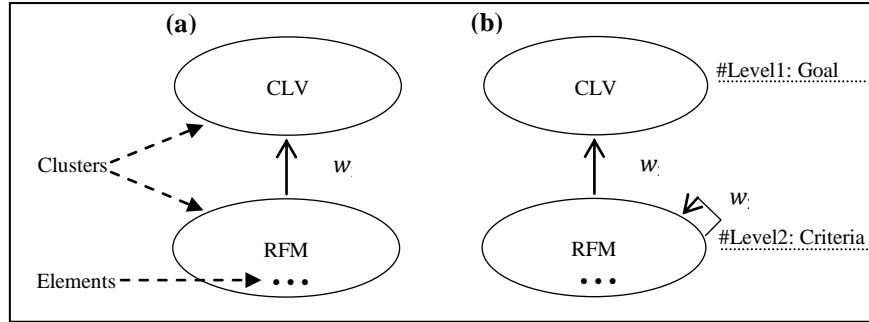
After select the dataset and data preprocessing phase, use suitable record attributes to RFM analysis. This study applies Fuzzy AHP (FAHP) and Fuzzy ANP (FANP) techniques to assign weight to each of the RFM variables.

Before we turn to the technical discussion of the proposed fuzzy ANP, it should be pointed out that the concept of ‘fuzziness’ in human judgment within the framework of ANP is independent from the traditional concept of ‘inconsistency’ in judgment. Note that it is conceivable for a DM to express highly inconsistent preferences with a very low level of ‘fuzziness’. In AHP/ ANP, inconsistency of judgments in pair wise comparisons is measured by the consistency ratio (CR) proposed by Saaty [28] as a test of the reliability of the decision outcomes. If the computed CR is more than 0.10, the DM is asked to reconsider and modify his judgment to improve the consistency according to his understanding. In this sense, allowing a modicum of inconsistency in pair wise comparison matrix can be seen as one of the attempts to incorporate ‘fuzziness’ indirectly in the decision model of AHP/ANP. Higher value of CR implies that inconsistency occurs because of some ‘errors in judgment’ on the part of the DM [29].

The detail process of this step is expressed into four sub-steps:



*Step 2-1: Model construction and problem structuring:* The problem should be stated clearly and be composed into a rational system, like a network. This network structure can be obtained by decision-makers through brainstorming or other appropriate methods. The hierarchical and network representation of the RFM model is shown in Fig.



**Figure 4. (a) The Hierarchical Representation of the RFM Model. (b) The Network Representation of the RFM Model**

*Step 2-2: Pairwise comparison matrices and priority vectors:* By using triangular fuzzy numbers, the decision maker(s) are asked to respond to a series of pair wise comparisons with respect to an upper level with respect to their importance towards their control criteria. In the case of interdependencies, components in the same level are viewed as controlling components for each other. Levels may also be interdependent. Triangular fuzzy numbers ( $\tilde{1}$ ,  $\tilde{3}$ ,  $\tilde{5}$ ,  $\tilde{7}$  and  $\tilde{9}$  that are shown in Table are used to indicate the relative strength of each pair of elements in the same hierarchy. Then, the fuzzy judgment matrix,  $\tilde{A} = (\tilde{a}_{ij})$ , via pair wise comparison is constructed as given below:

$$\tilde{A} = \begin{pmatrix} \tilde{a}_{11} & \tilde{a}_{12} & \dots & \tilde{a}_{1n} \\ \tilde{a}_{21} & \tilde{a}_{22} & \dots & \tilde{a}_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ \tilde{a}_{n1} & \tilde{a}_{n2} & \dots & \tilde{a}_{nn} \end{pmatrix} \quad (3)$$

Regard to any entity is a triangular fuzzy number then:

$$\tilde{A} = \begin{pmatrix} (a_{11}^l, a_{11}^m, a_{11}^u) & (a_{12}^l, a_{12}^m, a_{12}^u) & \dots & (a_{1n}^l, a_{1n}^m, a_{1n}^u) \\ (a_{21}^l, a_{21}^m, a_{21}^u) & (a_{22}^l, a_{22}^m, a_{22}^u) & \dots & (a_{2n}^l, a_{2n}^m, a_{2n}^u) \\ \vdots & \vdots & \ddots & \vdots \\ (a_{n1}^l, a_{n1}^m, a_{n1}^u) & (a_{n2}^l, a_{n2}^m, a_{n2}^u) & \dots & (a_{nn}^l, a_{nn}^m, a_{nn}^u) \end{pmatrix} \quad (4)$$

