Scheduling Tasks on Heterogeneous Multi-Core Processors Based on Modified Ant Colony Optimization

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Abstract

Traditional techniques of single CPU no longer fit the trend of big data processing and parallel computing environment. Accordingly, heterogeneous multi-core processors bring opportunities. However, task scheduling strategies on heterogeneous multi-core processors are not as mature as the hardware techniques. To this end, in this paper, we study on the task scheduling algorithm on heterogeneous multi-core processors. Specifically, we assume there exists dependence between tasks, and due to the different computing capabilities of processors, the workload on each processor should be considered as well. Therefore, we formulate the problem as to optimize the makespan and load balance of the whole task execution process, and propose a modified Ant Colony Optimization (ACO) algorithm to find the optimal solution. Experiments are also conducted for evaluation.

Keywords: Task Scheduling, Multi-Core Processors, Ant Colony Optimization

1. Introduction

With the increasing development of information techniques, applications of big data processing [1] and parallel computing [2] presents more requirements on the performance of processors. However, with the restrictions of integrated circuit techniques of single CPU, it is hard to improve the performance by increasing the frequency only. Accordingly, the development of multi-core processors [3-4] conforms to the trend.

However, as indicated by Amdahl law [5], there still remains problem in improving performance through increasing the number of processors on a single chip, since the overall system would be restricted to the sequential execution part of the computing. Besides, adding more cores to the same chip brings more energy burdens [6]. To this end, heterogeneous multi-core processors with different computing capabilities and structures can accelerate the execution of tasks by assigning them to appropriate processors.

Even though the hardware technique of processors architecture is mature, the task scheduling strategies on heterogeneous multi-core processors still need corresponding revolution. Therefore, in this paper, we study on the task scheduling problem on heterogeneous multi-core processors. Specifically, we assume there exists dependence between tasks, and the execution sequence influences the overall performance. Besides, due to the different computing capabilities of processors, the workload on each processor...
would be different as well. In order to achieve the best efficiency of the system, we also consider the load balance factor. Therefore, we try to optimize the makespan and load balance of the whole task execution process by scheduling tasks to proper multi-core processors.

Ant colony optimization (ACO) [7] is a swarm intelligence method to find approximate solutions to difficult optimization problems. The basic idea is to find the shortest path by the amount of pheromones released by ants on each trail. It has been proved that employing ACO for task scheduling problems is feasible [8-10]. In this paper, we modified ACO algorithm to schedule tasks on heterogeneous multi-core processors with the objective to optimize the makespan and load balance of the whole task execution.

The remain of this paper is organized as follows. Section 2 discusses the related work, and Section 3 describes the problem statement. In Section 4, the proposed task scheduling algorithm based on ACO is presented, and in Section 5 we conduct some experiments for evaluation. Finally, the paper is concluded in Section 6.

2. Related Work

Generally, related work can be categorized into two groups: task scheduling algorithms and efforts on ant colony algorithms.

Many efforts have been made on task scheduling, including clustering based [11], list based [12] and replication based [13] methods. For example, Yang et al., [14] proposed Dominant Sequence Clustering (DSC) algorithm keeps track of the critical path of the task graph and adjusts the critical nodes into one cluster. Critical Path Fast Duplication (CPFD) classifies three kinds of nodes with priorities: Critical Path Node (CPN), In-Branch Node (IBN) and Out-Branch Node (OBN), and then do the scheduling process. Kruatrachue et al., Proposed the Duplication Scheduling Heuristic (DSH) [15] algorithm with the consideration of intervals between the task execution and replication.

There are plenty of works on ant colony algorithms. For example, Seo et al., [16] employed ACO to solve the job scheduling problem in workshops. Zhang et al. [17] proposed an adaptive ACO to solve TSP problem, using evolution coefficient to evaluate the solutions of different ants. Ellabib et al., [18] designed a multi-ant system to solve the vehicle routing problem with time window. Yang et al., [19] employed multi-ant systems to solve the data clustering problem, where within each cluster, ants have different pheromones and transfer probabilities. Ghoseiri et al., [19] developed a multi-object ACO algorithm to solve the bi-objective optimization problem. Different from existing works, in this paper, we introduce idea from immune algorithm to improve the diversity of solutions and accelerate the search.

Besides, there are also some efforts on applying swarm intelligence algorithms to solve task scheduling problem in cloud computing environment. For example, [20] proposed to use genetic algorithm to schedule independent tasks in cloud computing environment. [21] designed a PSO based algorithm to optimize the communication and execution time. [22] tried to minimize the makespan using ACO algorithm. Different from above works, we aim to optimize the makespan as well as the load balance of the whole system with the improved ACO algorithm over the local optimal and low convergence phenomenons.

