## **Fast Algorithm for Mining Generalized Association Rules**

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#### Abstract

In this paper, we present a new algorithm for mining generalized association rules. We develop the algorithm which scans database one time only and use Tidset to compute the support of generalized itemset faster. A tree structure called GIT-tree, an extension of IT-tree, is developed to store database for mining frequent itemsets from hierarchical database. Our algorithm is often faster than MMS\_Cumulate, an algorithm mining frequent itemsets in hierarchical database with multiple minimum supports, in experimental databases.

Keywords: generalized association rules, GIT-tree, hierarchical database, multiple minimum supports.

#### 1. Introduction

Mining association rules plays an important role in knowledge discovery and data mining (KDD) [1, 9]. Its purpose is mining the hidden knowledge in databases.

Mining association rules in hierarchical database has been proposed in [2, 3, 5, 8, 10, 11]. In [8], the "Mining Generalized Association Rules" problem is mining association rules among items in hierarchical tree that satisfy minSup and minConf. However, this study does not change the support in different hierarchical levels. The paper [3] proposed the uniform minimum support in each level, items in the same level get the same minimum support. The purpose is mining association rules among itemsets in the same level. Another association rule mining method with multiple minimum supports was proposed in [10]. This allows users identify the different minimum supports for different items, so we can mine both frequent and rare rules. However, this method does not traverse the whole hierarchism so that it is very difficult to find association rules among items in different levels.

The research in [3] also considered in mining association rules among items in different levels. However, the limitations of this method are still based on Apriori method and used a uniform minimum support for each level.

Paper [5] introduced MMS\_Stratify and MMS\_Cumulate algorithms for mining frequent itemsets from hierarchical database with multiple minimum supports and proposed the computing of the minimum support of items based on the lift measure. This makes us no need to identify the minimum supports of items.

The main contributions of paper are as follows:

We develop GIT-tree data structure, an extension of IT-tree [6].

We propose an algorithm for mining frequent itemsets in hierarchical databases based on GIT-tree: using formulas in [5], we develop an algorithm of mining frequent itemsets based on GIT-tree for reducing run-time.

Section 2 presents concepts and definitions. Section 3 proposes GIT-tree for mining frequent itemsets in hierarchical database. We present our algorithm in section 4. Experimental results are presented in section 5.

### 2. Concepts

Let  $I = \{i_1, i_2, ..., i_m\}$  be set of items,  $D = \{t_1, t_2, ..., t_n\}$  be set of transactions, each transaction  $t_i = \langle tid, X \rangle$  determines a unique tid and an itemset X ( $X \subseteq I$ ). Suppose that hierarchical database is a graph in  $I \cup J$ , where  $J = \{j_1, j_2, ..., j_p\}$  represents for a general set of items that derives from I. An arc in graph G is an is-a relation, means that if an arc starts from I to I, then I is parent of I.

Figure 1 illustrates hierarchical database which are built for  $I = \{Laser\ printer,\ Ink-jet\ printer,\ Dot\ matrix\ printer,\ Desktop\ PC,\ Notebook,\ Scanner\}\ and\ J = \{Non-impact\ printer,\ Printer,\ PC\}.$ 

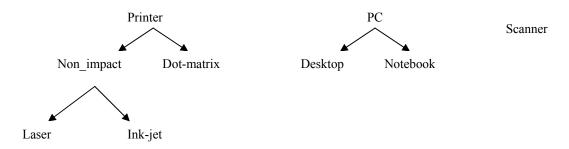


Figure 1. Example of hierarchical tree [5]

- **2.1. Definition 1**: Given transaction  $t = \langle tid, X \rangle$ , itemset Y belongs to t if every items of Y belong to X, or parent node of an item belongs to X. An itemset X has the support s, called  $\sup(X)$ , in D if s% of transactions in D contains X.
- **2.2.** Definition 2: Given set of transactions D and a hierarchical tree G, a general association rule is the form:

$$X \rightarrow Y - X$$

where  $X, Y \subset I \cup J, \emptyset \neq X \subset Y$ , there is no item in Y which is the parent node of any item in X. The support of rule is  $\sup(Y)$ . The confidence of rule,  $\operatorname{conf}(X \to Y - X) = \sup(Y)/\sup(X)$ .