A reciprocal value is assigned to the inverse comparison, that is,  $\tilde{a}_{ij} = 1/\tilde{a}_{ji}$  where  $\tilde{a}_{ij}$  ( $\tilde{a}_{ji}$ ) denotes the importance of the  $i$ th ( $j$ th) element. Therefore:

$$\tilde{A} \approx \begin{pmatrix} (1,1,1) & (a_{12}^l, a_{12}^m, a_{12}^u) & \dots & (a_{1n}^l, a_{1n}^m, a_{1n}^u) \\ (1/a_{12}^u, 1/a_{12}^m, 1/a_{12}^l) & (1,1,1) & \dots & (a_{2n}^l, a_{2n}^m, a_{2n}^u) \\ \vdots & \vdots & \ddots & \vdots \\ (1/a_{1n}^u, 1/a_{1n}^m, 1/a_{1n}^l) & (1/a_{2n}^u, 1/a_{2n}^m, 1/a_{2n}^l) & \dots & (1,1,1) \end{pmatrix} \quad (5)$$

Like with AHP, pair wise comparison in Fuzzy ANP is performed in the framework of a matrix, and a local priority vector can be derived as an estimate of the relative importance associated with the elements (or clusters) being compared by solving the following equation:



$$A \times W = \lambda_{\max} \times W \quad (6)$$

Where A is the matrix of pair wise comparison, w is the eigenvector, and  $\lambda_{\max}$  is the largest eigenvalue of A.

*Step 2-3: Super matrix formation:* The super matrix concept is similar to the Markov chain process [30]. The super matrix was introduced to serve as a unifying framework for the study of priorities in hierarchy and in ‘systems with feedback’ [28]. To obtain global priorities in a system with interdependent influences, the local priority vectors are entered in the appropriate columns of a matrix. As an example, the super matrix representation for the hierarchy structure that is shown in Fig(a) is as:

$$\tilde{W}_h = \begin{pmatrix} 0 & 0 \\ \tilde{w}_{21} & I \end{pmatrix} \quad (7)$$

Where  $\tilde{w}_{21}$  is a fuzzy sub matrix which represents the impact of the RFM variables on the CLV, the importance in any these sub matrices present with a triangular number and I is the identity matrix that its entities are as triangular numbers.

In  $\tilde{W}_h$ , this assumption was considered that clusters and elements are in depended but when there is dependence among clusters or elements,  $\tilde{W}_h$  change. If the criteria are dependent among themselves, then the (2, 2) entry of  $\tilde{W}_h$  given by  $\tilde{w}_{22}$ . The interdependency is shown by the presence of the matrix element,  $\tilde{w}_{22}$  of the supermatrix of a RFM network with two levels is as follows:

$$\tilde{W}_n = \begin{pmatrix} 0 & 0 \\ \tilde{w}_{21} & \tilde{w}_{22} \end{pmatrix} \quad (8)$$

Each column of the super matrix  $\tilde{W}_n$  is weighted, and the result, known as the weighted supermatrix, is stochastic. Because  $\tilde{W}_n$  is a column stochastic matrix, it is known that the synthesis of all the interactions among the elements of this system is given by  $\tilde{W}_n^\infty$ .

$$\tilde{W}_n^\infty = \lim_{k \rightarrow \infty} W_n^k \quad (9)$$

Rising  $\tilde{W}_n$  to powers gives the long-term relative influences of the elements on each other. To achieve convergence of the importance weights, the weighted (stochastic) super matrix is raised to power. This matrix is called the limit super matrix and is as:

$$\tilde{W}_n^\infty = \begin{pmatrix} 0 & 0 \\ \tilde{Z} & \tilde{Y} \end{pmatrix} \quad (10)$$

Here,  $\tilde{Z}$  is the priority vector of weights of the alternatives. Hence, the vector  $\tilde{Z}$  can be used for evaluating and ordering RFM variables. A detailed discussion regarding the mathematical processes of the ANP is provided in [30-33].

*Step 2-4: Analyse the RFM variables:* The last step is ranking the resulted fuzzy. There are many different methods of defuzzification available. In this paper use the center of area method for defuzzification. This method is the most prevalent and physically most appealing of all the defuzzification methods, and information about the center of the area is presented under the fuzzy-membership function [34]. This is defined as follows:

$$x^{ca} = (\int \mu_A(z).zdz)/(\int \mu_A(z)dz) \quad (11)$$

According to the normalized results of Eq. (11), use RFM variables to cluster customers.