3. Problem Statement

Generally, the task allocation problem can be described as follows: we aim to find an optimal solution to assign \( n \) tasks onto \( m \) resources, in order to improve the overall performance. The metrics of evaluating the performance of the system include optimal makespan, Quality of Service (QoS), load balancing and economic principles [6]. In this paper, we consider the objective is to minimize the total makespan and also achieve load balance. The reason behind is the computing capability of resources in a heterogeneous
multi-core system varies, and the more balance the overall workload is, the more efficient the execution is.

Specifically, we assume the scope of our task scheduling problem is as follows. (1) The multi-core processors are heterogeneous, which means the computing capability varies for different processors and the scheduling method should consider the execution performance on each core. (2) We study on static scheduling only. That is, the number of tasks, communication cost between them, and the dependence relationship between data remain unchanged during the execution, and the assignment and execution sequence are deterministic. (3) There would be dependence and communication cost between tasks, and therefore the sequence of tasks execution as well as their time costs are significant for the overall system. Besides, the communication cost for tasks assigned to the same core is 0. (4) No preemption is allowed. That is, only one task is executed on one single core during one period of time, and one task can only be executed on one core at the same time. (5) We assume the decomposition and synthesis of tasks are performed by the cloud platform, and we only focus on the task assignment in this work.

Now we give the formulation of the task allocation problem. Suppose there are $m$ resources $R = \{ R_1, R_2, ..., R_m \}$ and $n$ tasks $T = \{ T_1, T_2, ..., T_n \}$. Let matrix $S_{mn}$ denote the execution time of each task on each resource:

$S = \{ s_{i,j} \}$ denotes the execution time of $T_i$ on $R_j : 1 \leq i \leq n, 1 \leq j \leq m \}.$

Besides, let $E_{mn}$ be the resource allocation matrix, that is,

$E = \{ e_{i,j} \}$ denotes if $T_i$ is allocated on $R_j$; if so, $e_{i,j} = 1$, otherwise, $e_{i,j} = 0; 1 \leq i \leq n, 1 \leq j \leq m \}.$

The objective is to find an optimal solution to achieve the best makespan and load balance. Suppose the sequence of task/resource is $X$, and the objective function can be defined as:

$F (X) = \min \{ w_1 \text{Makespan} (X) + w_2 \text{Load} (X) \},$

where $w_1$ denotes the weight of each dimension, and $\sum w_i = 1$, and the component in above equation adjusted so that the objective is minimum optimization. \text{Makespan} (X) is the makespan of the whole task sequence:

$\text{Makespan} (X) = \sum_{i=1}^{\infty} \sum_{j=1}^{\infty} C_i s_{i,j} e_{i,j},$

and \text{Load} (X) is the load factor of the resources:

$\text{Load} (X) = \sum_{j=1}^{\infty} \left[ 1 - C_2 \frac{Y_j}{L_j} \right],$

where $C_i, C_2$ are constants, $Y_j$ is the number of tasks assigned to resource $R_j$, and $L_j$ is the computing capability of $R_j$. 
4. Task Scheduling based on Modified ACO

4.1. Basics of ACO Algorithm

As shown in Figure 1, the principles of ACO can be explained through the double-bridge experiment conducted by Deneubourg et al. [23]. There are two designed routes in Figure 1-A, where the upper route is longer than the lower one. Two groups of ants are put at each end of the bridge, denoted as L and R respectively. At initial stage, since there is no pheromone heuristics, the decision at the cross is randomly made, as shown in Figure 1-B. After a while, more and more ants would select the lower route because it is shorter. Then, more pheromones are released on the lower route, which in turn increases the probability of being selected. Therefore, for new ants coming at the cross, they are more likely to choose the lower route, as shown in Figure 1-C and 1-D, where the dotted lines denote the amount of pheromones. Finally, with the accumulation of pheromones, almost all ants would be gathered on the lower route with the positive feedback mechanism.

The original ACO algorithm can be described as follows. Given a set of nodes \( N = \{1, 2, ..., n\} \), the connections between nodes are denoted as \( A = \{(i, j) | i, j \in N\} \), and the distance between nodes is expressed as a matrix \( D = (d_{ij})_{n \times n} \). The initialized value of pheromone on each path \((i, j)\) is \( \tau_{ij} = \frac{1}{|A|} \), where \( A \) is the length of \((i, j)\).

Suppose there are \( m \) ants starting from node \( i_0 \).

The workflow of ACO is as follows. If the termination condition is satisfied, the algorithm ends and output the best solution. Otherwise, ant \( x \) starts from \( i_0 \), and \( L(x) \) denotes the set of nodes \( x \) has passed. Initialize \( L(x) \) as an empty set, and \( 1 \leq x \leq m \).