**2.3.** Definition 3: Let ms(x) be the minimum support of an item  $x \in I \cup J$ . An itemset  $X = \{x_1, x_2, ..., x_k\}$ , where  $x_i \in I \cup J$  and  $1 \le i \le k$ , is frequent if the support of X is greater or equal the smallest value of items in X.

$$\sup (X) \ge \min_{x_i \in X} ms(x_i) \tag{1}$$

**2.4. Definition 4**: An association rule  $X \to Y - X$  is strong if its frequent satisfies  $\sup (X \to Y - X) \ge \min_{y_i \in Y} ms(y_i)$  and  $conf(X \to Y - X) \ge minConf$ .

The greatest difficulty of general association rule mining is the identification of minimum support for each item. To solve this problem, the paper [2] proposed a formula to compute the minimum support:

$$ms(x) = \begin{cases} \alpha \times \sup(x) & \text{if } \alpha \times \sup(x) > \min Sup\\ \min Sup & \text{if } else \end{cases}$$
 (2)

The parameter  $\alpha$  ( $0 \le \alpha \le 1$ ) is used to adjust the minimum support of single item x, which relates to its reality frequent in databases. If  $\alpha = 0$ , it becomes the homogeneous form. As the formula, user still identifies the minSup and parameter  $\alpha$ .

The formula above make user difficult in identifying the parameter  $\alpha$ . Thus, authors in [5] proposed the formula to identify the minimum support:

$$ms(x_i) = \begin{cases} \sup(x_i) \times \max\{\min Conf, \sup(x_{i+1})\} & \text{if } 1 \le i \le n-1 \\ \sup(x_i) & \text{if } i = n \end{cases}$$
(3)

Example: consider the database

Table 1. Transaction database [5]

Table 1: Transaction database [5]		
tid	Items	
1	Notebook, Laser printer	
2	Scanner, Dot-matrix printer	
3	Dot-matrix printer, Ink-jet printer	
4	Notebook, Dot-matrix printer, Laser	
	printer	
5	Scanner	
6	Desktop Computer	

From Table 1, and equation 3, we have the result:

Table 2. Items are sorted according to supports and minConf = 50%

Item	Support (%)	ms (%)
Desktop	16.7	8.3
Ink-jet	16.7	8.3
Laser	33.3	16.7
Notebook	33.3	16.7
Scanner	33.3	16.7
Dot-matrix	50.0	25.0
Non-impact	50.0	25.0
PC	50.0	33.3
Printer	66.7	66.7

## 2.5. Definition 5: The minimum support of an itemset:

$$ms(X) = \min_{x \in X} ms(x)$$
 (4)

Remark 1: From equation 4, we see that the order of items in  $X = \{x_1, x_2, ..., x_m\}$  is increasing follow ms, then  $ms(X) = ms(x_1)$ . Besides, if we have ms(X) and ms(Y), then  $ms(X \cup Y) = min\{ms(X), ms(Y)\}$ . Based on this remark, we need not use equation 4 (use the loop) to compute  $ms(X \cup Y)$ .

### 3. GIT-tree

Based on IT-tree [6], we add one more field ms(X) to identify minimum support of itemset X.

3.1. Vertex: Includes 3 fields

X: an itemset.

Tidset: the set of transaction contains X.

ms: The minimum support of X.

A vertex is denoted:  $X \times Tidset(X)$ .

**3.2.** Arc: Connecting the vertex at  $k^{th}$  level (called X) with the vertex at  $(k+1)^{th}$  (called Y) in which  $X \equiv_{\theta_k} Y$  ( $X \equiv_{\theta_k} Y$  if X and Y have the same k-prefix – see [6] for more details) and Y does not contain the item that is the parent of any item in X.

Consider the database in Table 1. We have results:

Table 3. Map items to IDs and ms of each item

ID	Item	Support(%)	ms(%)
A	Desktop	16.7	8.3
В	Ink-jet	16.7	8.3
С	Laser	33.3	16.7
D	Notebook	33.3	16.7
Е	Scanner	33.3	16.7
F	Dot-matrix	50.0	25.0
G	Non-impact	50.0	25.0
Н	PC	50.0	33.3
I	Printer	66.7	66.7

Table 4. Database in Table 1 after mapping

ti d	Items
u	_ ~
1	D, C
2	E, F
3	F, B
4	D, F, C
5	Е
6	A

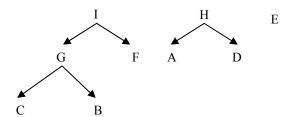


Figure 2. Hierarchical tree after mapping

Table 5. Database after add parent items

Tid	Items
1	D, C, H, G, I
2	E, F, I
3	F, B, I, G
4	D, F, C, H, I, G
5	Е
6	A, H

Table 6. Convert into vertical transaction database

item	Tids
A	6
В	3
C	1, 4
D	1, 4
Е	2, 5 2, 3, 4
F	2, 3, 4
G	1, 3, 4
Н	1, 4, 6
I	1, 2, 3, 4

With minConf = 50%, we have results in Table 7.