*Step 3: cluster customer value by SOM methodology:*



According to quantitative value of RFM variables for each customer, partition data (m object) into K clusters using the SOM methodology for clustering customer value. The analytical steps of SOM methodology are as follows[35]:

1. Determine dimension of the output map and its number of cells.
1. Initialize weights ( $w_{ij}$ ) to neurons.
2. While stopping condition is false, do
3. For each input vector x, do
4. For each j, compute:  $D(j) = \sum_i (w_{ij} - x_i)^2$
5. For index J such that D(j) is a minimum.
6. For all units j within a specified neighborhood of J, and for all i:  $w_{ij}^{new} = w_{ij}^{old} + \alpha(x_i - w_{ij}^{old})$
7. End
8. Update learning rate
9. Reduce radius of topological neighborhood at specified times.
10. End

*Step 4: evaluate the results:*

To avoid spurious results, and to assure that the resulting clusters are reflective of the general population, the clustering solution should be validated. One common validation method is to split the Customer profile data randomly into training and testing sets and the same settings is used for two sets. The validation of method is evaluated based on having a low error for the training set and a minimum difference between the training and testing set.

#### 4. Application of the Proposed Procedure

In this section, we apply proposed procedure for data of a case company, and then analyze its solutions. The applying proposed procedure on a case study can be expressed in detail as follows:

*Step 1: select the dataset and data preprocessing:*

The used case study is one of textile manufacturing business with over 30 years of trading history named by Albasco Co. The case company originally relied mainly on Iran markets. It began using of Information Technology 5 years ago and has collected the data of 3millions customers to personalize web pages and target email. Each customer in the database had a profile with numerous attributes such as payment preferences, products interests, purchase history, even birthday and anniversaries. To preprocess the dataset to make knowledge discovery easier is needed. Thus, we firstly delete the records which include missing values or inaccurate values, eliminate the redundant attributes and transform the datum into a format that will be more easily and effectively processed for clustering customer value.

*Step 2: transfer the data into RFM variables:*

After data preprocessing, the dataset remains 1 million instances which are characterized by the following seven fields: (i) ID, (ii) city, (iii) country, (iv) Recency, (v) Frequency, (vi)



Monetary, (vii) Credit amount. However, only the four attributes, ID, Recency, Frequency and Monetary are used to calculate customers life time cycle and cluster customers based on them.

*Step 2-1: Model construction and problem structuring:*

To convert the problem into a hierarchical structure, the top most elements are decomposed into dimensions and attribute-enablers. The decision model development requires identification of dimensions and attribute-enablers at each level and the definition of their interrelationships. The schematic structure established is shown in

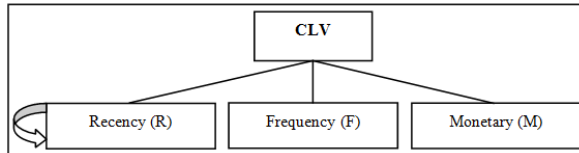
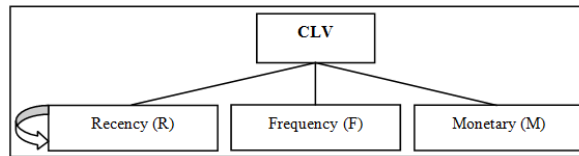


Fig. The aim of "CLV" is placed in the first level.



**Figure 5. ANP Model for RFM Analysis**

*Step 2-2: Pairwise comparison matrices and priority vectors:* In this study, select an expert team familiar with the operation of the textile industry to use their comment across process.

At first, consider that RFM variables are independency from each other and construct the pair wise comparison matrix of RFM variables. Any entity of this matrix shows importance of any variable on CLV by a fuzzy number as explained before (Table 1). Then, by using Eqs. (5) & (6), we calculate the weight of any factors (Table 2 & Table 3).

**Table 1. Pair Wise Comparison Matrix of RFM Variables without any Dependency among Factors**

	Recency			Frequency			Monetary			Weight		
	l	m	u	l	m	u	l	m	u	l	m	u
Recency	1	1	1	0.167	0.2	0.25	4	5	6	0.874	1	1.145
Frequency	4	5	6	1	1	1	0.125	0.143	0.167	0.794	0.894	1
Monetary	0.167	0.2	0.25	6	7	8	1	1	1	1	1.119	1.26

**Table 3. Weight of RFM Variables without any Dependency among Factor**

	Weight		
	l	m	u
Recency	0.874	1	1.145
Frequency	0.794	0.894	1
Monetary	1	1.119	1.26

On other hand, RFM variables aren't in depended usually, therefore, to regard the dependency among variables, determine the Inner dependence among the RFM variables by analyzing the impact of each variable on every other and construct any matrix by using pair wise comparisons. Using the analysis of both the internal and external environments of the



organization by experts, the dependencies among the RFM variables are determined (Figure 1). Based on the inner dependencies presented in Figure 1, pair wise comparison matrices are formed for the variables (Table 4).

