

## Research on Kinematics Simulation of PUMA560 Robot

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### **Abstract**

*This paper is on the basis of the kinematics model and the structure parameters of PUMA560 industrial robot, under the environment of ADAMS, establishing the virtual physical model of PUMA560 industrial robot. And when the robot fixture has been attached a load which the quality is  $m$ , then moving from one point to another point, using interpolation method and linear motion of the fixture to simulate trajectory and position under the environment of ADAMS respectively.*

**Keywords:** PUMA560, ADAM, modeling, simulation

### **1. Introduction**

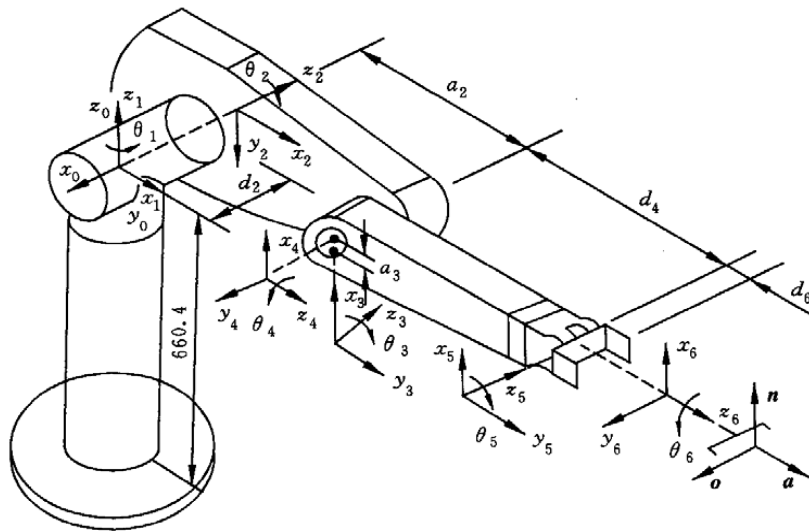
The robot is an important part of the industry, they can accurately perform a variety of tasks and operations, and they don't need the safety measures and comfortable working conditions when people working. For the development and design of the robot, engineering designers can build virtual prototype model on the PC, analyzing a variety of performances of virtual prototype model, improving the design continuously according to the requirement of the task, we use the virtual prototype model to test, instead of using the traditional physical prototype [1-2]. We could reduce the design process and the development process of mechanical products through the application of virtual prototype technology, reducing the product development time, reducing development costs, improving the quality of products greatly, to get the innovative and optimized product design[3-4].

In this paper, the application of ADAMS software is designed for virtual prototype of mechanical product development tools. ADAMS software provides a very large modeling and simulation environment for users, designers can make many kinds of mechanical system modeling simulation and analysis of the experiment, it is very powerful [5]. The main advantage of this software is that it can well reflect the characteristics of the actual physical model when using it to establish the virtual model, the simulation results are consistent with the results of actual physical model. Taking the PUMA560 robot as the research object in this paper, analyzing Kinematic of the mechanical system in ADAMS software to optimize the overall system [6-7].

### **2. Structure and Parameters of PUMA560 Robot**

PUMA560 belongs to the rotary multi joint robot, its six connecting rods are composed of six rotating joints connected together, the first three joints determine the position of the reference point of wrist, the other three joints determine the orientation of the wrist, like most of the industrial robot, the other three joint axes intersect at one point. This point can be used as the reference point of the wrist, it can also be used as origin of connecting rod coordinate system {4}, {5} and {6}. The axis of joint 1 is vertical direction, the axis of joint 2 and 3 are horizontal direction, and they are parallel, the distance is  $a_2$ , the axis of joint 1 and 2 are

vertical intersection, the axis of joint 3 and 4 are vertical staggered, the distance is  $a_3$ , the end actuator is fixed on the connecting rod 6, the foundation bed is fixed, each joint has a single degree of freedom, so PUMA560 is a robot with 6 degrees of freedom manipulator. It is shown in Figure 1.



