Maximum Power Point Tracking from a Wind Turbine Emulator Using a DC-DC Converter Controlled

Ruihong Yu, Yanqin Li and Jianxian Cai

Department of Disaster Prevention Apparatus, Institute of Disaster Prevention
East Yanjiao, Sanhe, Hebei, China, 065201
yuruihong97@sina.com

Abstract

Development and utilization of wind energy has become an important part of world sustainable energy development strategy. A control method realizing maximum power point tracking of wind turbine through adjusting the load characteristics was proposed in this article. The power management system based on DC/DC convertors was designed. The maximum power point tracker (MPPT) extracts maximum power from the wind turbine from cut-in to rated wind velocity by sensing only dc link power. The MPPT step and search algorithm in addition to the DC/DC are simulated using MATLAB-SIMULINK software. The results show that the DC/DC convertors topology can realize the maximum power point tracking control of the wind turbine.

Keywords: MPPT algorithm, DC/DC convertors, wind turbine system.

1. Introduction

Development and utilization of wind energy has become an important part of world sustainable energy development strategy. Wind power generation is the most important form of the development and utilization of wind energy. Wind power generation system can be divided into two categories that the constant speed constant frequency and variable speed constant frequency (VSCF). VSCF wind power generation system divided into two drive modes which is indirect and direct drive. The direct drive wind power system use the permanent magnet synchronous generator with low speed to transform the wind generator output power into alternating current which is frequency and constant voltage into the grid. So the system has the advantages of simple structure. It has become one of the main current of wind power generation.

The DC/DC converter is a core part of wind power maximum power point tracking controller. Its dynamic characteristics have an impact on the system. It is based on the theory of nonlinear dynamics system. Reference [1] using periodic switching model analysis of the hybrid dynamic characteristics of DC/DC converters, and study the system's controllability, observability and reachability; Reference [2] study on hybrid control problem of Boost power converter, through the design of hybrid control law for regulating output voltage of the converter; Reference [3] is based on sliding mode observer established hybrid system state model of DC-DC converter. Reference [4] uses the theory of hybrid systems, integration of two order DC-DC converter for hybrid system model; the system stability is analyzed based on the Lyapunov direct method, then put forward a new kind of sliding mode control strategy.

In this context, we will discuss about the basic knowledge of wind speed in Section 2 and the wind turbine model is proposed in Section 3. In Section 4, the wind turbine emulator
power electronics is presented. The model of maximum power controller and DC/DC converter is established in Section 5. Finally, the simulation and conclusion is made in the last section.

2. Basic Knowledge of Wind Speed

2.1 The distribution of wind speed

Numerical distribution model to describe the wind speed are two parameter Weibull distribution, three parameter Weibull distributions and Rayleigh distribution. Among them, two parameter Weibull curve fits the rule of wind speed distribution. It belongs to the unimodal normal distribution function, the probability density function:

\[
f(v) = \frac{k}{c} \left(\frac{v}{c}\right)^{k-1} e^{-\left(\frac{v}{c}\right)^k}
\]

Where the \( K \) is shape parameter; \( C \) is scale parameter. In the practical application, according to statistical data to determine the Weibull parameters of wind speed, then calculating the average wind speed \( \bar{v} \) and standard deviation \( \sigma \).

The expression for the follow function:

\[
\bar{v} = \frac{1}{n} \sum_{i=1}^{n} v_i
\]

\[
\sigma^2 = \frac{1}{n} \sum_{i=1}^{n} (v_i - \bar{v})^2
\]

Based on the mean and variance of the Weibull distribution approximation formula, we can get:

\[
\tau = \int_{\bar{v}}^{\infty} \left(\frac{v}{c}\right)^{k-1} e^{-\left(\frac{v}{c}\right)^k} \, dv = c \Gamma(1 + \frac{1}{k})
\]

\[
k = (\frac{\sigma}{\bar{v}})^{-1.086}
\]

Where

\[
\Gamma(a) = \int_{0}^{\infty} t^{a-1} e^{-t} \, dt
\]

2.2 The related factors of Rated wind speed

At present, the method for determining the rated wind speed can be expressed as

\[
v_r = c \left(\frac{k + 2}{k}\right)^{\frac{1}{3}}
\]

2.2.1 The relationship between the rated speed and rated power

The rated power of the wind power generator is:

\[
P = \frac{1}{2} \rho A \bar{v}^3 C_p
\]

Where, the \( \rho \) is air density; \( A \) is the rotor rotational area’s is the power coefficient. The formula (7) shows that the rated power and rated wind speed is proportional to \( 3 \) times, it also related to the local density of the air, the wind area and power coefficient.
2.2.2 The relationship between wind speed and the rotor diameter

The Rated power of wind generator is

\[ P(v_r) = \frac{1}{8} \eta \rho \pi d v_r^3 \]

Where, the \( \eta \) is efficiency, and \( d \) is rotor diameter.

