

# Control of an Induction Machine Coupled in a Two Tanks System

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## **Abstract**

*This article proposes the study and simulation of an induction machine supplied with a photovoltaic generator to ensure the designed volume control of two coupled tanks. We propose a sliding mode control technique to make the speed and the flux of the induction machine robust to parameter variations and control the volume of water containing in the second tank. The results of simulations of all the chain of conversion, carried out under MATLAB/Simulink software, made it possible to evaluate the performances of the proposed system.*

**Keywords:** *Sliding mode control, photovoltaic generator, coupled tanks, induction motor, MATLAB/Simulink*

## **1. Introduction**

The use of solar energy is the subject of the current investigation. Solar panels are the basic element in every photovoltaic system. They are composed of interconnected photocells. Each cell converts the rays from the sun into electricity through the photovoltaic effect. Photovoltaic panels have a specific electrical characteristic which is given by the manufacturer in the form of curves. In general, these curves represent the evolution of current and power depending on the panel voltage [1].

In this paper, we start by presenting the induction machine model alimented by photovoltaic panel. After that, we develop a control algorithm with variable structure for the sliding mode control of speed independently of flow with limitation of the current with a further switching path. Secondly, we will focus on investigating the volume control in the coupled tanks [9].

This document is presented as following: In section 2, the model of process is presented. Section 3 is devoted to control system. To validate the proposed approach, different simulation results are presented in Section 4.

## **2. Process description**

### **2.1. Induction motor**

The induction motor is now widely rumored to its well known qualities. However, the control of this machine is against more difficult than for other electrical machines because of the lack of natural flows and decoupling torque. Modeling this machine is an essential step for the development of his control [6]. An induction machine can be represented by three identical to the stator windings.

The equation of the machine is then written in the following form [3]:

$$[V_{s123}] = [R_s][I_{s123}] + \frac{d}{dt}[\Phi_{s123}]$$

$$[V_{r123}] = [R_r][I_{r123}] + \frac{d}{dt}[\Phi_{r123}] = 0$$

Noting that:

$$[\Phi_{r123}] = [\Phi_{r1} \quad \Phi_{r2} \quad \Phi_{r3}]^t$$

$$[I_{r123}] = [I_{r1} \quad I_{r2} \quad I_{r3}]^t$$

$$[V_{r123}] = [0 \quad 0 \quad 0]^t$$

$$[V_{s123}] = [V_{s1} \quad V_{s2} \quad V_{s3}]^t$$

$$[\Phi_{s123}] = [\Phi_{s1} \quad \Phi_{s2} \quad \Phi_{s3}]^t$$

$$[I_{s123}] = [I_{s1} \quad I_{s2} \quad I_{s3}]^t$$

$$[R_s] = \text{diag}(R_s); [R_r] = \text{diag}(R_r)$$

Hence:

$$[V_{sdq}] = [R_s][I_{sdq}] + \frac{d}{dt}[\Phi_{sdq}]$$

$$[V_{rdq}] = [R_s][I_{rdq}] + \frac{d}{dt}[\Phi_{rdq}] = 0$$

Where

$$[\Phi_{rdq}] = [\Phi_{rd} \quad \Phi_{rq}]^t$$

$$[I_{rdq}] = [I_{rd} \quad I_{rq}]^t$$

$$[V_{rdq}] = [0 \quad 0]^t$$

$$[V_{sdq}] = [V_{sd} \quad V_{sq}]^t$$

$$[\Phi_{sdq}] = [\Phi_{sd} \quad \Phi_{sq}]^t$$

$$[I_{sdq}] = [I_{sd} \quad I_{sq}]^t$$

$$\Phi_{ds} = L_s i_{ds} + L_m i_{dr} \quad \Phi_{qs} = L_s i_{qs} + L_m i_{qr}$$

$$\Phi_{dr} = L_r i_{dr} + L_m i_{dr} \quad \Phi_{qr} = L_r i_{qr} + L_m i_{qr}$$