**Figure 1. Curves of Sampling Current Changing**

The foundation bed of the coordinate system is denoted as  $\{0\}$ , the connecting rod of  $i$  coordinate system is denoted as  $\{i\}$ .  $a_{i-1}$  is the distance between  $z_{i-1}$  and  $z_i$  along  $x_{i-1}$  axis,  $\alpha_{i-1}$  is the angle moved from  $z_{i-1}$  to  $z_i$  along  $x_{i-1}$  axis,  $d_i$  is the distance between  $x_{i-1}$  and  $x_i$  along  $z_i$  axis,  $\theta_i$  is the angle moved from  $x_{i-1}$  to  $x_i$  along  $z_i$  axis. We can obtain from the structure, the robot is connected by a base and each joint arm. Each joint installs drive motor, driving each bar of the robot to move according to the trajectory under the function of control system, to realize the functions of assembly and transport of the end operator.

**Table 1. Connecting Rod Parameters Of PUMA560 Robot**

Connecting rod $i$	Variable $\theta_i$	$\alpha_{i-1}$	$a_{i-1}$	$d_i$	Variable range
1	$\theta_2 (90^\circ)$	$0^\circ$	0	0	$-160^\circ \sim 160^\circ$
2	$\theta_2 (0^\circ)$	$-90^\circ$	0	$d_2$	$-225^\circ \sim 45^\circ$
3	$\theta_3 (-90^\circ)$	$0^\circ$	$a_2$	0	$-45^\circ \sim 225^\circ$
4	$\theta_4 (0^\circ)$	$-90^\circ$	$a_3$	$d_4$	$-110^\circ \sim 170^\circ$
5	$\theta_5 (0^\circ)$	$90^\circ$	0	0	$-100^\circ \sim 100^\circ$
6	$\theta_6 (0^\circ)$	$-90^\circ$	0	0	$-266^\circ \sim 266^\circ$

Connecting rod parameters are shown in table 1,  $a_2 = 431.8mm$ ,  $a_3 = 20.32mm$ ,  $d_2 = 149.09mm$ ,  $d_4 = 433.07mm$ . In all parameters,  $\theta$  is variable,  $\alpha$ ,  $a$ ,  $d$  are constant.

### 3. PUMA560 Robot Kinematics

In order to solve each joint angle, we need to introduce homogeneous transformation between adjacent coordinates. For the convenience of writing, ordering  $S = \sin$ ,  $C = \cos$ ,  $T_i = {}^{i-1}T_i$ . The homogeneous transformation between two adjacent coordinates is:

$${}^{i-1}T_i = \begin{bmatrix} C\theta_i & -C\alpha_i S\theta_i & S\alpha_i S\theta_i & \alpha_i C\theta_i \\ S\theta_i & C\alpha_i C\theta_i & -S\alpha_i C\theta_i & \alpha_i S\theta_i \\ 0 & S\alpha_i & C\alpha_i & d_i \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad (1)$$

Multiply each matrix, we can get the general transformation matrix is:

$${}^0T_6 = {}^0T_1(\theta_1) {}^1T_2(\theta_2) {}^2T_3(\theta_3) {}^3T_4(\theta_4) {}^4T_5(\theta_5) {}^5T_6(\theta_6) = \begin{bmatrix} n_x & o_x & a_x & p_x \\ n_y & o_y & a_y & p_y \\ n_z & o_z & a_z & p_z \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad (2)$$

The total transformation matrix is the function of each joint variable  $\theta_1, \theta_2, \dots, \theta_6$ .

$$n_x = c_1 [c_{23}(c_4 c_5 c_6 - s_4 s_6) - s_{23} s_5 c_6] + s_1 (s_4 c_5 c_6 + c_4 s_6) \quad (3)$$

$$n_y = s_1 [c_{23}(c_4 c_5 c_6 - s_4 s_6) - s_{23} s_5 c_6] - c_1 (s_4 c_5 c_6 + c_4 s_6) \quad (4)$$

$$n_z = -s_{23}(c_4 c_5 c_6 - s_4 s_6) - c_{23} s_5 c_6 \quad (5)$$

$$o_x = c_1 [c_{23}(-c_4 c_5 s_6 - s_4 s_6) + s_{23} s_5 s_6] + s_1 (c_4 c_6 - s_4 c_5 s_6) \quad (6)$$

$$o_y = s_1 [c_{23}(-c_4 c_5 s_6 - s_4 s_6) + s_{23} s_5 s_6] - c_1 (c_4 c_6 - s_4 c_5 s_6) \quad (7)$$