**Table 2. Pair Wise Comparison Matrix of RFM Variables by considering "Monetary" as a Controlling Factor**

	Recency			Frequency			Weight		
	l	m	u	l	m	u	l	m	u
Recency	1	1	1	4	5	6	2	2.224	2.449
Frequency	0.167	0.2	0.25	1	1	1	0.408	0.447	0.5

After forming dependency matrices, we calculate the relative weight of any factors by using Eq. (6). The resulting is presented in the last column of Table 4. **Error! Reference source not found.** Then, using the computed relative importance weights, the inner dependence matrix of the RFM variables ( $\tilde{W}_{22}$ ) is formed (Table 5).

**Table 5. Inner Dependency among Variables Matrix ( $\tilde{W}_{22}$ )**

	Recency			Frequency			Monetary		
	l	m	u	l	m	u	l	m	u
Recency	1	1	1	2	2.236	2.449	0	0	0
Frequency	1	1	1	1	1	1	1	1	1
Monetary	0	0	0	0.408	0.447	0.5	1	1	1

*Step 2-3: Super matrix formation:* by using the obtained matrices ( $\tilde{W}_{21}$  and  $\tilde{W}_{22}$ ) and Eq. (8), form the super matrix. This matrix isn't normalized; therefore we should normalize it and calculate weight of any RFM variable by using the normalized supper matrix (Table 6).

**Table 6. Normalized Super Matrix**

	CLV			Recency			Frequency			Monetary		
	l	m	u	l	m	u	l	m	u	l	m	u
CLV	0	0	0	0	0	0	0	0	0	0	0	0
Recency	0.327	0.332	0.336	0.5	0.5	0.5	0.587	0.607	0.620	0	0	0
Frequency	0.297	0.296	0.294	0.5	0.5	0.5	0.293	0.271	0.253	0.5	0.5	0.5
Monetary	0.375	0.371	0.37	0	0	0	0.13	0.122	0.126	0.5	0.5	0.5

As said before, to calculate ultimate weight of any RFM variable, we need to power super matrix until it is steady. As norm of normalized matrix is leather than one, it satisfy in defined conditions and we can use (2, 1) entry of  $W_n^\infty$ . Therefore, weight of any RFM variable is calculated as Table 7:



**Table 7. Weight of RFM Variables**

	Fuzzy Analytical Hierarchy Process(FAHP)					Fuzzy Analytical Network Process(FANP)				
	Fuzzy weight			Crisp weight	Rank	Fuzzy weight			Crisp weight	Rank
	l	m	u			l	m	u		
Recency	0.873	1	1.447	1.00	2	0.453	0.460	0.463	0.459	1
Frequency	0.794	0.894	1	0.895	3	0.415	0.409	0.403	0.409	2
Monetary	1	1.119	1.26	1.126	1	0.131	0.130	0.133	0.132	3

*Step 2-4: Analyse the RFM variables:* To rank the RFM variables, use the ultimate weight obtained of previous step. These weights are as fuzzy numbers and we need to rank fuzzy numbers therefore we convert them to crisp number and rank respect to their crisp weights. As said before, the most popular defuzzification method is the center of area method that we use it in this paper. Therefore, resulted fuzzy numbers convert to a crisp number by using Eq.(11). The weight of RFM variables is listed in Table 7.

According to the FANP technique is shown in Table 7, the priority values are 0.459, 0.409 and 0.132 for "Recency", "Frequency" and "Monetary" variables, respectively. Therefore, the "Recency" variable is ranked the best, "Frequency" variable is the second and "Monetary" variable is the third. By assuming there is no dependence among the variables and using same pairwise comparison matrices to compute AHP priority values, the overall priorities computed for the RFM variables are difference. In the AHP analysis, the "Monetary" variable is found to be the most effective variable on CLV, with an overall priority value of 1.126. However, the priority ordering of the RFM variables is changed to "Monetary"- "Recency"- "Frequency". However, such a difference is expected because AHP does not take into account dependencies among variables while ANP does. For this reason, the ANP method is better able to model real world situations as compared to the AHP method. The superiority of ANP allows RFM analysis to yield more realistic results. Not only has the suggested model enabled us to satisfy the objective of our study but it has also demonstrated the functionality of the model.