The relationship between the rotor diameter and the rated wind speed is:

\[ d = 2 \sqrt{\frac{2P(v_r)}{\pi \rho C_p v_r^3}} \]

The formula (9) shows that appropriately increasing the rated wind speed can reduce the rotor diameter. But with the rotor diameter increases, the weight of hub will increase.

3. Wind Turbine Model

The model of the WT employed in the system includes the nonlinearities and dynamics of a realistic wind turbine. In this research, the dynamics of the furling action and rotor are incorporated.

![Figure 1. Block diagram of the Wind Turbine Emulator system](image)

Rather an inertia disk was added to the system to represent the inertia of the wind turbine rotor. A wind turbine can be characterized by the non-dimensional curve of power coefficient \( C_p \) as a function of Tip-Speed Ratio (TSR) \( \lambda \), where, \( \lambda \) is given in terms of rotor speed, \( \omega_r \), (rad/s), wind speed, \( v \) (m/s), and rotor radius, \( R_{in} \) as

\[ \lambda = \frac{R_{in} \omega_r}{v} \]

The relationship between \( C_p \) and \( \lambda \) is typical and can be approximated by a quadratic equation. In this research, the curve was obtained from the literature [5]. A model for \( C_p \) as a function of \( \lambda \) was calculated and the curve generated by the approximate model and the actual data are presented in Figure 2(a). Statistical analysis showed that the \( R^2 \) value of the model was 99.8% and goodness of fit was less than 0.0001, which shows that the predicted model for \( C_p \) with the fitted coefficients is acceptable.

The resulting equation was found to be:

\[ C_p(\lambda) = 0.000056\lambda^4 - 0.005\lambda^3 + 0.105\lambda^2 - 0.4\lambda + 0.25 \]
The curve between wind speed and furling angle was derived from published data [6, 7]. An approximate model was used to determine the relation between wind speed and furling angle and found that a fifth order model is sufficient to represent the relationship. The actual data and approximated model curve are represented in Figure 2(b).

**Figure 2.** (a) Power coefficient as a function of tip-speed ratio; (b) Furling angle versus wind speed

### 4. Wind Turbine Emulator Power Electronics

To represent the WT rotor, a separately excited DC motor was used because DC drive can operate more accurately at low speeds, thus ensuring accurate emulation at low wind speeds. The PC based controller triggers the phase controlled relay through a LabMaster I/O board. An inertia disk was coupled to the synchronous generator. It represents the inertia of a real wind turbine rotor. A complete schematic of the wind turbine section of the emulator is shown in Figure 3 [8, 9].

**Figure 3.** Schematic of the wind turbine section of the emulator
5. Maximum Power Controller and DC/DC Converter Controller

According to the formula 7, curve as shown in Figure 4 for the wind turbine output power P and speed w under different wind speeds. Each wind speed has a maximum power point. These maximum power points are connected by a curve. Then we can get the maximum power curve of wind turbine. At each point of the maximum power curve, the changes in wind turbine output power relative to change of the speed is zero.

![Figure 4. Typical power versus speed characteristics of a wind turbine](image)

At this time, the wind turbine output power can be expressed as

\[
\frac{dP}{d\omega} = 0
\]  

(12)

From Figure 4 we can also know, through the mediation of the rotating speed of the wind wheel can mediate the maximum output power. In order to achieve this goal, we have through the mediation of DC converter to change the load characteristics of wind turbine, and mediation rotate speed of wind. Then the wind turbine output power can track the maximum power. This is based on the circuit theory: when the external load equivalent impedance and power source internal impedance conjugate, external load can get the maximum output power [10-12]. The main circuit of the DC converter is composed of inductor, switch, rectifier diode and a filter capacitor which is a series in the loop. It transforms the impedance by controlling the duty ratio. Not only it can complete the voltage transformation, but can change input impedance of the DC converter [13-16].