$$o_z = -s_{23}(-c_4 c_5 c_6 - s_4 c_6) + c_{23} s_5 s_6 \quad (8)$$

$$a_x = -c_1 (c_{23} c_4 s_5 + s_{23} c_5) - c_1 s_4 s_5 \quad (9)$$

$$a_y = -s_1 (c_{23} c_4 s_5 + s_{23} c_5) + c_1 s_4 s_5 \quad (10)$$

$$a_z = s_{23} c_4 s_5 - c_{23} c_5 \quad (11)$$

$$p_x = c_1 [a_2 c_2 + a_3 c_{23} - d_4 s_{23}] - d_2 s_1 \quad (12)$$

$$p_y = s_1 [a_2 c_2 + a_3 c_{23} - d_4 s_{23}] + d_2 s_1 \quad (13)$$

$$p_z = -a_3 s_{23} - a_2 s_2 - d_4 c_{23} \quad (14)$$

In the above formulas,  $s_i = \sin \theta_i$ ,  $c_i = \cos \theta_i$ .

$$c_{23} = \cos(\theta_1 + \theta_2) = c_2 c_3 - s_2 s_3 \quad (15)$$

$$s_{23} = \sin(\theta_2 + \theta_3) = c_2 s_3 + s_2 c_3 \quad (16)$$

To check the accuracy of the result  ${}^0T_6$ , calculating the value of  ${}^0T_6$  when  $\theta_1 = 90^\circ$ ,  $\theta_2 = 0^\circ$ ,  $\theta_3 = -90^\circ$ ,  $\theta_4 = \theta_5 = \theta_6 = 0^\circ$ , the calculation result is:

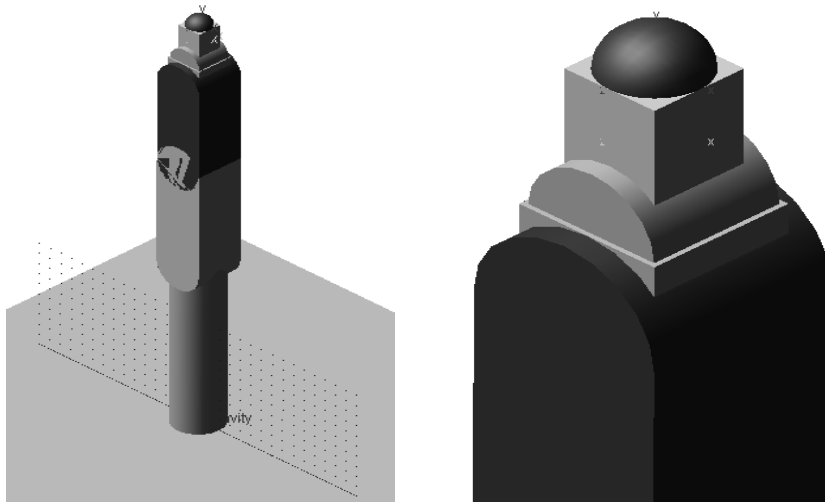
$${}^0T_6 = \begin{bmatrix} 0 & 1 & 0 & -d_2 \\ 0 & 0 & 1 & a_2 + d_4 \\ 1 & 0 & 0 & a_3 \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad (17)$$

It is consistent with the situation that shown in Figure 1.

#### 4. Creating PUMA560 Robot Kinematics Model

Modeling includes building geometric model, adding constraint mechanism and establishing driving function, and so on. Using ADAMS to modeling, we need to analyze and simplify according to the actual model.

Using geometric modeling tool library to establishing the three-dimensional model of PUMA560 robot under ADAMS/View environment, taking foundation, joint 4, joint 6 to create cube, taking joint 1 and joint 5 to create cylinder, taking joint 2 and joint 3 as connecting rod, taking clutch to create sphere and named as Gruz. To import the corresponding dimension values and coordinate points to the created geometric model according to the PUMA560 robot appearance parameters. And last, generating PUMA560 robot model as shown in Figure 2. It can be seen that we could create more complex model through Boolean operation function of ADANS.