$$L_s = l_s + L_m$$

$$L_r = l_r + L_m$$

$$P[\theta_s] \frac{dP[\theta_s]}{dt} = \omega_s \begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$$

$$P[\theta_s - \theta] \frac{dP[\theta_s - \theta]}{dt} = \omega_r \begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$$

$$\omega_s = \frac{d\theta_s}{dt}$$

$$\omega_r = \omega_s - \omega = \frac{d(\theta_s - \theta)}{dt}$$

The park model leads to several expressions of the electromagnetic torque  $C_{em}$  we retain:

$$C_{em} = n_p \frac{L_m}{L_r} (i_{qs} \Phi_{dr} - i_{ds} \Phi_{qr})$$

## 2.2. Coupled tanks system

This process behaves two vertical tanks coupled by a flow canal, a manual valve used to change the canal section, in consequently, to change the flow characteristics between the reservoirs [8]. A level sensor is installed at the top of every reservoir. The relation between the speed of the IM  $\Omega$  and the entry debit of the second reservoir  $q_2$  :

$$q_2 = a_1 \cdot a_2 \cdot G_p \cdot \Omega$$

The second reservoir can be filled from the first reservoir by the intermediary of the canal 1, while the debit of the second reservoir towards the first is assured by the canal 2. The equilibrated equation of the flow, for the first reservoir [9] is given by:

$$\dot{V}_1 = q_{21} - q_1$$

For the second reservoir:

$$\dot{V}_2 = q_2 - q_{21}$$

Such as:

$$q_1 = s_1 \cdot \sqrt{2gV_1}$$

$$q_{21} = s_2 \cdot a_0 \sqrt{2g(V_2 - V_1)}$$

Finally, the model of coupled tanks is:

$$\begin{cases} \dot{V}_1 = s_2 \cdot a_0 \sqrt{2g(V_2 - V_1)} - s_1 \cdot \sqrt{2gV_1} \\ \dot{V}_2 = a_1 \cdot a_2 \cdot G_p \cdot \Omega - s_2 \cdot a_0 \sqrt{2g(V_2 - V_1)} \\ y = k_s \cdot V_2 \end{cases}$$

### 2.3. Photovoltaic panel

An ideal photovoltaic cell is presented as an electric current generator which behavior is equivalent to a current source shunted by a diode which expression is [1] [2]:

$$I = I_{pv,cell} - I_d$$

$$\text{With: } I_d = I_{0,cell} \left[ \exp\left(\frac{qV}{aKT}\right) - 1 \right]$$

Where:

- $I_{pv,cell}$  : the current generated by the solar light, which is proportional to the irradiance (in A).
- $I_d$  : the diode current, given by Shockley law (in A).
- $I_{0,cell}$ : the leakage current of the diode (in A).
- $q$  is the electron charge which is equal to  $1,60217646 \cdot 10^{-19}$  C .
- $k$  is the Boltzmann constant, which is equal to  $1,3806503 \cdot 10^{-23}$  J.K<sup>-1</sup> ;
- $T$  is the temperature of the PN junction (K).
- $a$  is the ideality constant of the diode. Nearer the value is close to unity, the diode is considered ideal.

In the model "one diode" of a solar cell, the series resistance is due to the contribution of base resistances. The shunt resistance is the consequence of the surface along the periphery of the cell;

The current-voltage characteristic of an actual solar cell I-V is derived from the following equation:

$$I = I_{pv} - I_d - I_r$$

With:

$$I_r = \frac{V + R_s I}{R_p}$$

Where:

- $I_{pv}$  is the photo-cell current, which is proportional to the illumination G.

- $I_r$  is the leakage current through the shunt resistor.

$$I = I_{pv} - I_0 \left[ \exp\left(\frac{V + R_s I}{V_t a}\right) - 1 \right] - \frac{V + R_s I}{R_p}$$

Where:

- $R_s$  is the equivalent series resistance of the solar cell (in  $\Omega$ ).
- $R_p$  is the equivalent parallel resistance (in  $\Omega$ ).
- $V_t = \frac{N_s \cdot K \cdot T}{q}$  is the thermal potential of the photovoltaic module for  $N_s$  cells connected in series.