When ant \( x \) arrives at node \( i \), if \( L(x) = \{l \mid (i, l) \in A, l \notin L(x)\} \) is empty, the journal of \( x \) ends. Otherwise, let \( I = \{l \mid (i, l) \in A, l \notin L(x)\} - \{i_0\} \). If \( I \) is not empty, then \( x \) would transfer to node \( j \) with the probability of \( p_{ij} \).
\[ p_\alpha(t) = \begin{cases} \frac{\tau_{xy}(t)}{\eta_{xy}}, & \text{if } j \in I; \\ \sum_{i \in I} \frac{\tau_{yi}(t)}{\eta_{yi}}, & \text{otherwise.} \end{cases} \]  

(6)

Where \( \alpha \) is the heuristic factor indicating the importance of path with remaining pheromones, and \( \beta \) is the heuristic factor denoting the affect of heuristic information between steps. And \( L(x) \) is updated as \( L(x) \cup \{ j \} \). If \( I \) is empty, which means ant \( x \) returns back to \( i_0 \), then update \( i \) as \( i_0 \) and starts over. The next step is to update the local best solutions and pheromones on the path. Denote the fitness evaluation function as \( f \), and the shortest path of \( m \) ants as \( y \). If \( f(L(y)) < f(W) \), where \( W \) is the last best solution, update \( W \) as \( L(y) \), and update the pheromones as follows:

\[ \tau_{xy}(k) = \begin{cases} (1 - \mu_k \lambda_k)(k - 1) + \frac{\mu_k \lambda_k}{|W|}, & (i, j) \in W; \\ (1 - \mu_k \lambda_k)(k - 1), & \text{otherwise.} \end{cases} \]  

(7)

where \( \mu_k \) is the decay coefficient, and \( 0 < \mu_k < 1 \). In this way, the amount of pheromones on \( W \) are increased, and the pheromones on other routes are decreased, so that the best solution is discovered. Algorithm 1 shows the process of ACO.

4.2. Modified ACO for Task Scheduling on Heterogeneous Multi-core Processors

However, there are some limitations on traditional ACO algorithms, such as long searching time, local optimum and the stagnation phenomenon. Moreover, the capability in a heterogeneous multi-core processors environment is full of diversity. To this end, we propose to introduce the idea of immune algorithm into ACO to suit our task scheduling problem. Figure 3 shows the overall flow chart of our modified ACO algorithm.

4.2.1. Coding: The length of chromosome is set as the number of tasks \( n \), and the genes on chromosome denote the sequence of task/resource pairs. For example, chromosome \( \{1.1.2.5, \ldots, m\} \) means that task \( T_1 \) is assigned to \( R_1 \), \( T_2 \) is assigned to \( R_1 \), \( T_3 \) is assigned to \( R_2 \), \( T_4 \) is assigned to \( R_5 \), and lastly \( T_n \) is assigned to \( R_m \). The set of tasks assigned to \( R_i \) is denoted as \( Y_j = \{T_1, T_2, \ldots, T_i\} \).
Algorithm 1 Ant Colony Optimization (ACO) Algorithm

1: Initialize the nodes $N = \{1, 2, \ldots, n\}$, resources $M = \{1, 2, \ldots, m\}$, ants $X = \{1, 2, \ldots, x\}$, connections $A = \{(i, j) | i, j \in N\}$, initial pheromone $\tau_{ij} = \frac{1}{|A|}$, and best solution $W = \{1, 2, \ldots, n\}$;
2: while Termination condition is not met do
3:   for Each ant $x$ do
4:     Initialize $L(x) = \emptyset$;
5:     for Each node $i$ in $N$ do
6:       Set $L(x) = \{l(i, l) \in A, l \not\in L(x)\};$
7:       if $L(x)$ is not empty then
8:         Calculate the transfer probability to next node $j$, $p_{ij}$;
9:         Update $L(x) = L(x) \cup j$;
10:     end if
11:   end for
12: end for
13: Denote the route of shortest path at current iteration as $y$;
14: Compute the fitness $f(L(y))$;
15: if $f(L(y)) < f(W)$ then
16:   Update $W = L(y)$;
17: end if
18: end while

Figure 2. Algorithm Description of Original ACO

4.2.2. Initialization: As mentioned before, the number of cores and computing capability of each processor are different. Therefore, we initialized the pheromone of each multi-core processor as follows:

$$\tau_{ij}(0) = c_{j} \times MIPS_{j},$$ (8)

where $c_{j}$ is the number of cores on $R_{j}$ and $MIPS_{j}$ is the computing capability of each core.