**Figure 2. Final Generated PUMA560 Robot Model**

Assuming that the actual movement of the robot is gradually and step by step in this paper, ADAMS provides a step driver function, the expression is: STEP (x, BeginAt, Initial Function Value, EndAt, Final Function Value). And in this expression, x is independent variable, the value of the variable is the initial value Initial Function Value when x is less-than Begin At; dependent variable value is termination value Initial Function Value when x is more than End At; dependent variable value is smooth over according to certain rules when z is between initial value and termination value.

According to the data of PUMA560, quoting formula:

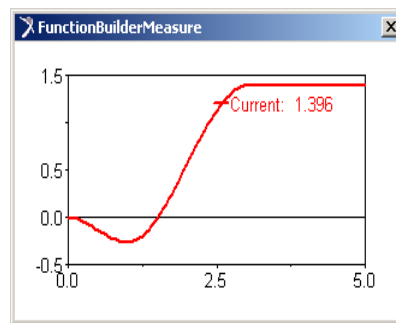
$$STEP(time, 0, 0, 1, \omega_H) * \pi / 180 + STEP(time, 1, 0, 3, \omega_H - \omega_K) * \pi / 180$$

Importing each joint driving function in "Function Builder" dialog box, each joint driving function form of robot are shown in Table 2.

**Table 2. Each Joint Driving Function List**

Joint name	Function
Joint 1	STEP( time , 0 , 0 , 1 , -15)*pi/180+STEP( time , 1 , 0 , 3 , -95)*pi/180
Joint 2	STEP( time , 0 , 0 , 1 , 75)*pi/180+STEP( time , 1 , 0 , 3 , 65)*pi/180
Joint 3	STEP( time , 0 , 0 , 1 , 30)*pi/180+STEP( time , 1 , 0 , 3 , -130)*pi/180
Joint 4	STEP( time , 0 , 0 , 1 , 25)*pi/180+STEP( time , 1 , 0 , 3 , 115)*pi/180
Joint 5	STEP( time , 0 , 0 , 1 , -80)*pi/180+STEP( time , 1 , 0 , 3 , -95)*pi/180
Joint 6	STEP( time , 0 , 0 , 1 , 15)*pi/180+STEP( time , 1 , 0 , 3 , 75)*pi/180







Chronologically, taking the horizontal axis as the time axis to establish joint angle curve of joint 1 through Step function, the curve is shown in Figure 3.



**Figure 3. Changing Curve of Joint Angle**

## 5. Kinematic Simulation of PUMA560 Robot

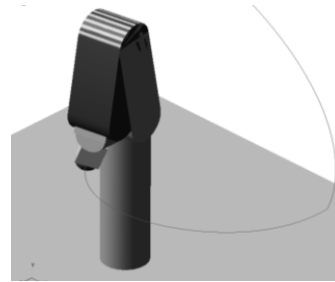
We adopt interactive simulation control according to the requirements of PUMA560 robot.

Clicking the simulation button in the main toolbar , pop-up interactive simulation control dialog:  is run simulation calculation,  is termination simulation calculation,  is return to the starting position,  is play a recent animation of simulation,  is verification model. Selecting the required article Kinematic, selecting Steps, to set the number of simulation steps to 100, selecting Step Size, to set the simulation time to 3s, so the initial state of robot simulation is shown in Figure 4, termination state is shown in Figure 5.



**Robot Simulation**

**Figure 4. The Initial State of PUMA56**

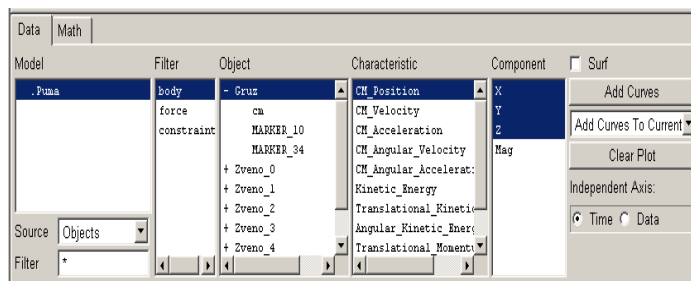


**Robot Simulation**

**Figure 5. The terminal state of PUMA560**

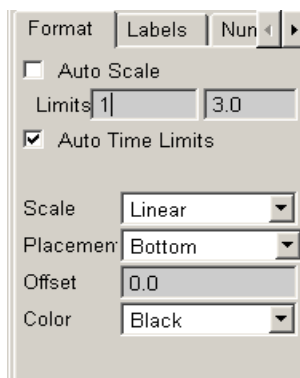
### 5.1. Interpolation Trajectory

Using PostProcess module of ADAMS, we could draw curve as shown in Figure 6, setting up Gruz.