The photovoltaic generator was developed in Matlab/Simulink, for a set of  $N_s * N_p$  photovoltaic module.  $N_s$  and  $N_p$  are respectively the number of photovoltaic modules in series and in parallel. Each module is packaged here by  $N_s$  photovoltaic cells assembled in series. In general, a module may include sets of cells connected in series or in parallel to increase the tension and intensity produced respectively. Note also that a solar panel may be constituted by a set of modules comprising a defined number of cells.

### 3. Control system

#### 3.1. Sliding mode control current stator

The control law sliding mode must simultaneously satisfy the conditions of invariance and attractiveness. For this purpose, the switching function  $S(y)$  must satisfy [4] [5]:

-The invariance condition 
$$\begin{cases} S(y) = 0 \\ \dot{S}(y) = 0 \\ S(y) = 0 \end{cases}$$

- The attractiveness condition:

$$\begin{cases} \dot{S}_i(y) < 0 \rightarrow \text{if} \rightarrow S_i(y) > 0 \\ \dot{S}_i(y) > 0 \rightarrow \text{if} \rightarrow S_i(y) < 0 \end{cases} \rightarrow \text{for } (i = 0 \dots m)$$

These conditions lead to determining a new vector control:

$$u^* = u_{eq} + u_{att}$$

The vector control comprises two terms [7]:

- The first is the control vector specifying the equivalent control for the system to stay on the sliding surface.

- The second is the vector control that ensures the attractive control system outside the sliding surface. It also requires the system dynamics starting from an initial point until it reaches the sliding surface.

The indirect control by sliding mode stator current vector of induction machine ensures the calculation of direct and inverse components of the reference voltage vector expressed in the  $d-q$  plane. Therefore, each component  $U_{ds}^*$  and  $U_{qs}^*$  is composed by two terms. The first term is the equivalent voltage vector that is active in steady state, while the second term is the voltage vector which is attractive assets in transition.

$$\begin{cases} U_{ds}^* = U_{dseq} + U_{dsatt} \\ U_{qs}^* = U_{qseq} + U_{qsatt} \end{cases}$$

For trajectories currents  $i_{ds}$  and  $i_{qs}$  remained on their sliding surfaces ( $S_{ids} = 0$  and  $S_{iqs} = 0$ ), we apply the voltage vectors  $U_{dseq}$  and  $U_{qseq}$  on the axis  $d$  and axis  $q$ . These vectors can be calculated taking into account the following invariance conditions:

$$\begin{cases} S_{ids} = (i_{ds}^* - i_{ds}) = 0 \\ \dot{S}_{ids} = 0 \end{cases} \quad \text{and} \quad \begin{cases} S_{iqs} = (i_{qs}^* - i_{qs}) = 0 \\ \dot{S}_{iqs} = 0 \end{cases}$$

From this attractive voltage vector system of reference voltage vector involves the switching function derivative  $\dot{S}_{ids}$  and  $\dot{S}_{iqs}$ . A structure of attractiveness is chosen at a constant speed and proportional action, which gives:

$$\begin{cases} U_{dsatt} = Q_d \operatorname{sgn}(S_{ids}) + K_d S_{ids} \\ U_{qsatt} = Q_q \operatorname{sgn}(S_{iqs}) + K_q S_{iqs} \end{cases}$$

In summary:

$$\begin{cases} U_{ds}^* = L_s (\dot{i}_{ds} + \omega_s i_{ds} + Q_d \operatorname{sgn}(S_{ids}) + K_d S_{ids}) \\ U_{qs}^* = L_s (\dot{i}_{qs} + \omega_s i_{qs} + Q_q \operatorname{sgn}(S_{iqs}) + K_q S_{iqs}) \end{cases}$$