4.2.3. Vaccine extraction: In this step, ants with desirable qualities are acquired, and extracted as vaccine at some probability. The vaccine is used to improve the diversity of the population, in order to avoid local optimal solutions. The probability of ant $x$ on resource $i$ being selected as vaccine is:

$$p(x_{i}) = \frac{\sum_{j=1}^{m} |s_{j} - s_{i}|}{\sum_{j=1}^{m} \sum_{i=1}^{n} |s_{j} - s_{i}|}, i = 1, 2, \ldots, m,$$ (9)

where $s_{j} = \sum_{i=1}^{n} s_{i}$ denotes the total time of all tasks executed on resource $j$. 

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4.2.4. Transitivity: The transfer probability at iteration $t$ is calculated as Equation (6). In order to avoid the local optimal solution, we introduce a threshold of pheromone. That is, if the amount of pheromone $\tau_{ij}(t)$ is no more than $\tau_0$, the algorithm does not consider the influence from other nodes. Besides, we adjust $\mu$ if there is no improvement of the local solutions within $N$ iterations:

$$\mu_{t+1} = \begin{cases} 
0.95 \mu_t, & \text{if } 0.95 \mu_t \geq \mu_{\min}; \\
\mu_{\min}, & \text{otherwise.} 
\end{cases}$$

(10)

where $\mu_{\min}$ is the minimum value of $\mu$.

4.2.5. Immune: Perform immune operation by integrating the extracted vaccine into the gene coding.
4.2.6. Update Pheromone: Let $\tau_j(t)$ be the amount of pheromone on resource $j$ at time $t$, and we have

$$\tau_j(t + 1) = (1 - \mu)\tau_j(t) + \mu\Delta \tau_j,$$

where $\mu \in (0,1)$.

5. Experiment

5.1. Settings and Metrics

We use CloudSim [24] for simulating the heterogeneous multi-core processors environment, and each resource is actually a virtual machine. The proposed algorithm is implemented in MATLAB software. The parameter settings are as follows: $X = 50$, $\alpha = 1$, $\beta = 5$, $\mu = 0.6$.

In our experiments, we compare our modified ACO algorithm with original ACO and Round Robin (RR) algorithms. We design the comparison experiments with different CCR (Communicate-to-Computation-Ratio), calculated as:

$$CCR = \frac{\sum_{i=1}^{n} \sum_{j=1}^{m} c_{ij}}{\sum_{i=1}^{n} \text{avg}_j(s_i)},$$

where $c_{ij}$ is the communication cost between tasks, and $\text{avg}_j(s_i)$ is the average execution time of task $i$ on different resources.

Beside, we employ the following metrics for evaluation.

1. The scheduling length ratio (SLR), calculated as:

$$SLR = \frac{\text{makespan}}{CP},$$

where $\text{makespan}$ is the overall execution time of all tasks, and $CP$ is the critical path. The smaller $SLR$ is, the better the scheduling algorithm is.

2. Speedup, used to describe the parallel performance of task execution:

$$Speedup = \frac{\min\{\sum_{j=1}^{m} s_{ij}\}}{\text{makespan}},$$

where $s_{ij}$ is the time cost of task $i$ on resource $j$, and $\min\{\sum_{j=1}^{m} s_{ij}\}$ is the time cost of sequential execution of all tasks. The larger $Speedup$ is, the more efficient the
algorithm would be.

(3) Speed of convergence, which is a significant metric for swarm intelligence algorithms. The less iterations for global best solution, the more efficient the algorithm is.

5.2. Experimental Results

![Figure 4. Results of SLR Comparison](image1)

![Figure 5. Results of Speedup Comparison](image2)

Figure 4 shows the results of SLR for three algorithms. We can see that as the CCR increases, the value of SLR grows as well. The reason is that the more communication cost there is between tasks, the more execution time it costs for the scheduling. Furthermore, our modified ACO algorithm outperforms others, and RR performs worst. We can also conclude that employing swarm intelligence optimization method is efficient
for task scheduling.

As shown in Figure 5, the speedup for all three algorithms decreases when the CCR goes big. Indeed, more communication affects the parallelism of the whole system. Similarly, we can also observe that our modified ACO has the best speedup performance.

Figure 6 gives the results of convergence of our modified ACO and ACO algorithms. We can see that our modified ACO converges after approximately 40 iterations, while the ACO converges after 50 iterations. Therefore, our modified algorithm has faster speed of convergence compared to the original ACO algorithm.

![Figure 6. Results of Convergence](image)

6. Conclusion

In this paper, we propose a modified Ant Colony Optimization (ACO) algorithm with immune algorithm, and apply it on the task scheduling problem in heterogeneous multi-core processors environment. However, we focus on the static scheduling in this work. That is, we assume the number of resource nodes is determined beforehand, and the computing capability of each processor is deterministic as well. In future, we will try to extend the algorithm for dynamic task scheduling, and apply it to elastic computing.

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References

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