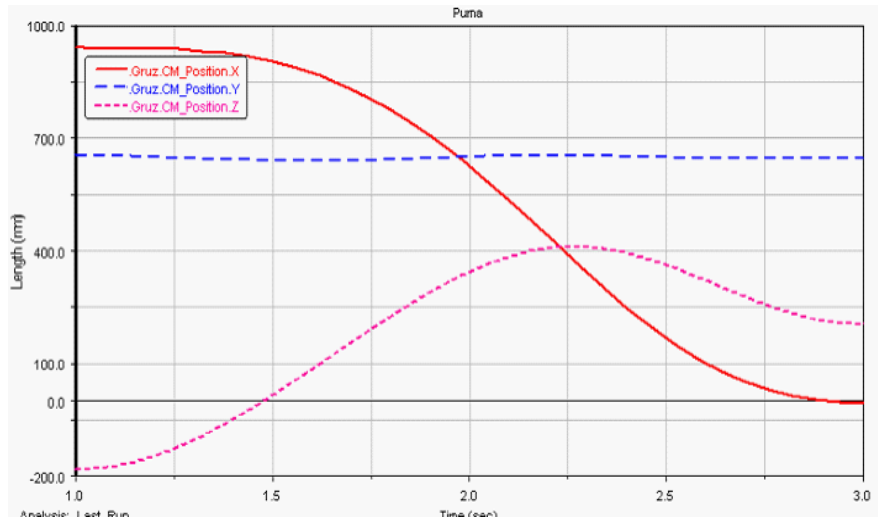
**Figure 6. Curve Data Source Selection Region**

At the post processing interface, selecting the Plotting item in the upper left corner of the processing type drop-down menu select box, it is the interface to process data curves. Editing dialog box as shown in Figure 7.



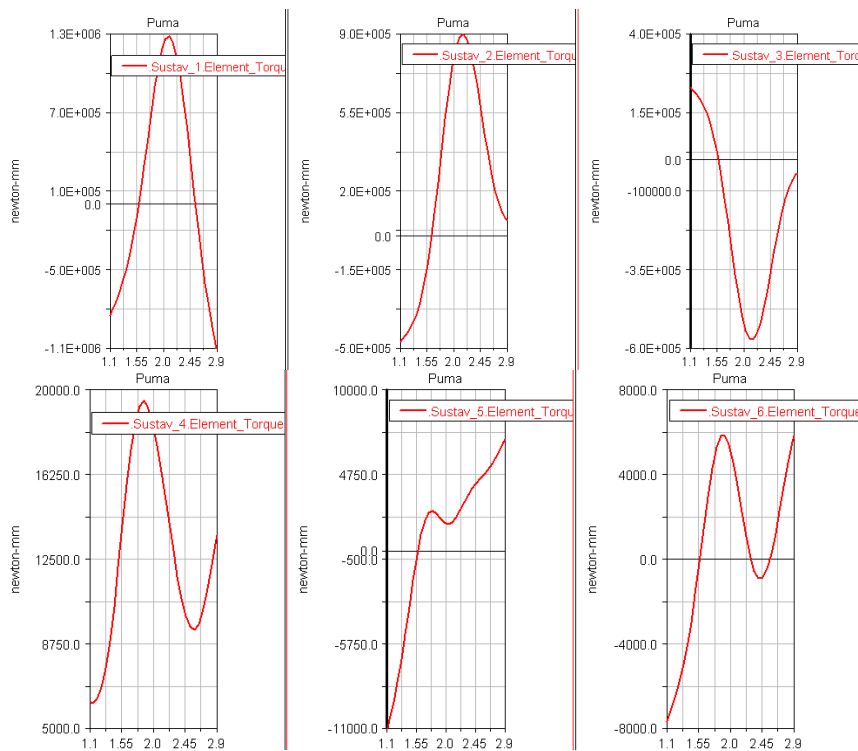
**Figure 7. Curve Attribute Edit Area**

We could obtain the diagram as shown in Figure 8.