The input voltage, output voltage and the duty ratio of the DC converter will be express in following formula:

\[
D = 1 - \frac{V_{in}}{V_{out}}
\]  

(13)

Where, the \(D\) is duty ratio of the DC converter, \(V_{in}\) is input voltage of the DC converter, and \(V_{out}\) is output voltage of the DC converter.

We transform the formula (13) as below:

\[
\frac{dP}{d\omega} = \frac{dP}{dD} \cdot \frac{dD}{dV_{in}} \cdot \frac{dV_{in}}{d\omega} \cdot \frac{d\omega}{d\omega} = 0
\]  

(14)

Where, the \(\omega\) is the angular velocity of the generator.
At the same time, the following relationship has established:

\[
\frac{dD}{dV_n} = \frac{1}{V_{om}} \\
\begin{align*}
&\neq 0 \\
&\text{(15)}
\end{align*}
\]

There is proportional relationship between the input voltage of DC converter and generator EMF, therefore, we can get:

\[
\frac{dV_n}{d\omega} \neq 0 \\
\begin{align*}
&\text{(16)}
\end{align*}
\]

From the formula (14) to (16), we can get:

\[
\frac{dP}{d\omega} = \frac{dP}{dD} = 0 \\
\begin{align*}
&\text{(17)}
\end{align*}
\]

So, we can prove the theory that through the mediation of DC converter duty ratio to achieve the maximum power tracking control of the wind turbine.

In order to extract the maximum power, an optimum TSR control was selected. The actual TSR of the wind turbine was compared with the optimum TSR and the microcontroller controlled the duty ratio of the buck-boost converter in order to control the effective dump load connected to the system. The basic structure of the maximum power extractor is shown in Figure 5 and Figure 6.

![Figure 5. Structure of the maximum power point extractor](image)

![Figure 6. Maximum power tracking process](image)
6. Simulation

The MATLAB Simulink model of the Wind Turbine Emulator system is first presented. Simulation results with the MPPT in addition to the comments will then be given for two wind speeds 6, 8 and 10 m/s. The electric machine and the dc-to-dc converter parameters are given in Appendix. It is noticed from Figure 10 that the controller is able to search for maximum power and keep the power coefficient of the wind turbine is much closed.

![Graphs showing wind speed, inverter phase A current, and tip-speed ratio over time.]

Figure 7. MPPT for a step change in wind speed
Figure 8. Simulation results for wind speed 6 m/s
Figure 9. Simulation results for wind speed 8 m/s
Figure 10. Simulation results for wind speed 10 m/s
7. Conclusions

The system maximum energy capture characteristics are simulated in Matlab / Simulink environment. The simulation results show that, by controlling the DC converter can realize the goals that wind turbine output power tracking the maximum theoretical power. Wind turbine power coefficient and duty ratio has remained near the optimal value in system design. This has fully demonstrated the correctness of the wind power energy management system and the feasibility of control strategy of maximum power point tracking in this article.

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References

Authors

Ruihong Yu. She received her B.Sc. in electrical engineering and automation (2002) from School of Electrical Engineering of Shandong University, China. And she received her M.Sc. in electric power system and automation (2006) from Xihua University, China. Now she is a Lecture with the Department of Disaster Prevention Instrument, Institute of Disaster Prevention, Hebei, CN. Her current research interests include automatic control, detection technology and automatic equipment.

Yanqin Li. She received her B.Sc. in electrical information engineering (2004) from department of Electrical Engineering of Taiyuan Science Institute, China. She received her M.Sc. in electricity and system (2007) from Taiyuan University of technology, China. Now she is a Lecture with the Department of Disaster Prevention Instrument, Institute of Disaster Prevention, Hebei, CN. Her current research interest is blind signal processing.

Jianxian Cai. She received her M.Sc. in control theory and control engineering (2003) from Yanshan University, China, and received PhD in pattern recognition and artificial intelligence (2010) from Beijing University of Technology, China. Currently, she is associate professor with the Department of Disaster Prevention Instrument, Institute of Disaster Prevention, Hebei, CN. Her main research interests include automatic control, robot intelligent control and machine learning.