Moreover, the management assessments of the firm on which the case study was conducted have said that they have found the results obtained from the suggested model to be meaningful and useful. They claim that results of FANP technique to weight RFM variables are indeed accepted as the “best priority”.

Another parameter that verifies the validity of the model is the Saaty’s CR of the pair wise comparison matrices. This is a necessary condition to satisfy the consistency in the fuzzy pair wise comparison matrix [29]. In this study, the computed CR values from the modal value of the fuzzy comparison matrices were within the tolerable range of 0.00–0.09.

*Step 3: cluster customer value by SOM methodology:*

At first, the RFM values of customers normalize by equations (12), (13), and (14).

$$NR_i = (R_{Max} - R_i)/(R_{Max} - R_{Min}) \quad (12)$$

$$NF_i = (F_i - F_{Min})/(F_{Max} - F_{Min}) \quad (13)$$

$$NM_i = (M_i - M_{Min})/(M_{Max} - M_{Min}) \quad (14)$$

Where,  $NR_i$ ,  $NF_i$  and  $NM_i$  are normalized Recency, normalized Frequency and normalized Monetary respectively.  $R_i$  ( $F_i$ ,  $M_i$ ) represented the original Recency (Frequency, Monetary) values of  $i^{th}$  customer, while  $R_{Max}$  ( $F_{Max}$ ,  $M_{Max}$ ) and  $R_{Min}$  ( $F_{Min}$ ,  $M_{Min}$ ) represented the largest and smallest Recency (Frequency, Monetary) value of all customers. Since Recency variable has negative impact to CLV, the shown cost form in equation (12) **Error! Reference source not found.** is used to normalize the Recency value.



After value normalizing, the normalized RFM values of each customer multiple by the weight of RFM variable,  $W_R$ ,  $W_F$  and  $W_M$ . As mentioned in previous step, FANP technique yields to more realistic results. Therefore, we use crisp RFM weights resulted of FANP technique as  $W_R$ ,  $W_F$  and  $W_M$ .

To analyse customers, cluster them by using SOM methodology. The input dataset consists of 1 million customers of the textile manufacturing. These data belong to 2008/2009/2010 years, and they correspond to customer behavior patterns based on RFM variables. Record's ID is used to label each customer in process. The dataset is split up into sub dataset: the 63.2% dataset (632000 records) is used as a training set, and the other 36.8% (368000) is used as a testing set[36].

The first stage of SOM methodology is Determining dimension of the output map and its number of cells. The dimension of the output map in this research is assumed to be two ( $q=2$ ), because most visible media (for example: paper, monitor panel and etc.) are 2-dimensional. By using the heuristic method in SOM toolbar of MATLAB[37], the output map is assumed a hexagonal network formed by a total of 6400 neurons ( $80 \times 80$ ) was used. This size has been chosen to allow a better visualization of the output data of the training map. A network with a greater number of cells would have hindered the visualization of the labels in each neuron. In the same way, a smaller map than the one used by the authors would cause many labels to be overlapped.

Finally, dataset run in Matlab 2008 environment in a single processor desktop computer with 2Core 1.6 GHz machine CPU and 1GB RAM under WINXP platform. Different training architecture configurations, training algorithms and initial weight of neurons result to different maps. Therefore, SOM is run ten times for each architecture configuration and the map with the most accurate is used to analyse customers. The solution quality is analyzed in terms of mean quantization error, which measures the resolution of the map. Quantization error is the average distance (weighted with the mask) from each data vector of cluster to its BMU that supplied with SOM toolbox. Table 8 shows attributes of 13 resulted clusters Based on the best map of the SOM. The placed customers in a cluster have similar lifetime values, in terms of weighted RFM.

In Table 8,  $AR_{c_i}$  refers to average Recency of cluster  $c_i$ ,  $AF_{c_i}$  refers to average Frequency of cluster  $c_i$ ,  $AM_{c_i}$  refers to average Monetary of cluster  $c_i$ ,  $CLV_{c_i}$  is customer life time value of cluster  $c_i$  According to equation (1), and  $Q_c$  is quantization error.