**Figure 8. Gruz Diagram**


We could get X axis direction diagram of other joints according to above steps. They are shown in Figure 9.



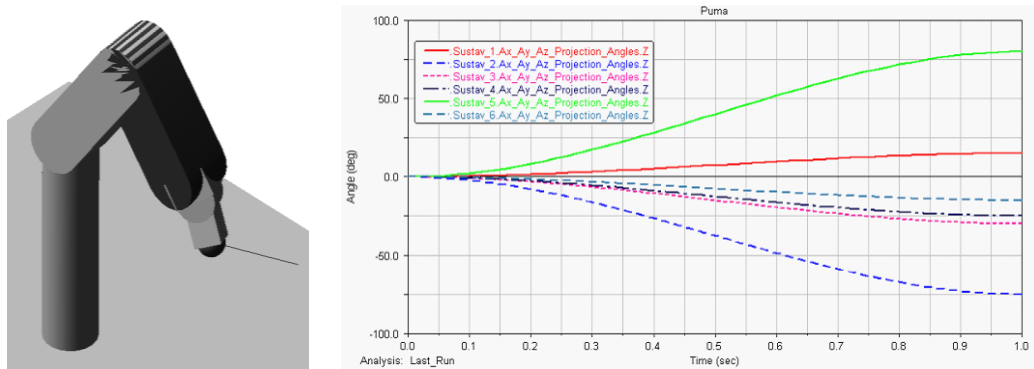
**Figure 9. Other Joint Junction Curves**

### 5.2. Straight-Line Trajectory

In order to get the track of the linear motion, firstly we set up all the joints that could be free to rotate, click the right mouse button, select Joint—Modify, open Modify joint, and select Impose motions in sub window, in Impose motions window, set up z axis as Free, other joints and so on.

Establishing the linear track of load, adopt General point motion() connecting the load with the grand, click the left mouse button, create motion oscillator, and select

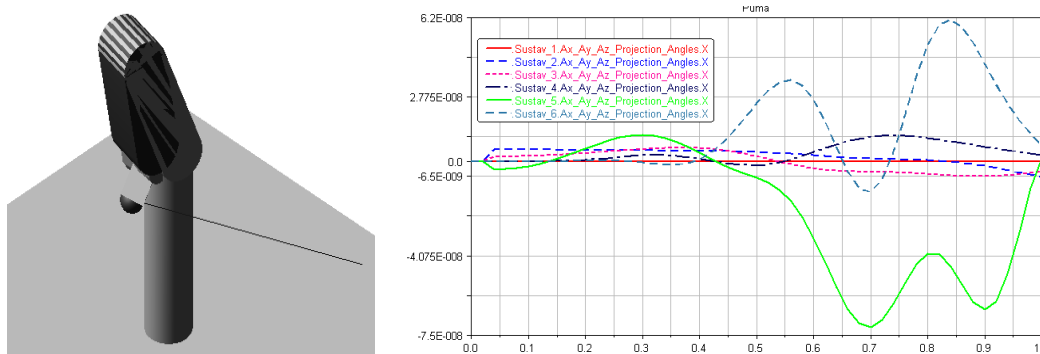
General motion—Modify in menu, we could obtain displacement and angular velocity diagrams of the load, it is shown in Figure 10.



**Figure 10. Displacement and Angular Velocity Diagrams of Each Component**

From Figure 10, we know that there is no linear movement way from start to finish to robot load.

We could also establish angular velocity of linear motion trajectory through another method, assuming  $R_y = 0$ , we could obtain the diagram in X axis direction, it is shown in Figure 11.



**Figure 11. Angular Velocity Diagram in X Axis Direction of Each Component**

## 6. Conclusion

We construct the model to PUMA560 robot in ADAMS according to the structure parameters of PUMA560 robot, such as length, quality and inertia mass of the hinged arm. Using ADAMS dynamic analysis software to simulate the moving condition of mechanical arm, and obtaining the torque curves of each joint in the process of the movement, and analyzing the simulation results. It can be seen that the robot modeling and simulation approach which combines with ADAMS technology has the characteristic of good real-time and good visibility, it applies to kinematic simulation analysis of complex mechanical systems, and it is contribute to the design of the system optimization.

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