### 3.2. Sliding mode control speed of induction motor

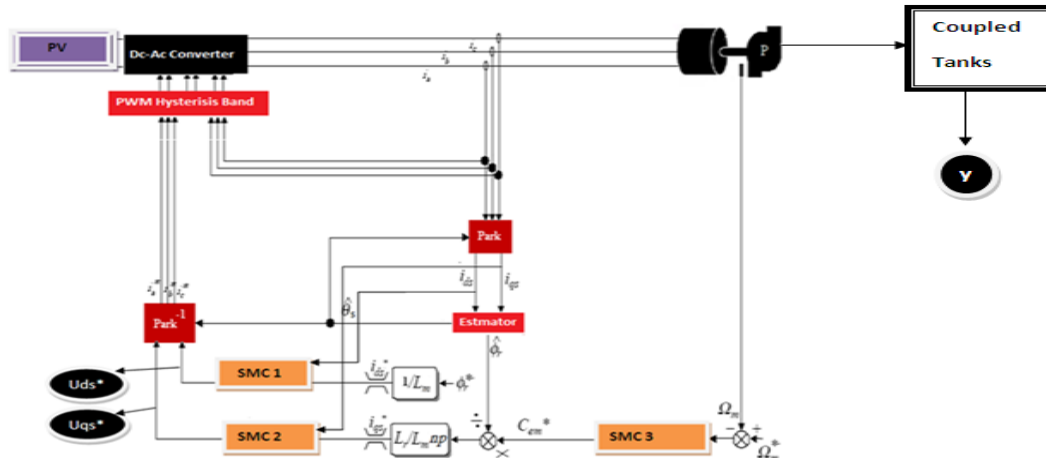
Addressing the same principle given by the preceding paragraph, we can construct the block allowing the control of the rotor speed [4]:

$$i_{qs}^* = i_{qseq} + i_{qsatt} = G_1 \Omega^* + G_2 C_r + G_3 (Q \operatorname{sgn}(S_\Omega) + K S_\Omega)$$

Where:  $G_1$ ,  $G_2$ ,  $G_3$ ,  $Q$  and  $K$  are positive constant related to the asynchronous machine.

## 4. Simulations Results

The operation of the entire environment was simulated under MATLAB<sup>®</sup>, Simulink<sup>®</sup>. The speed and flux references are respectively:  $X_{m0} = 2864.79$  rpm,  $U_{r0} = 0.93$  Wb. The initial volume of water in the second tank is  $V_2 = 0.2$  m<sup>3</sup>.



**Figure 1. Block Diagram Control of an Induction Machine Coupled in a Two Tanks System**

- The Asynchronous motor-pump is characterized by:

Numbers of poles: 2,  
Nominal voltage: 230/400 V,  
Nominal current: 1.6 A,  
Nominal power output: 750 W,  
Nominal frequency: 50 Hz,  
Total moment of inertia  $J$ : 0.0015 kg m<sup>2</sup>,  
Constant of pump torque  $K_r$ : 2.772 kg m<sup>2</sup> rd<sup>-1</sup>,  
Coefficient of friction  $F$ :  $3.44 \cdot 10^{-5}$  kg m<sup>2</sup> s<sup>-1</sup>,  
Stator resistance  $R_s$ : 10.621  $\Omega$ ,  
Rotor resistance  $R_r$ : 7 $\Omega$ ,

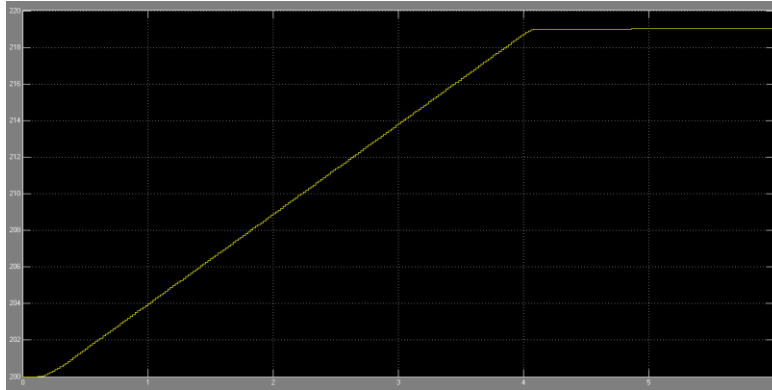
- The photovoltaic panel is characterized by:

Total cell in series in a module: 72,  
Resistance series: 2.7  $\Omega$ ,  
Shunt resistance: 1 M  $\Omega$ ,  
Short circuit current: 1.2 A,  
Open circuit voltage: 92 V,  
Ideality factor: 630,  
Number of Module in Series: 4,  
Number of Module in parallel: 1,  
 $T_r$  is the reference temperature = 298 K,  
 $G$  is the PV module illumination: 1000W/m<sup>2</sup>,

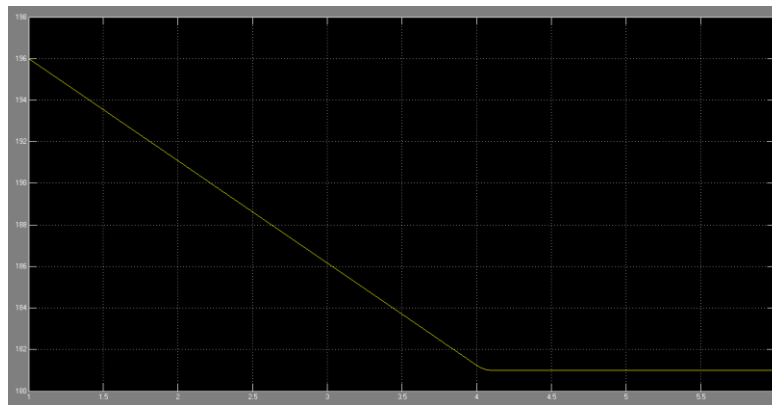
- The parameters of reservoirs:

Initial volume of water in both tanks:  $V_1=V_2=0.2$  m<sup>3</sup>  
Section of pipe  $s_1, s_2$ :  $7.9 \cdot 10^{-3}$  m<sup>2</sup>

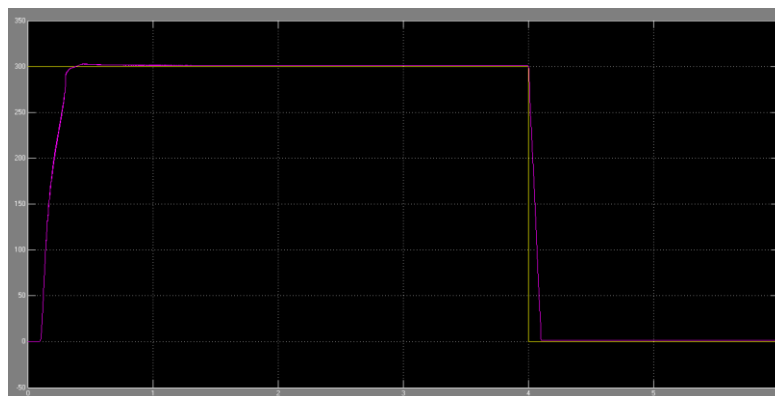
Coefficients landfills  $a_0, a_1, a_2 = 1$   
Gain pump  $G_p = 500 \text{ m}^3 \cdot \text{s}^{-1} \cdot \text{v}^{-1}$   
Sensor gain  $k_s = 24.5 \text{ v} \cdot \text{m}^{-1}$   
Gravitational constant  $g = 9.8 \text{ m} \cdot \text{s}^{-2}$



**Figure 2. Simulation Response of Water Volume in the Second Tank**



**Figure 3. Simulation Response of Water Volume in the First Tank**



**Figure 4. Simulation Response of Speed Induction Motor**



## 5. Conclusion

In this document, we have developed an adjustment method with a variable structure. This method includes the sliding mode approach to control the speed of the induction machine which is coupled to photovoltaic panel. The control of two coupled tanks is ensured by the speed variation.

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