Table 7. The support with ms+ of items (where ms+ =  $\lceil ms*|D|/100 \rceil$ )

ID	Support	ms+
A	1	1
В	1	1
С	2	1
D	2	1
Е	2	1
F	3	2
G	3	2
Н	3	2
I	4	4

# 4. Algorithm for mining frequent itemsets in hierarchical database based on GIT-tree

In [5], authors proposed algorithms MMS\_Stratify and MMS\_Cumulate based on Apriori algorithm that lead to do many database scans, and the candidate number will be very large. In this section, we apply GIT-tree to mine frequent itemsets in hierarchical database to reduce the mining time.

## 4.1. Algorithm

```
Input: Hierarchical database D and minConf
Output: Generalized frequent itemsets in D
Create IMS /* minimum supports table*/
Create IA /* The item and its parent node in hierarchical tree G*/
SMS = Sort(IMS) /* sort IMS table in increasing order of ms(x) */
F = F-gen (SMS, D, IA)
L_{\rm r} = First level of GIT-tree contains nodes i \times Tidset(i) with i \in I \cup J
ENUMERATE GENERALIZED FIs(L_r)
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    for all node X \times Tidset(X) \in L_r do
         L_c = \emptyset
         for all Y \times Tidset(Y) \in L_r with Y after X do
           X' = X \cup Y
           if \forall x \in X', \neg \exists y \in X': parent(x)=y then
                T = Tidset(X) \cap Tidset(Y)
                 ms(X') = min(ms(X), ms(Y))
                 if |T| \ge ms(X') then
                   L_{c} = L_{c} \cup \left\{ \begin{matrix} X' \times T \\ ms(X') \end{matrix} \right\}
```

ENUMERATE GENERALIZED  $FIs(L_c)$ 

Algorithm 1. Mining frequent itemsets in hierarchical database using GIT-tree

First, we create the minimum support table of items based on equation 3, then create parent-child relation table in hierarchical tree G. Finally, algorithm sorts the IMS in increasing order of minimum support (aim to create set F that includes single items satisfying minimum support threshold of the smallest minimum support item).

Function ENUMERATE\_GENERALIZED\_FIs( $L_r$ ) creates GIT-tree to mine generalized frequent itemsets. It creates a new equivalence class  $L_c$  by considering every Y after X to form itemset X' and Tidset of X' (T). If items in X have not parent-child relation each other, we consider whether its support satisfies the minimum support or not (ms(X') is computed by remark 1). If it satisfies ms(X'), then we add this node to  $L_c$ .

#### 4.2. Illustration

Consider the database in Table 6, we have results as follows:

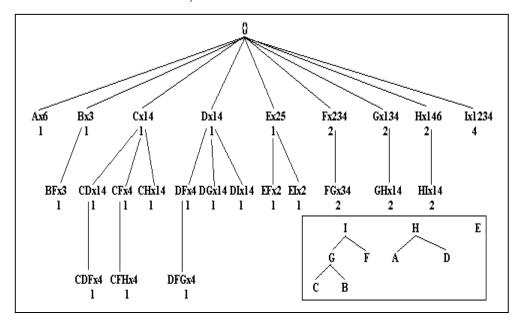


Figure 3. GIT-tree for mining generalized frequent itemsets

Each node in GIT-tree includes 3 elements: itemset, Tidset and ms. Example: DG belongs to transactions (tids) 1, 4 and ms(DG) = 1. When we combine nodes X, Y at higher level to be node at lower level, we compute the intersection between two tidsets and find  $min\{ms(X), ms(Y)\}$ .

Example:

Consider the combination between D and G to be DG, we compute  $Tidset(DG) = Tidset(D) \cap Tidset(G) = 14$ , and then compute  $ms(DG) = min\{ms(D), ms(G)\} = min\{1, 2\} = 1$ . Because  $|Tidset(DG)| \ge ms(DG)$  so we add DG to next level.