**Table. 3. The Cluster Results by SOM Model**

Cluster	$AR_{c_i}$	$AF_{c_i}$	$AM_{c_i}$	The number	$Q_c$ (Testing)	$Q_c$ (Training)	CLV	CLV Ranking
$C_1$	0.01	0.66	0.43	119117	1.28	2.034	0.33129	12
$C_2$	0.27	0.73	0.35	72068	1.04	1.847	0.4687	7
$C_3$	0.01	0.84	0.18	122124	0.94	1.265	0.37191	10
$C_4$	0.74	0.11	0.59	41039	1.13	1.983	0.46253	8
$C_5$	0.57	0.93	0.26	54050	1.25	2.414	0.67632	3
$C_6$	0.26	0.51	0.08	137147	0.092	1.258	0.33849	11
$C_7$	0.15	0.78	0.18	108082	0.071	1.019	0.41163	9
$C_8$	0.79	0.43	0.06	75108	0.13	0.511	0.5464	5
$C_9$	0.71	0.96	0.97	9012	0.142	0.483	0.84657	1
$C_{10}$	0.81	0.99	0.08	18011	0.094	0.334	0.78726	2
$C_{11}$	0.85	0.27	0.45	29022	0.126	0.787	0.55998	4
$C_{12}$	0.09	0.13	0.9	152162	0.134	0.245	0.21328	13
$C_{13}$	0.6	0.39	0.37	63058	0.095	1.262	0.48375	6



*Step 4: evaluate the results:*

The lower values of the  $Q_c$  index (for testing and training data) in In Table 8,  $AR_{c_i}$  refers to average Recency of cluster  $c_i$ ,  $AF_{c_i}$  refers to average Frequency of cluster  $c_i$ ,  $AM_{c_i}$  refers to average Monetary of cluster  $c_i$ ,  $CLV_{c_i}$  is customer life time value of cluster  $c_i$  According to equitation (1), and  $Q_c$  is quantization error.

**Table. 3** demonstrate the efficiency of the proposed method to identification of new customers and validate the resulted map. Moreover, SOM results to same  $Q_c$  index for two sets and 13 clusters, that it can show robustness of model.

The ranking CLV for Albasco customers is 0.213, 0.331, 0.338, 0.676, 0.787 and 0.846 in 12, 1, 6, 5, 10 and 9 classes on output, respectively. By this ranking it is obtained that the less customers have high the CLV rate (about 8.1% of all customers have the CLV more than 0.65). They are golden customers for firm. Therefore, customer retention strategies should perform for these customers. As such, one-to-one marketing, loyalty programs and complaints management can aim at maintaining a long term relationship with them. Many of customers have the low CLV rate (about 40% of all customers have the CLV less than 0.35). These classes may include new customers or customers who are being lost to the competition. Customer identification and customer attraction is better for these customers. Such as target customers' analysis and direct marketing. The rest of customers (about 51% of all customers), have the medium CLV. The customer development strategies are suitable for them. Such as lifetime value analysis, up/cross selling and market basket analysis.

## 5. Conclusion and Discussion

The Concept of customer lifetime value (CLV) or customer loyalty in CRM is important to help decision-makers target markets more clearly in fiercely competitive environments. A popular method to measure the CLV is RFM analysis that it assigns quantitative weighting to RFM variables. Although some studies do perform such quantitative weighting, these studies fail to consider the relations or dependencies of the variables of the RFM analysis. It is generally not possible to assume the RFM variables to be independent and unrelated with one another. This is particularly true in decayable commodities or stuffs that time decrease their quality.

This study performs a RFM analysis, with a case study example (Albasco Co.) in Iran's textile industry, wherein the possible dependencies among RFM variables are included. The FANP technique, which allows measurement of dependency among RFM variables and modeling of vagueness and imprecision attributes, is utilized in this work. The FAHP technique is also used with RFM analysis to compare the effects of the dependency among the RFM variables on prioritizing and weighting them. The weights of the variables of the RFM analysis differ according to the method used in the analysis (FAHP or FANP), due to the dependency among the RFM variables. With the findings in this empirical case study, we positively conclude that the FANP technique is more efficient than the FAHP technique. Therefore, our work involved the introduction a novel methodology which joins FANP and SOM to cluster customers. Based on results of our methodology, this study believes to aid Albasco Co easier interpreting and more precise focusing the target customers. It can be resulted to gain maximize profits with win-win situation for Albasco Co.

Since the RFM weights vary with the characteristics of product and industry, Future research may seek to apply proposed methodology in other industries.



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