Note: Although GI has support is 3 (Tidset(GI) = Tidset(G)  $\cap$  Tidset(I) = 134  $\cap$  1234 = 134)  $\geq$  ms(GI) = min(ms(G), ms(I)) = 2, but I is a generalized item of G, GI does not combine together.

## 4.3. Diffset for fast computing the support

In [7], authors used Diffset for fast computing the support of itemset and saving memory that stores Tidset. We also use it for mining generalized frequent itemsets to reduce run-time and memory.

Table 8. Average size of Tidset and Diffset in database from UCI [7]

Database	MinSup (%)	Avg. of Diffset size	Avg. of Tidset size	Scale Tidset/Diffset
chess	0.5	26	1820	70
connect	90	143	62204	434.99
mushroom	5	60	622	10.37
pumsb_star	35	301	18977	63.04
pumsb	90	330	45036	136.47
T10I4D100K	0.1	31	230	7.42
T40I10D100K	0.5	96	755	7.86

## 5. Experimental results

Experimental results are performed in databases from Microsoft Foodmart2000 of Microsoft SQL2000. We call the algorithm based on GIT-tree is MMS\_GIT-Tree. Database Foodmart is results from sales\_fact\_1997 and synthetized database is gotten from sales\_fact\_1997, sales\_fact\_1998 and sales\_fact\_dec\_1998 in Foodmart2000. Hierarchical items include 3 levels: 1560 items in level 1 (products), 110 general items in level 2 (product subset) and 47 general items in top level (product types). Both of them have 5581 transactions.

For accurate purpose, we run 5 times with each minConf, and the result is averaged of 5 times.

Table 9. Comparing run-time in database Sales\_fact\_1997 with minConf thresholds

minConf	Time (s)		
(%)	MMS_Cumulate	MMS_GIT-Tree	
90	25.14	24.68	
85	25.38	24.82	
80	26.12	24.96	
75	27.86	25.05	
70	30.92	25.21	
65	39.25	25.39	
60	57.69	26.85	
55	104.85	27.09	
50	257.36	27.36	

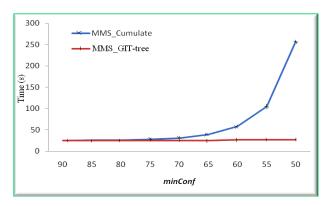


Figure 4. Comparing the run-time between MMS\_Cumulate and MMS\_GIT-Tree in Sales\_fact\_1997

Table 10. Comparing the run-time in database sales\_fact\_synthetized

minConf	Time (s)		
(%)	MMS_Cumulate	MMS_GIT-Tree	
90	104.36	101.88	
85	115.83	102.29	
80	156.22	103.02	
75	252.91	103.34	
70	580.10	108.21	

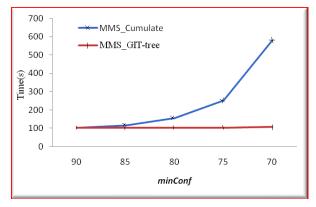


Figure 5. Comparing run-time between MMS\_Cumulate and MMS\_GIT-Tree in Sales\_fact\_synthetized

From Figures 4 and 5, we see that the run-time based on GIT-tree is more effective than that of MMS\_Cumulate, especially when minConf is low. It happens because the smaller the minConf is, the larger the number of candidates MMS\_Cumulate are. This costs a lot of time to mine candidates and compute the support of candidates. In contrast, GIT-tree based on the intersection of Tidset to compute the support of itemsets fast, so the mining time is faster.

#### 6. Conclusion and future works

Identifying the minimum support (minSup) for mining association rules in database and hierarchical database has many difficulties. Thus, authors in [5] proposed the method to direct compute the minimum support of items based on their support. However, the Apriori-based algorithm consumed a lot of time. This paper introduces an efficient algorithm to mine frequent itemsets in hierarchical database with multiple minimum supports that based on GIT-tree. Experimental results show the effect of proposed algorithm.

In future, we will develop the efficient algorithm for fast mining generalized association rules which are generated among generalized frequent itemsets. Besides, the evaluation of rules through measures is considered to find the best rules for users. Next, efficient algorithm for mining frequent closed itemsets from hierarchical database will be discussed.

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